

Rock Mechanics and Radioactive Waste Isolation.
“One small step for geology, one giant leap for rock mechanics”

Fourth Müller Lecture

presented by

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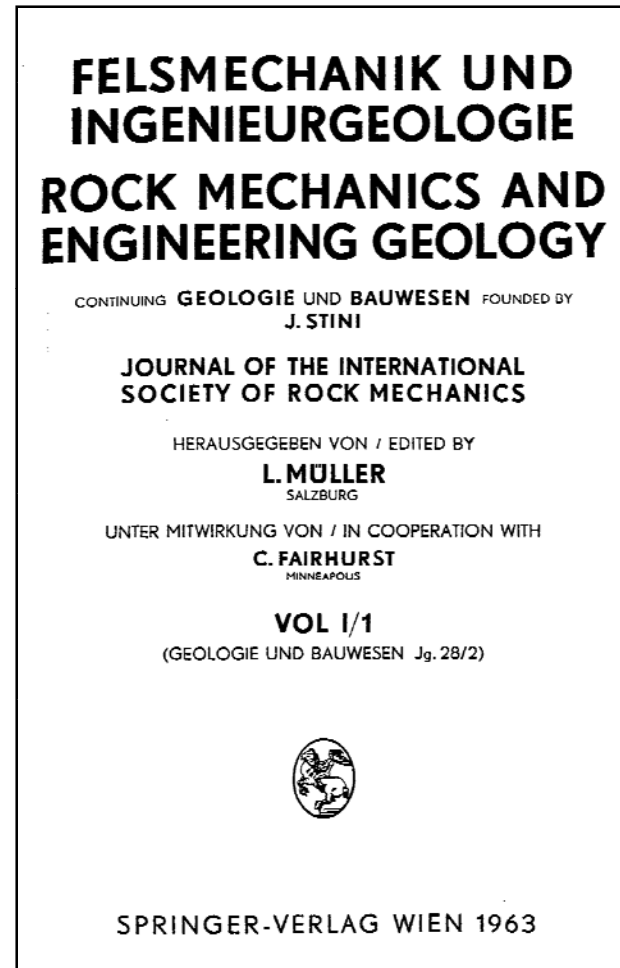
Tenth Congress of the International Society for Rock Mechanics
Sandton, South Africa, September 8-12, 2003

International Society for Rock Mechanics

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- 19 - Prof. A. Watznauer, East Germany
- 20 - Prof. Charles Fairhurst, USA

Journal



Ph.D. degrees in Rock Mechanics, University of Minnesota (1960-2003) & Departmental Colleagues & Associates

1960-1969:

Paul Gnirk
Bezalel Haimson
William Hustrulid
Hassan Imam
Herbert Kutter
William Pariseau
Hilmar von Schoenfeldt
Wolfgang Wawersik

1990-present:

Jose Adachi
Margaret Asgian
Nathali Boukpeti
Ilya Berchenko
Bjorn Birgisson
Mark Board
Roberto Carbonell
Carlos Carranza-Torres
Fernanda Carvalho
Liangsheng Cheng
Branko Damjanac

1970-1979:

Francois Cornet
Steve Crouch
Jaak Daemen
Michael Hardy
John Hudson
Darrell Porter
Jean-Claude Roegiers
Raymond Sterling
Ed Van Eeckhout
Michael Voegele

Ali Fakimi
Dimitri Garagash
Matt Handley
Haiying Huang
Mark Larson
Chengho Lee
Marc Loken
Mark Mack
Sanchai Maitaim
Lee Petersen
Thomas Richard

1980-1989:

Gary Callahan
Christine Detournay
Emmanuel Detournay
Roger Hart
Jose Lemos
Ernest Lindner
Loren Lorig
Panos Papanastasiou
Samuel Sharp
Yongjia Wang

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Randall Barnes
Barry Brady
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Neville Cook
Peter Cundall
Andrew Drescher
Bojan Guzina
Joe Labuz
Tom Lang
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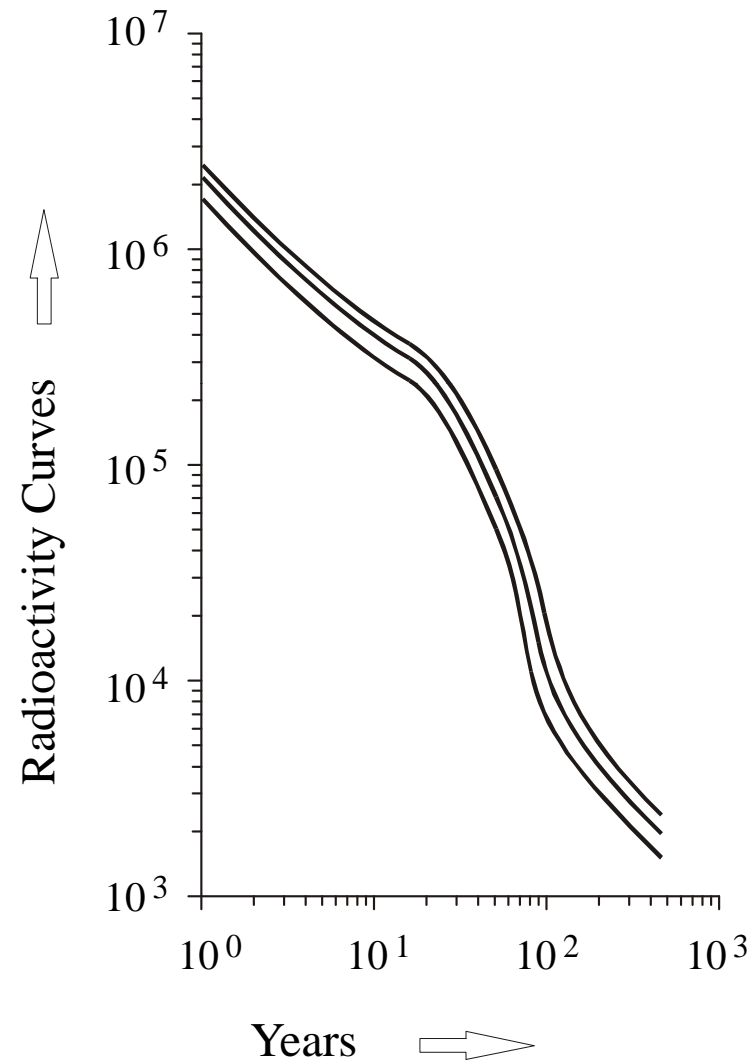


The problem. Waste Decay

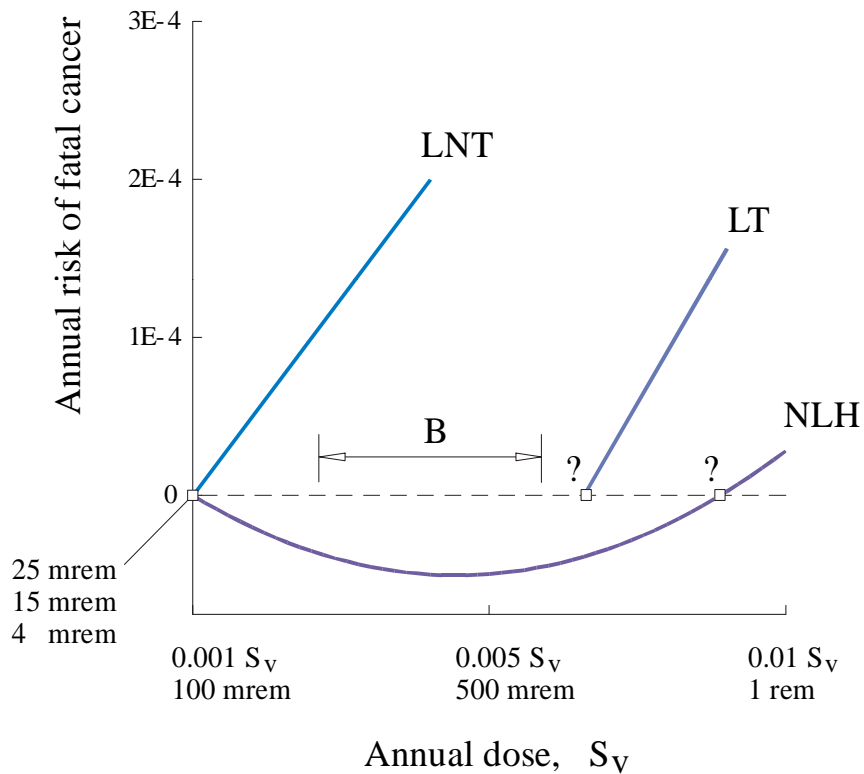
- Contains the byproducts of fission reactions.
- Is highly radioactive.
- Must be isolated from the public for many thousands of years.

Needed 1 million year radionuclide 'container'

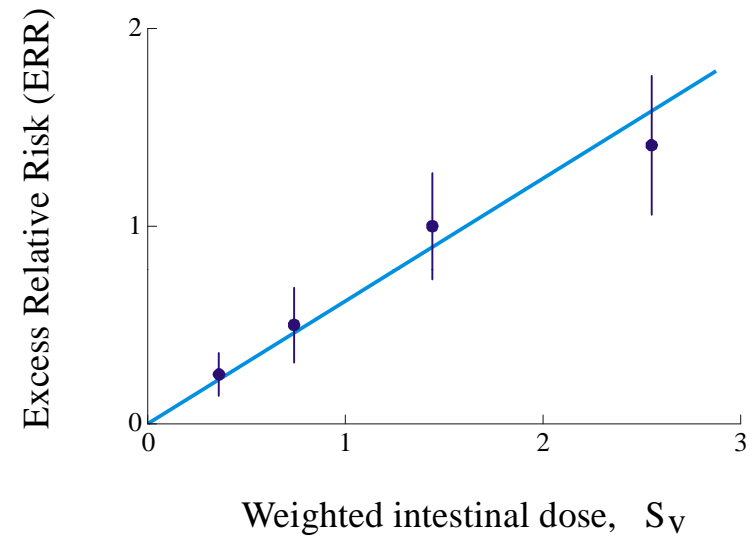
Geological Isolation?



Alternative hypothetical extrapolations of cancer death rate curves from high to low radiation dose rates



Dose-response relationships for solid cancer, all types combined, in atomic bomb survivors, 1958-1987 (from UNSCEAR, 1994)

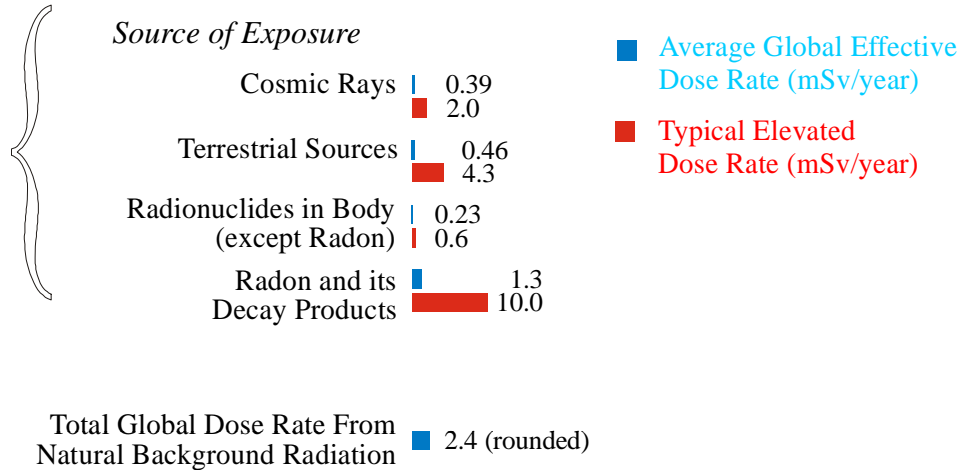


- LNT Linear, no threshold
- LT Linear, threshold
- NLH Non-linear, Hormesis
- B Range of natural background radiation in U.S. (approximate)

Radiation Risk and Waste Isolation Standard. LNT and Natural Background

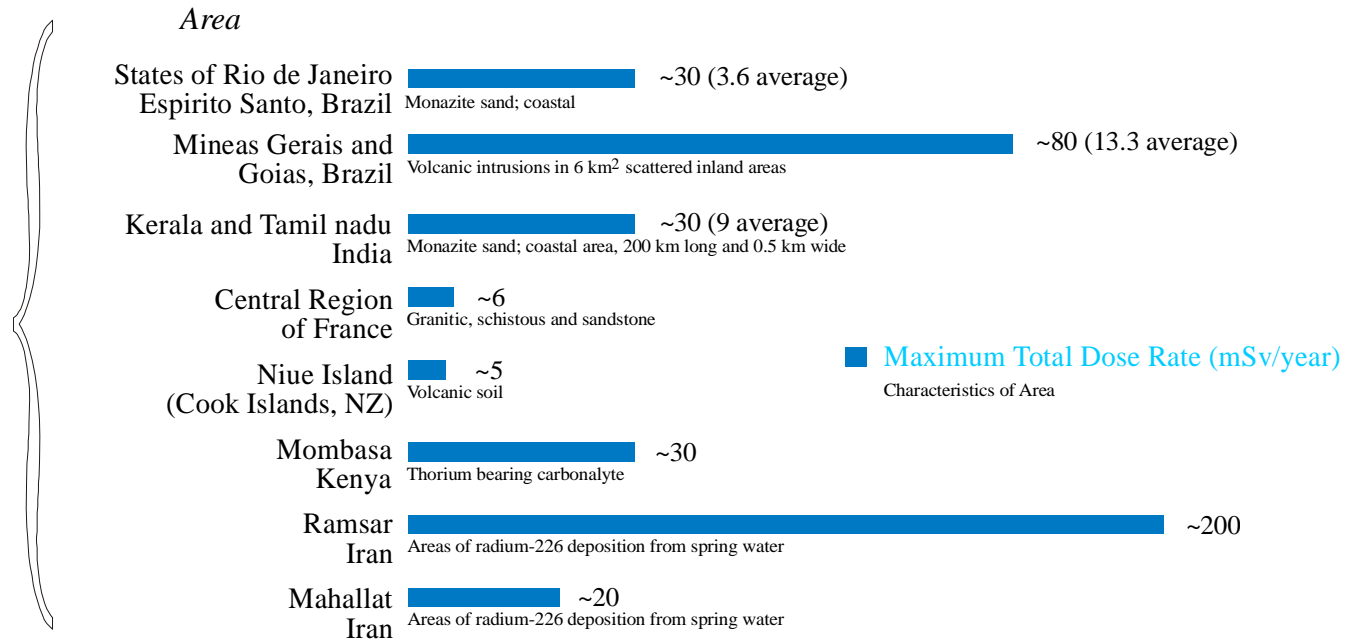
Risk of death from radiation

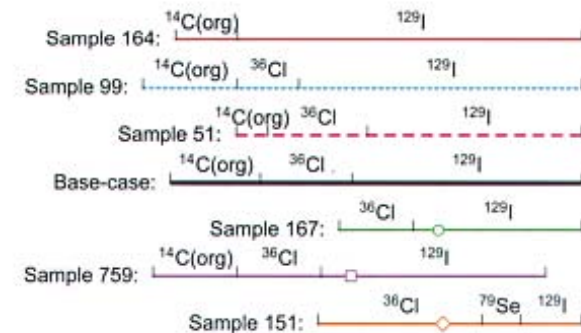
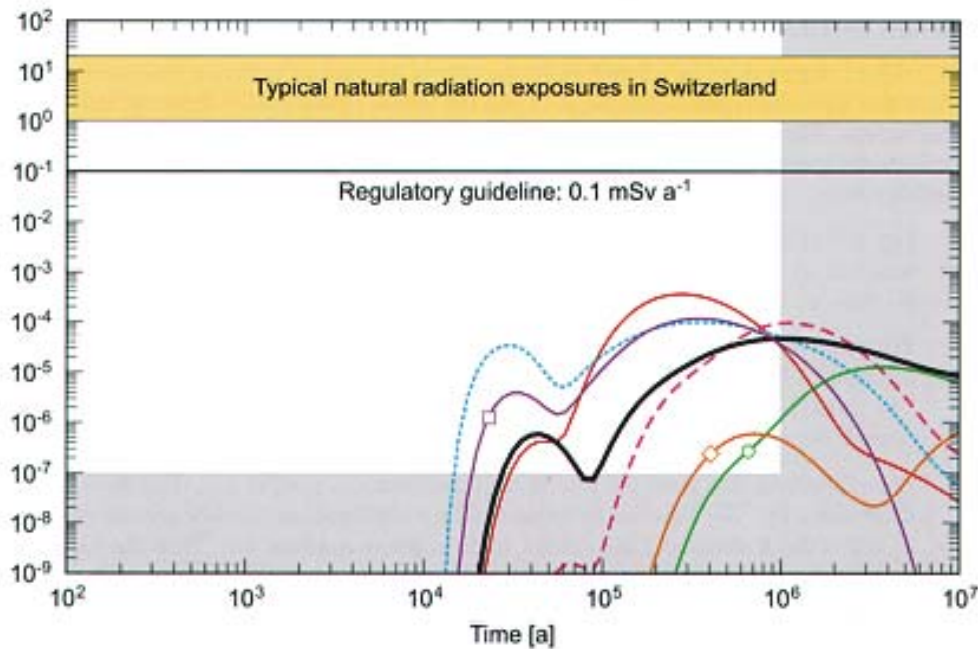
Global
Dose rates
from Natural
Background
Radiation



Reference:
ICRP, 1999. "Protection of the Public in Situations of Prolonged Radiation Exposure," Publication 82, Annals of the ICRP, Vol. 29, Nos. 1-2, International Commission on Radiological Protection, Pergamon Press, New York, NY. Table A.1, page 73, and Table A.2, page 74.

Examples of
Areas with
High Natural
Background
Dose Rates



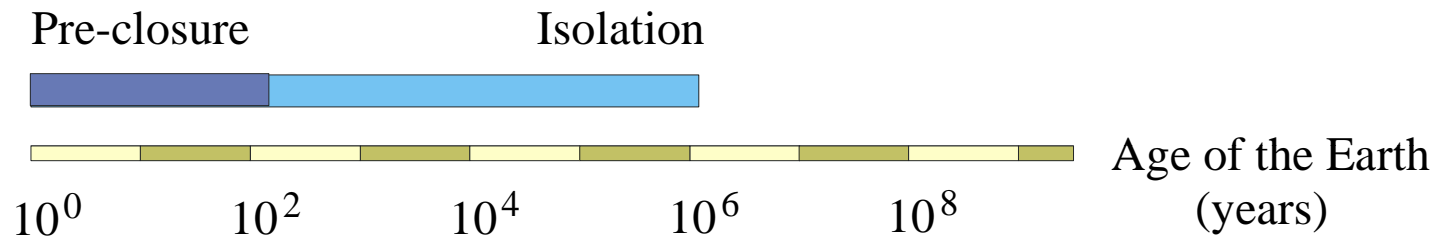


Dose as a function of time, for SF, for a number of different realisations, including those that gave the highest (sample 164) and the lowest (sample 151) dose maximum out of 1000 realisations.

The Base Case is included to allow an easy comparison. The other curves represent realisations that give the highest dose maximum or the lowest dose maximum in the period between 10^4 and 10^5 years or 10^6 and 10^7 years, respectively. The bars beneath the graph indicate the radionuclides that make the highest contribution to dose at any particular time.

Predicted Performance of a Repository in Opalinus Clay Spent Fuel
—from *NAGRA Technical Report 02-05*, p.229

“One small step for geology, one giant leap for rock mechanics”



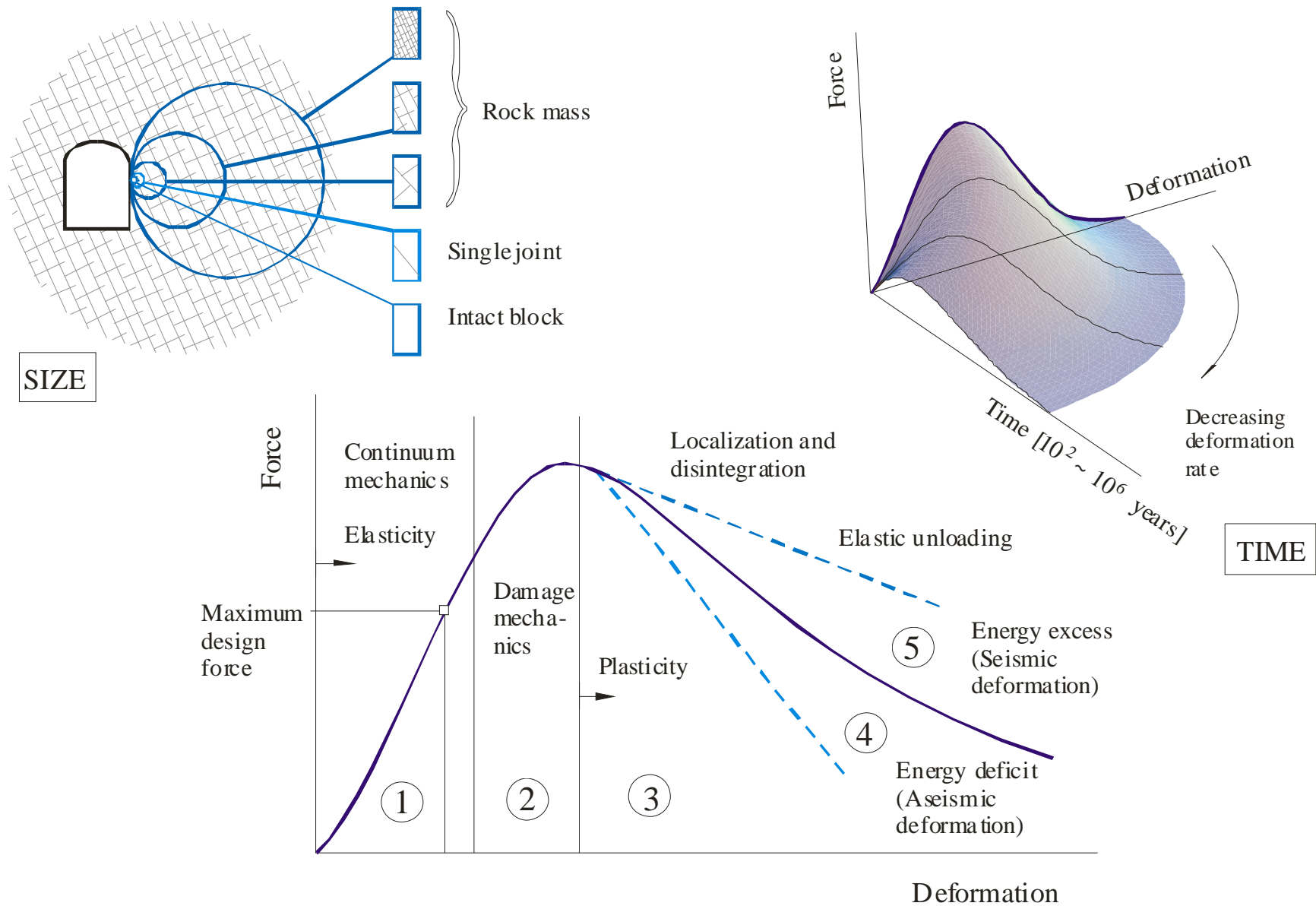
- Engineering Problem

Unprecedented Period of Time

Requires Improved Scientific Base

Periods of Isolation. Geological Isolation Time Scales.

“We don’t know the rock mass strength. That is why we need an International Society” Muller, 24 May 1962



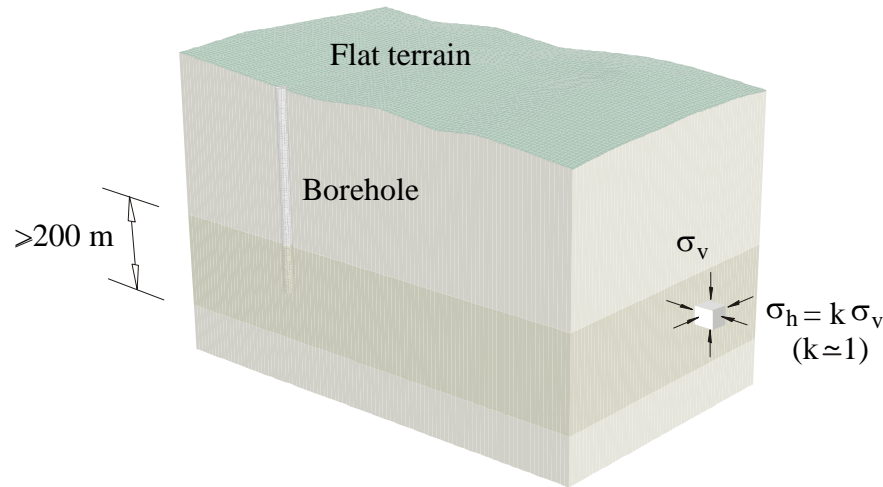
“In the field of geomechanics, granular media and block-jointed rock masses are obvious examples where the concept of the ideal physical continuum –one in which no gaps are formed– cannot be expected to apply... The clastic model offers an alternative approach.

Indeed, it is this writer’s view that only with clastic models or some further development thereof can the problem of predicting the complete load-deformation behaviour of solids be tackled optimistically.”

D.H. Trollope (1968)

Geological Isolation

Choose a geologically simple, stable site!
(low tectonic strain rate)



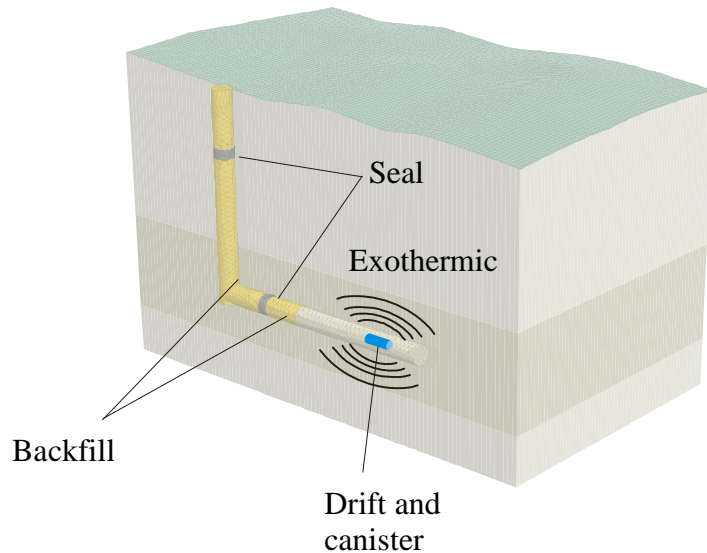
Overlying and underlying strata:

- Infrequent joints/faults.
- Far-field stresses close to isotropic.
- Groundwater discharge to large body of non-potable water (ocean, sea).

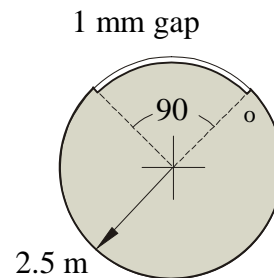
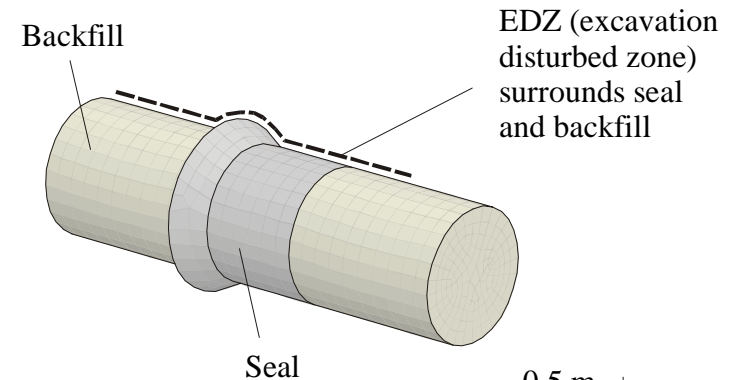
Repository stratum, simple host medium::

- Low permeability.
- Low hydraulic gradient.
- High ion-exchange potential.

Establish and close the repository



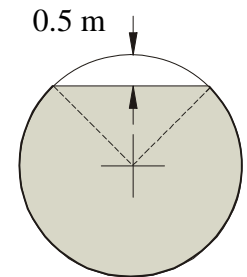
Detail of seal and backfill



Hydraulic Conductivity

$$K_{\text{no gap}} \sim 10^{-9} \text{ m/s}$$

$$K_{\text{1mm gap}} \sim 10^{-3} \text{ m/s}$$



Compaction (6%) due to particle friction reduction after $t \sim 10,000$ years

Rock Type	Rock Characteristics				
	Permeability	Ion Exchange	Thermal Conductivity	Strength	Ductility
Clay	Very Low ₊	Very High ₊	Low ₋	Low ₋	High ₊
Salt	Impermeable ₊	None ₋	High ₊	Low ₋	High ₊
Crystalline	Matrix Low ₊	Usually None ₋	Variable _o	High ₊	Low ₋
	Fractures High ₋				
Volcanic Tuff	High _o	High ₊	Low ₋	Low ₋	Moderate _o

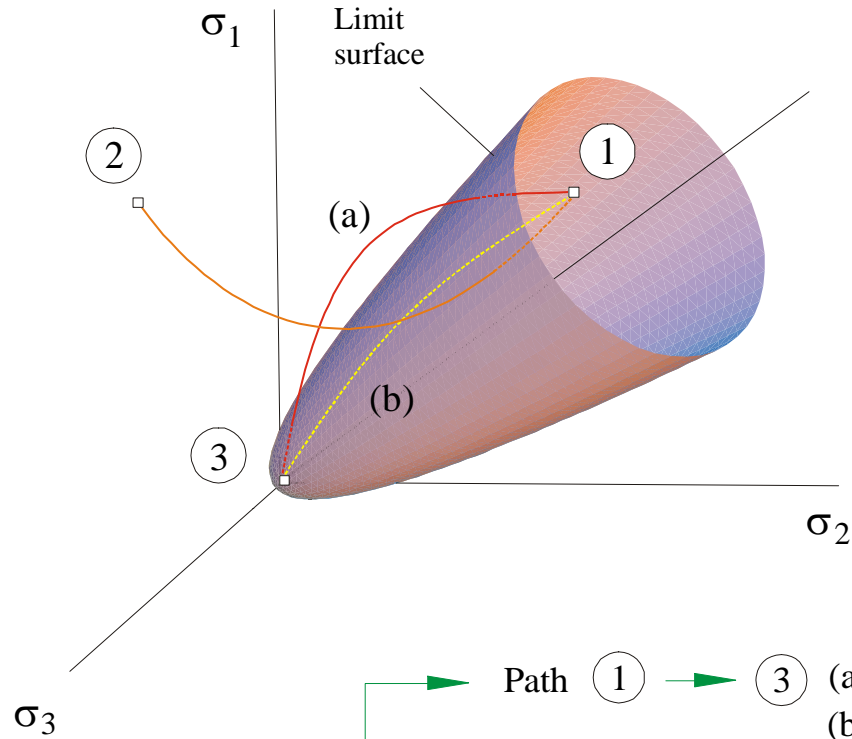
Current Research (and Operational) Sites

Clay	Indurated	Bure, France Mont Terri, Switzerland	} Below water table: Reducing environment.
	Non-Indurated	Benken, Switzerland	
Salt	Domal	Mol, Belgium Gorleben, Germany	
	Bedded	WIPP, Carlsbad, NM, USA (intermediate level operational)	
Crystalline	Unfractured Granite	Pinawa, Manitoba, Canada	} Above water table: Oxidizing environment.
	Fractured Granite	Aspö, Sweden, Finland (construction approved May 2002)	
Volcanic Tuff			
		Yucca Mountain, NV, USA (license application construct Dec 2004)	

Preferred Repository Host Rocks and Current Research Sites

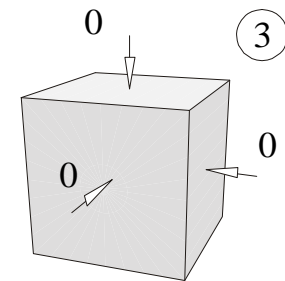
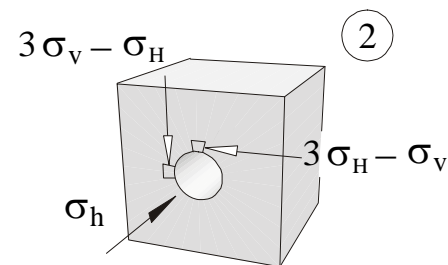
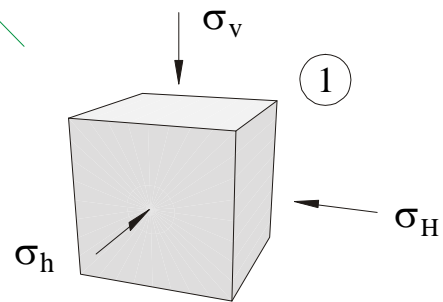
Some specific issues

- Rock testing (and prediction)
 - *samples* → *coring, slotting*
 - *full scale* → *underground excavations*
- Excavation technology
- Excavation damage
- Time dependent deformation /rock mass strength
- Transparent earth



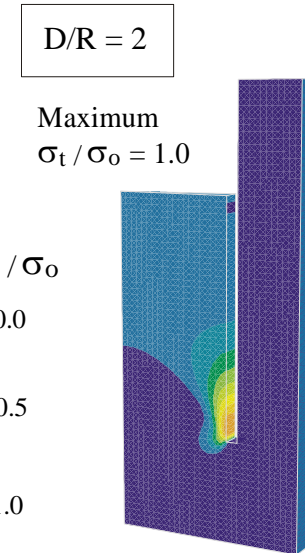
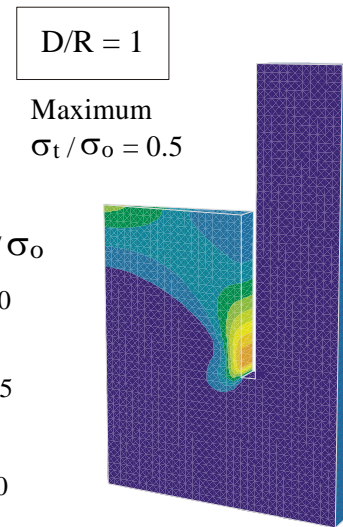
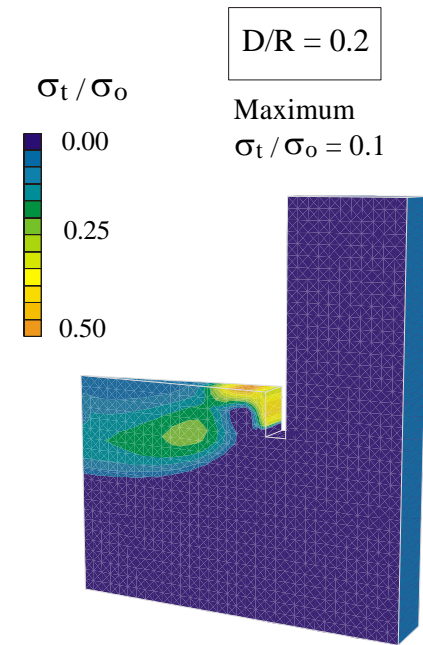
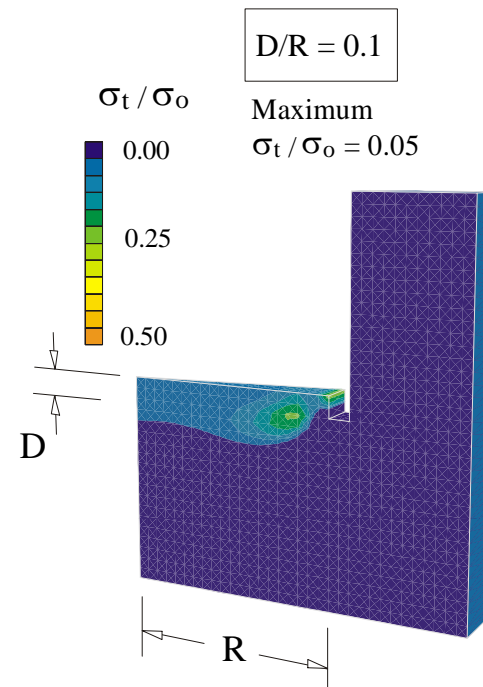
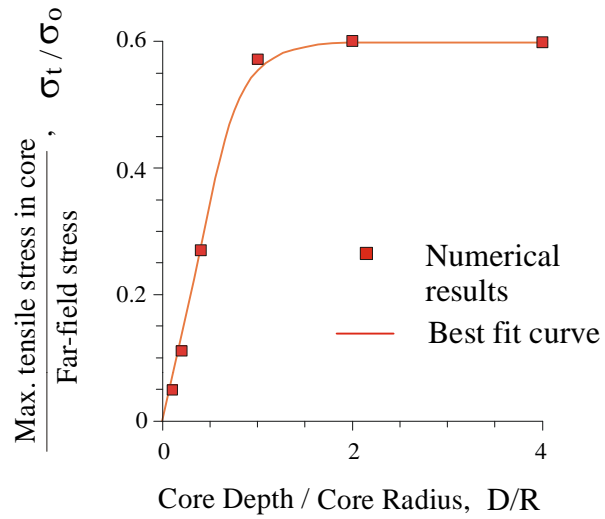
Unloading path effects on coring,
slotting and underground excavation

Path ① → ③ (a) Coring (surface or underground)
(b) Slotting (block center)



Path ① → ② Underground excavation

Potential for core damage during coring operation



Let $n = \frac{\sigma_t}{\sigma_c} = \frac{\text{tensile strength}}{\text{compressive strength}}$
 $[n \sim 0.1]$

Let $m = \frac{\sigma_t^i}{\sigma_o} = \frac{\text{induced tension in core}}{\text{in-situ horizontal stress}}$
 $[m \sim 0.5]$

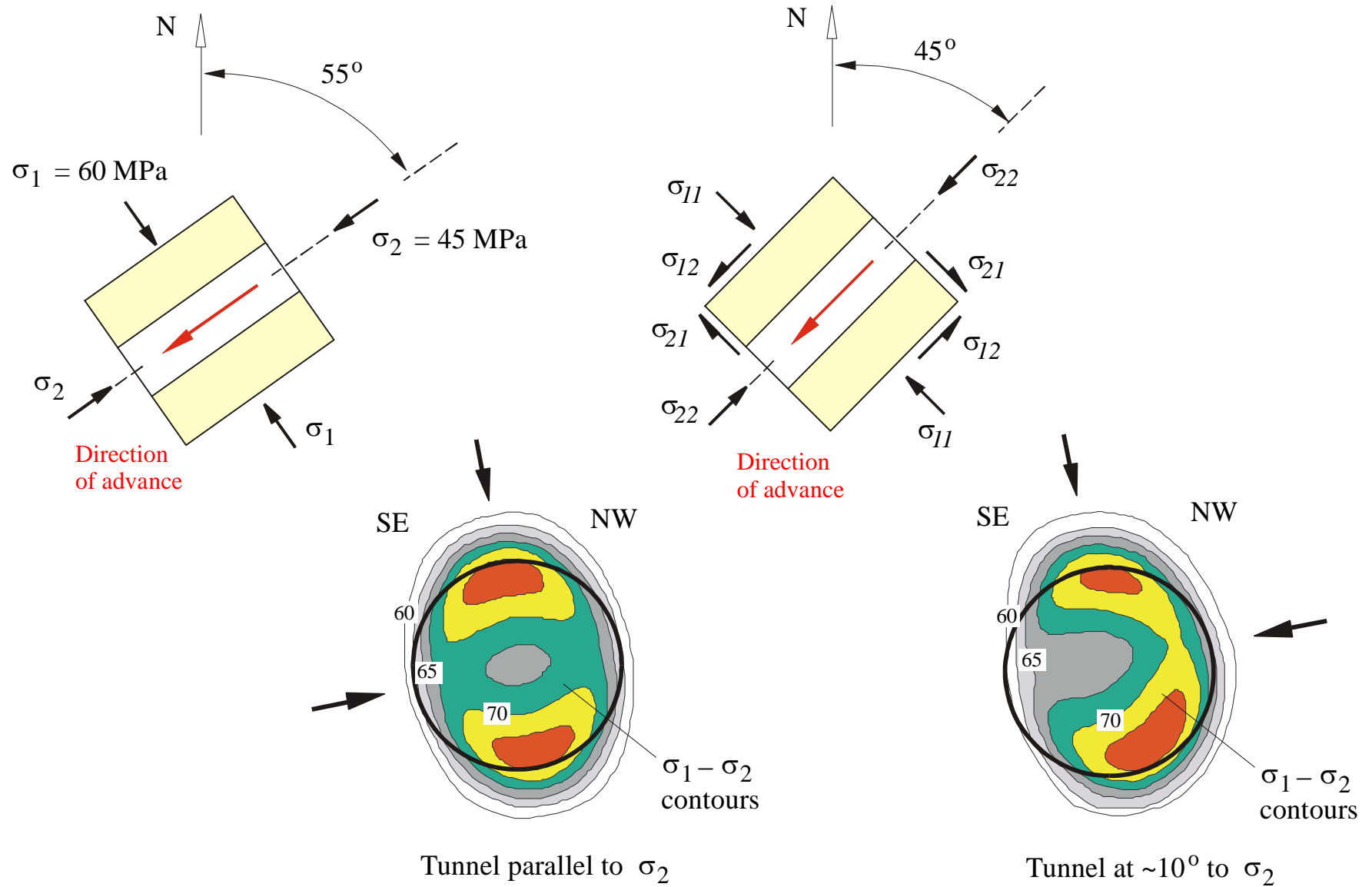
Then core damage occurs if

$$\sigma_o > n/m \sigma_c$$

i.e., $\sigma_o > 0.2 \sigma_c$

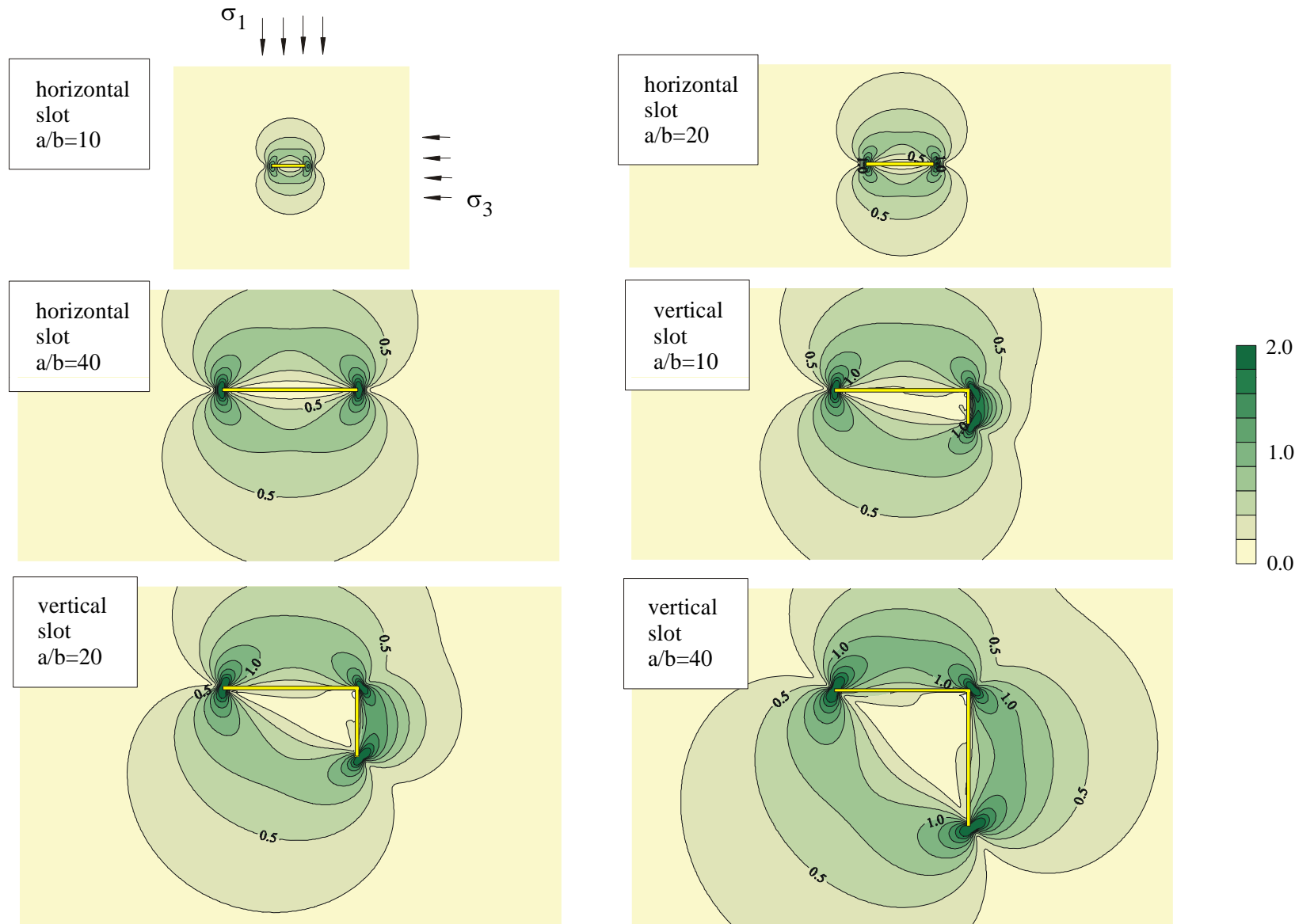


Discing of a 1.3 m diameter core from highly stressed rock (Courtesy of URL/AECL, Canada)

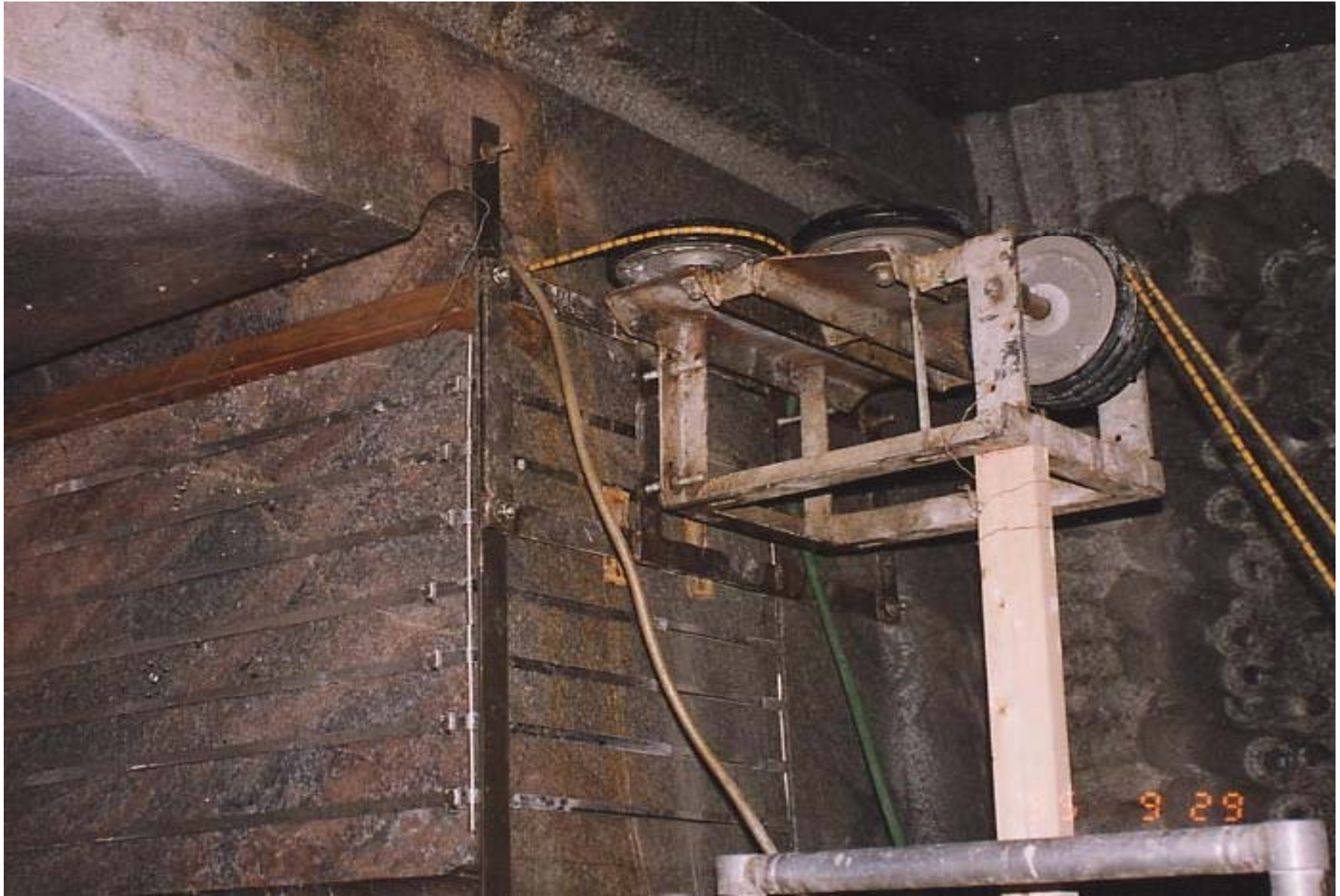


Asymmetric breakout produced by shear stresses acting parallel to excavation (R.S., Read, 1995)

Contours of Maximum Shear Stress $\frac{\sigma_1 - \sigma_3}{\sigma_0}$ developed during slotting of a rock block



Note: Results are for $\sigma_1 = \sigma_3 = \sigma_0$

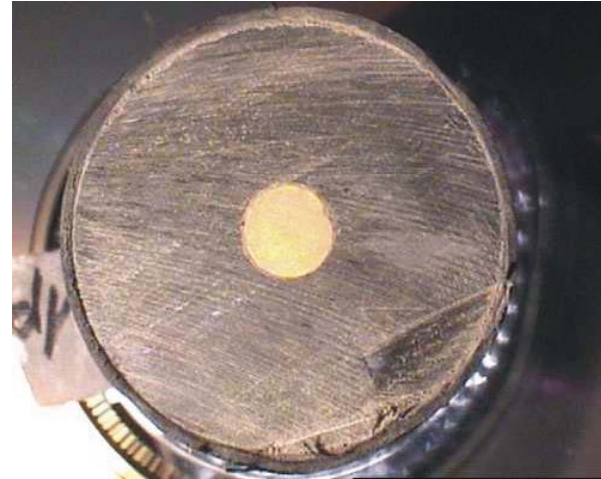
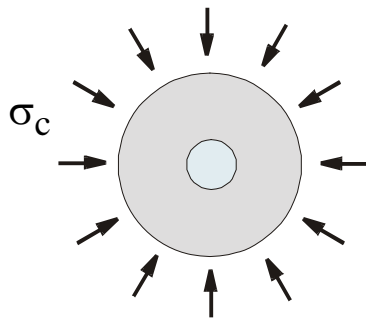


Wire saw slotting tool (Courtesy of URL/AECL, Canada)

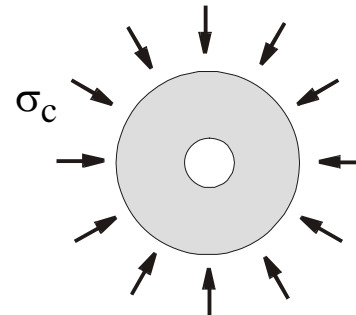
Tunnel Near-field. Disintegration of EDZ



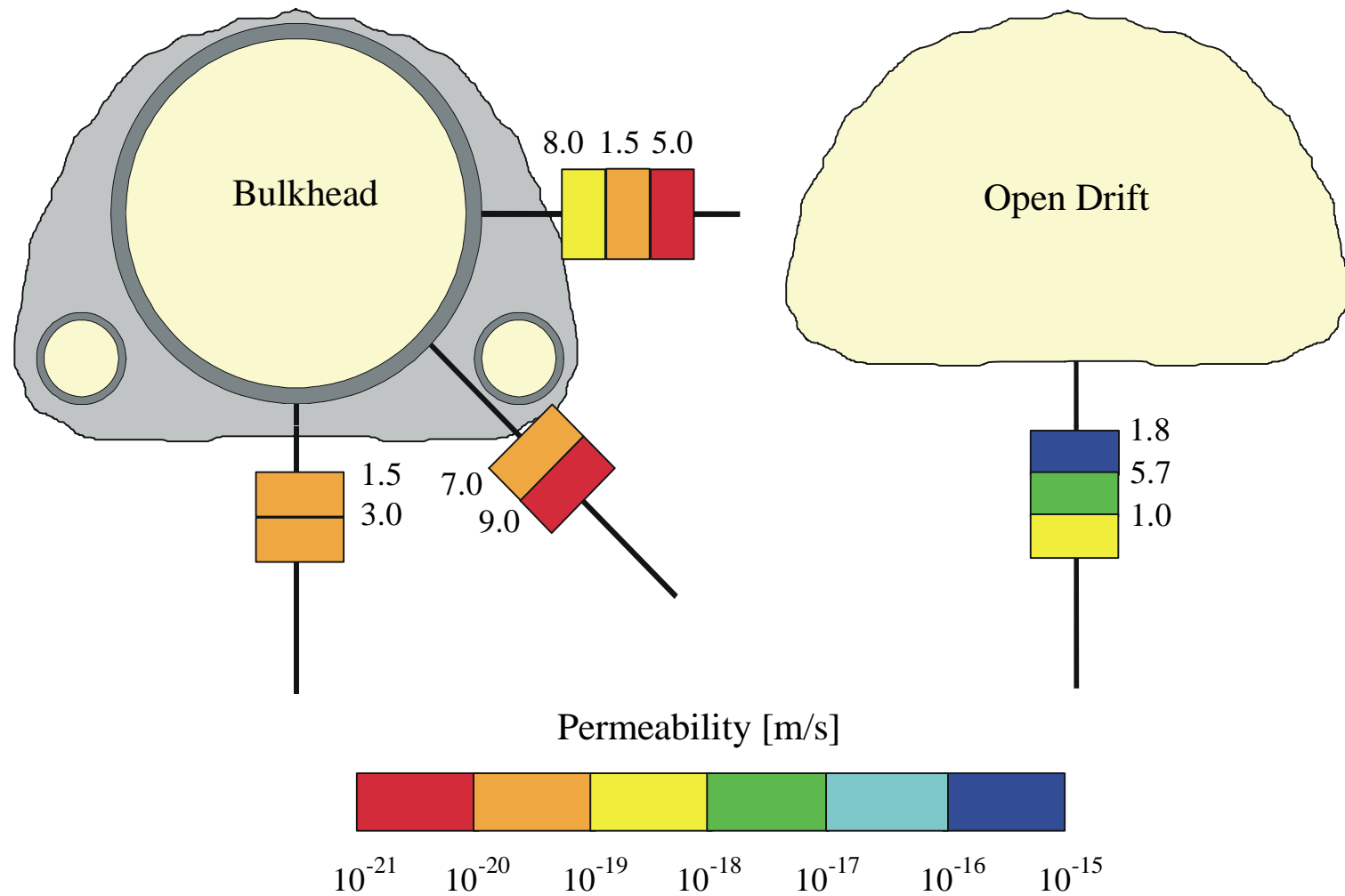
$\sigma_c = 13 \text{ MPa}$
water circulated in inner borehole



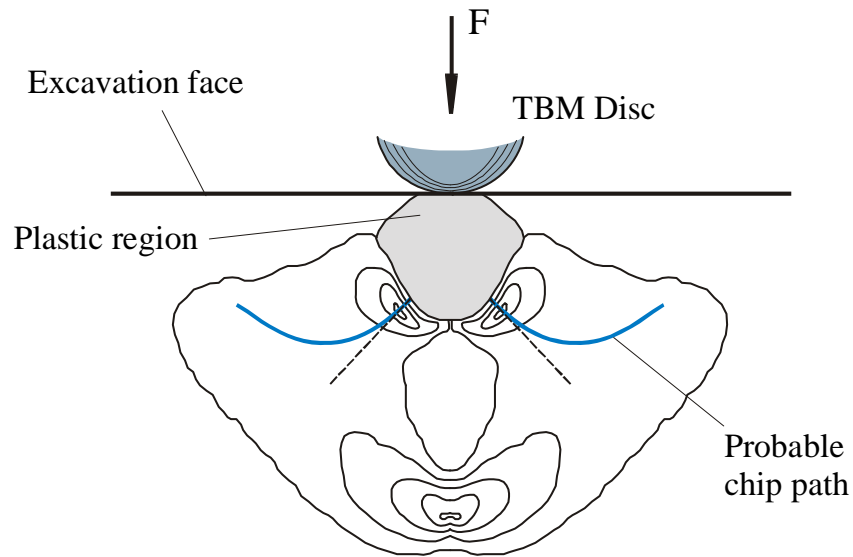
$\sigma_c = 30 \text{ MPa}$
dry inner borehole



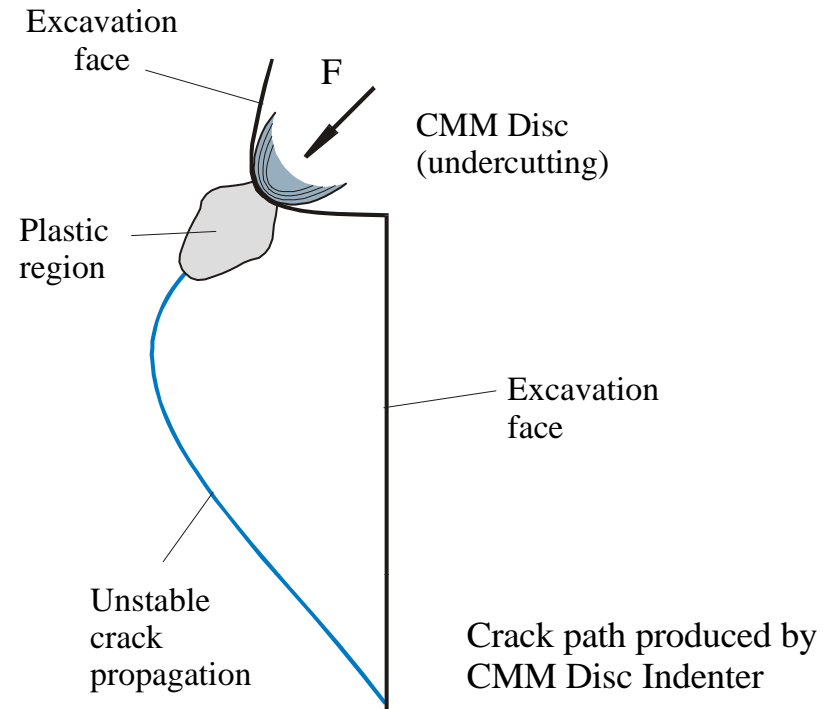
Effect of water on the EDZ in the Opalinus Clay, Mont Terri, Switzerland (Courtesy of **nagra** )



ALOHA2: Permeability Distribution Around the Bulkhead Drift (Courtesy of **GRS**)



Stress distribution beneath a TBM Disc Indenter after the stable vertical crack has developed

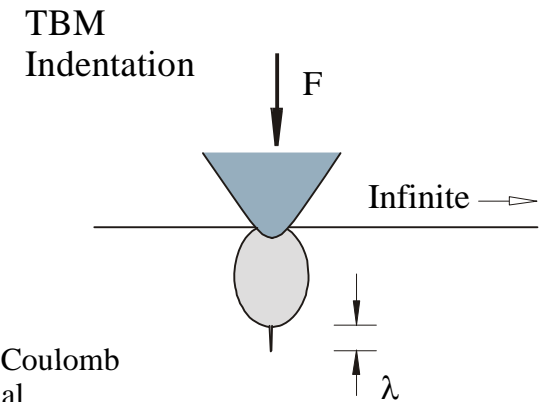
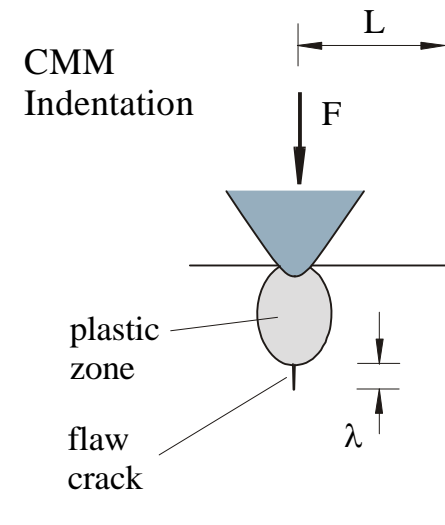
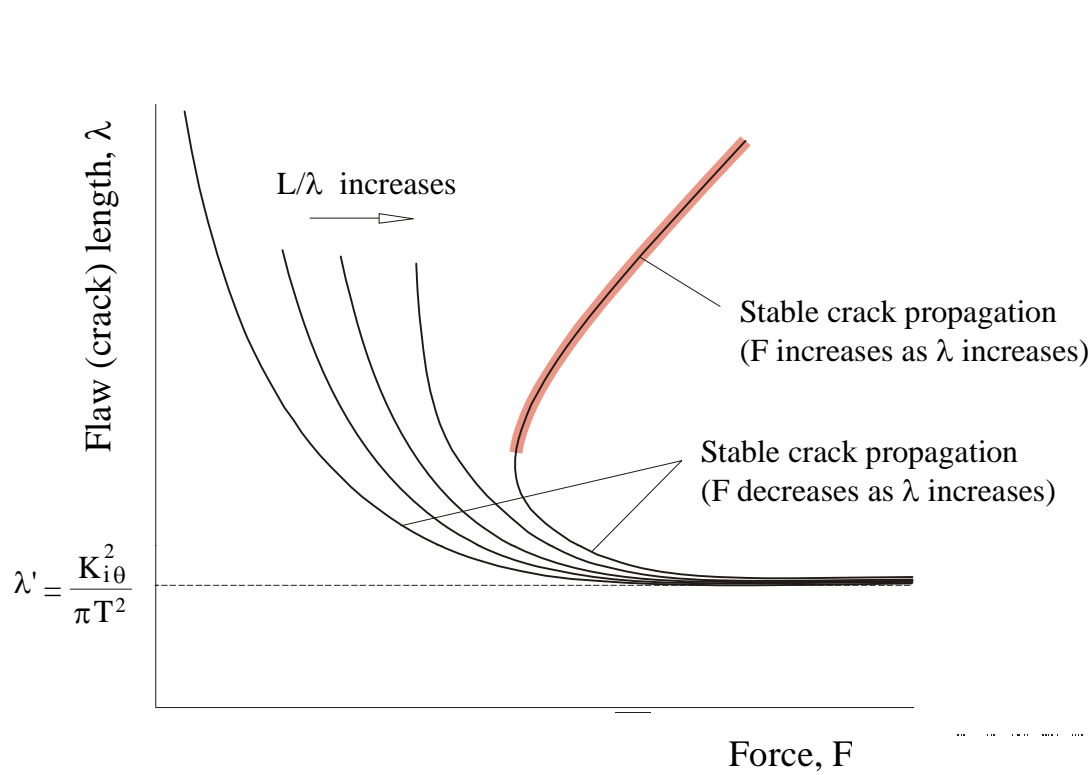


Note: Tensile crack can not propagate until plastic region reaches critical size

Disc tip radius	CMM Indenter Force (N/mm of contact length)			
	S = 25 mm	S = 50 mm	S = 100 mm	S = ∞
6 mm	1,700 (74%)	2,310 (100%)	2,700 (117%)	3,000 (130%)
8 mm		2,500 (100%)	3,150 (126%)	(3,500?) (140%?)
12 mm		3,150 (100%)	3,600 (114%)	4,200 (133%)

Note: Indenter Force Increase is small for large increase in cutting depth S.

Comparison of chip formation in classical TBM and in CMM (undercutting)



$K_{i\theta}$ = fracture toughness

λ' = pre-existing crack length in rock

T = tensile strength of rock (q/K_p)

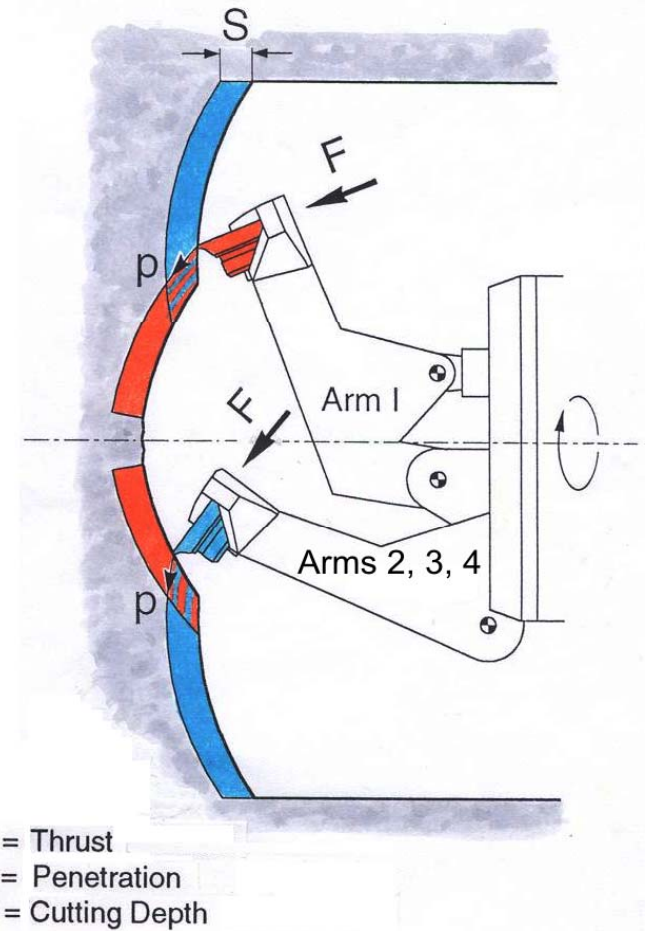
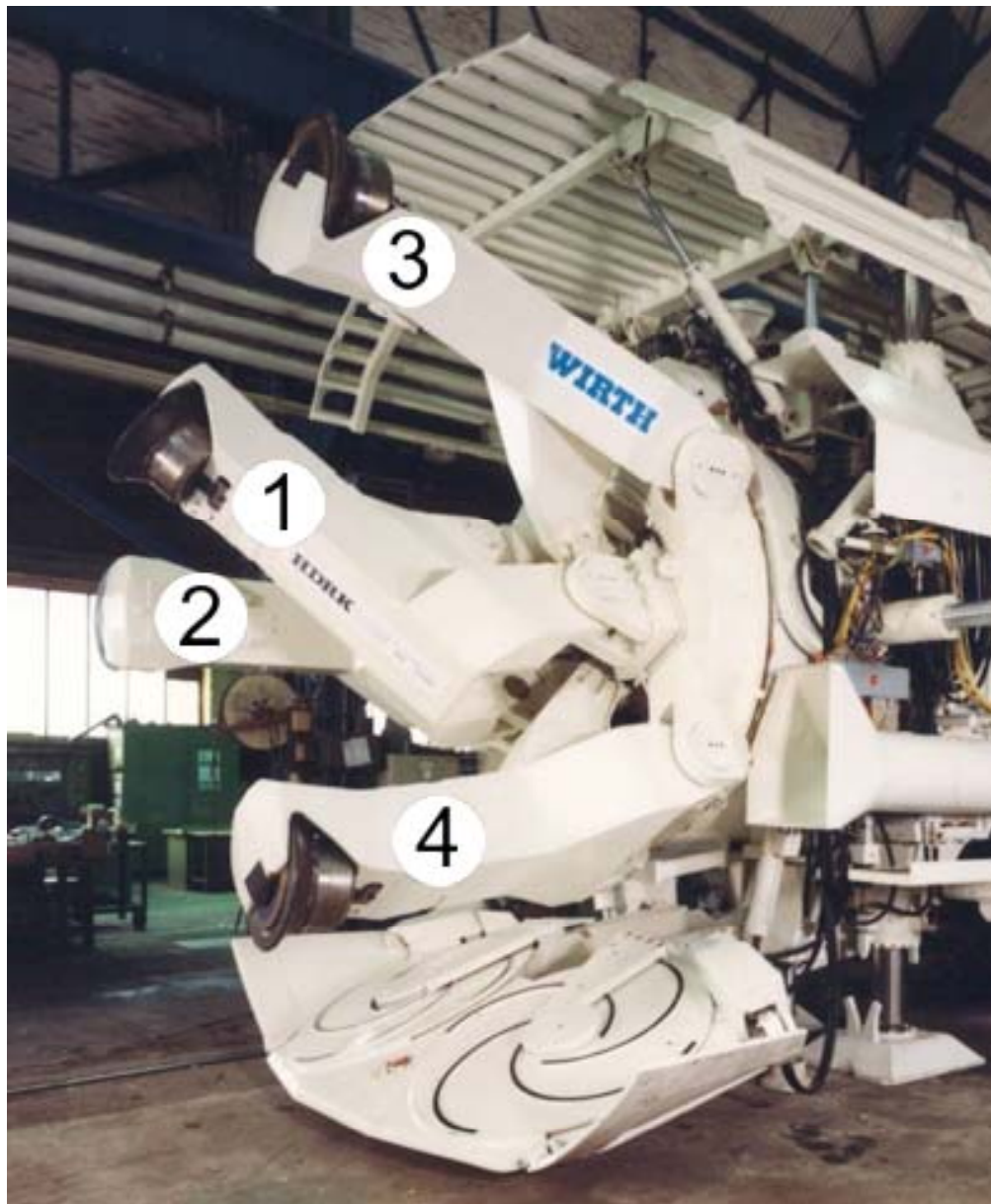
q = unconfined compressive strength

$K_p = (1 + \sin \phi) / (1 - \sin \phi)$

ϕ = friction angle

Mohr-Coulomb material

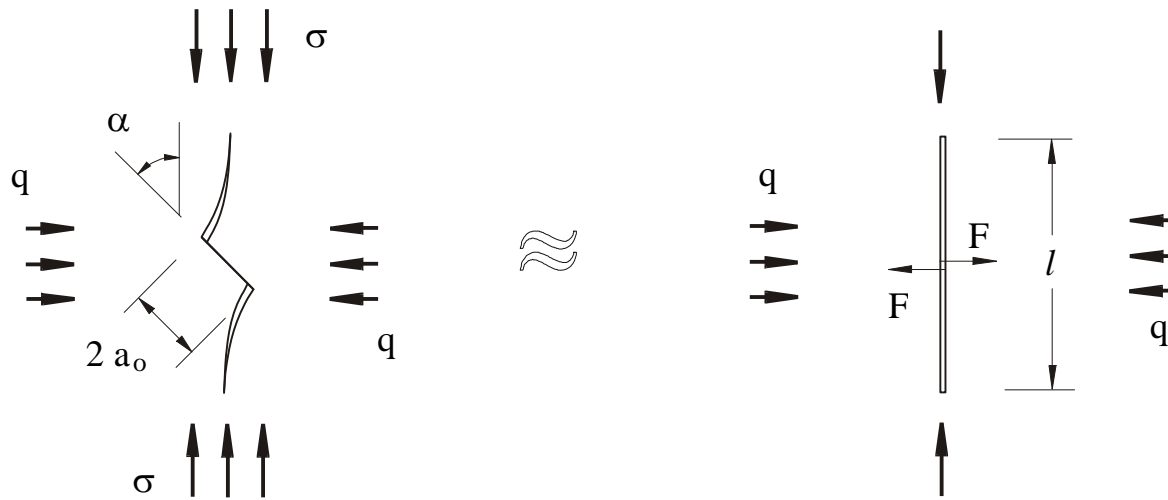
Relationship between applied force on an indenter and the length of edge crack (λ) beneath the plastic crushed zone



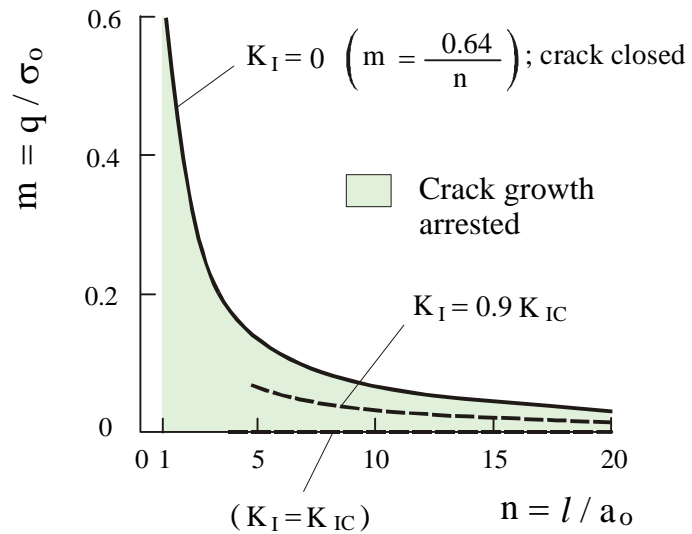
WIRTH-HDRK Continuous Mining Machine (CMM)



Rock cuttings produced by CMM



Wing crack growth under compression, Fairhurst and Cook (1966) model



$$K_I = F / \sqrt{\pi l} - q \sqrt{\pi l} ; \quad F = 2 \sigma a_o \quad (1)$$

Crack growth if $K_I > K_{IC}$ [$\sigma > \sigma_c$]

(after Germanovich and Dyskin, 2000)

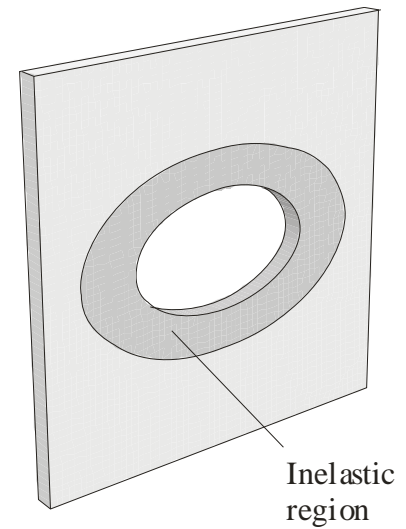
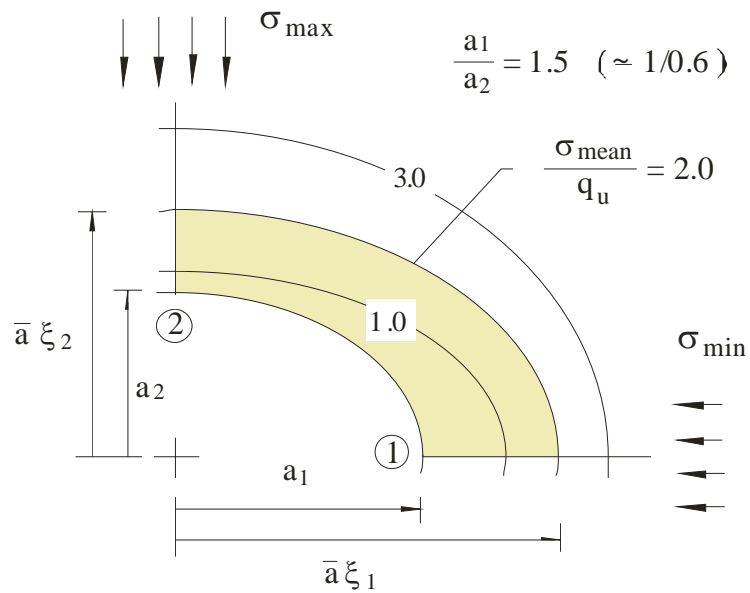
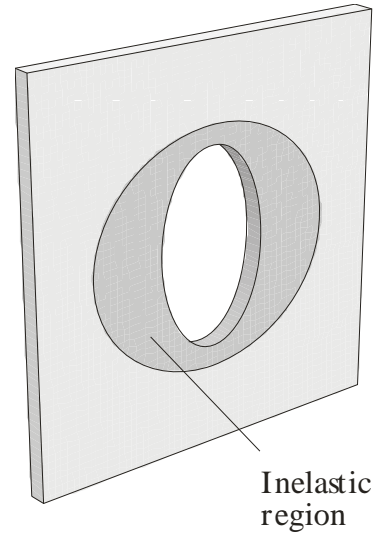
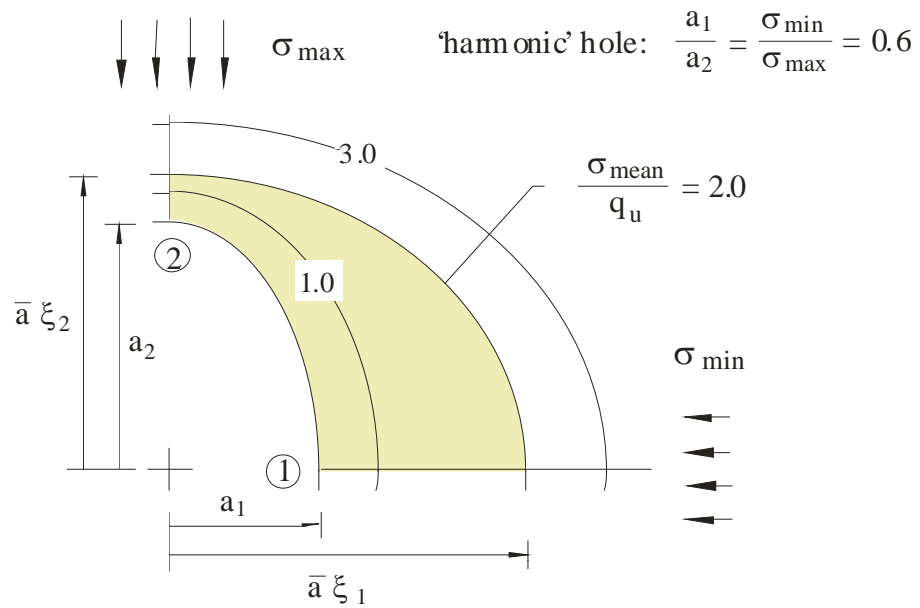
Rewriting (1)

$$K_I = \sigma_o \sqrt{a_o} \left[\frac{2}{\sqrt{n\pi}} - m \sqrt{n\pi} \right]$$

where $n = l / a_o$ $m = q / \sigma_o$

$$K_I = 0 \quad \text{if} \quad m \geq \frac{2}{n\pi} \simeq \frac{0.64}{n}$$

Suppression of crack growth by small confining pressure



“Harmonic Hole” — Optimum shape of hole to minimize the extent of excavation damage?

$$\frac{a_1}{a_2} = \frac{\sigma_{\min}}{\sigma_{\max}} = 0.6$$

$$\begin{aligned} a_1 &= 1.2 \text{ m} & \sigma_{\min} &= 1.19 \text{ MPa} \\ a_2 &= 2.0 \text{ m} & \sigma_{\max} &= 0.71 \text{ MPa} \end{aligned}$$

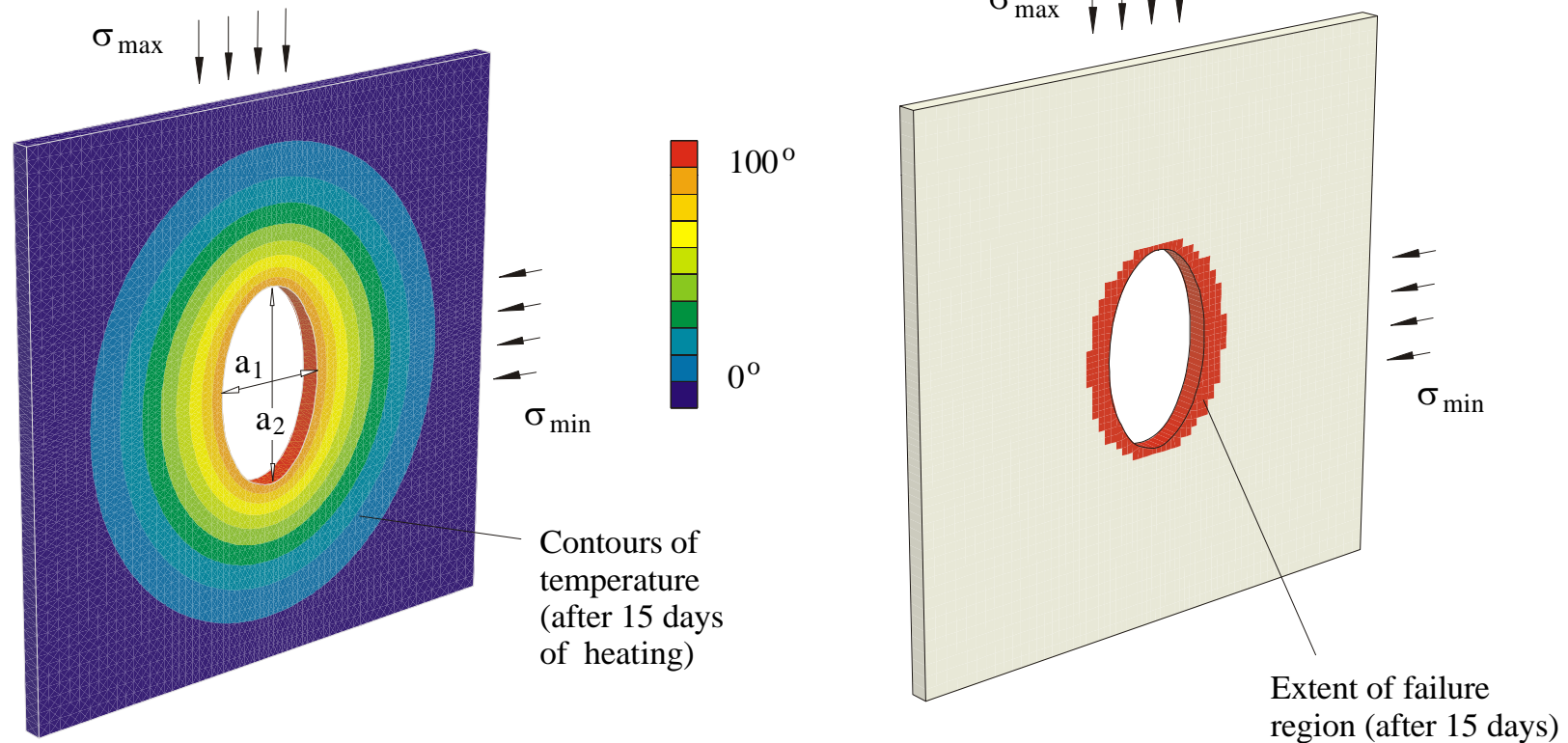
Thermal properties

$$\begin{aligned} \kappa &= 3 \text{ W/m}^\circ\text{C} \\ c_p &= 844.83 \text{ J/kg}^\circ\text{C} \\ \alpha_t &= 40 \times 10^{-6} \text{ 1/}^\circ\text{C} \end{aligned}$$

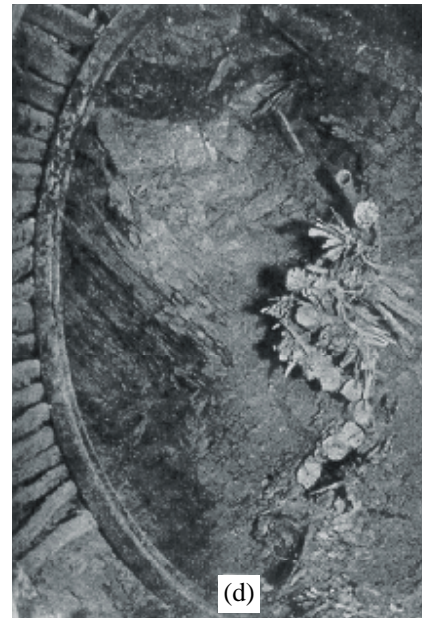
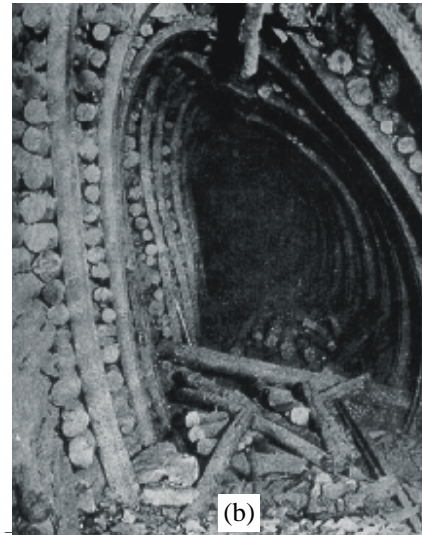
Mechanical properties

$$\begin{aligned} \phi &= 30^\circ \\ q_u &= 1 \text{ MPa} \\ \rho &= 2650 \text{ kg/m}^3 \end{aligned}$$

Wall temperature $T=100^\circ\text{C}$
(fixed)

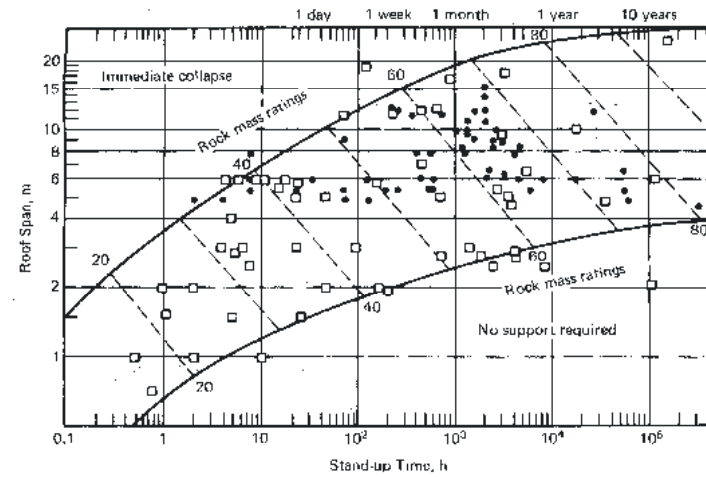


“Harmonic Hole” —Effect of thermal load on excavation damage

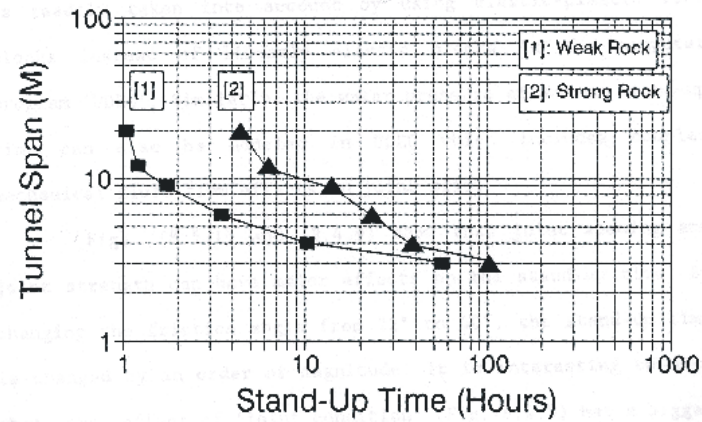


“Harmonic hole” - Kolar Gold Fied (Caw, 1956)

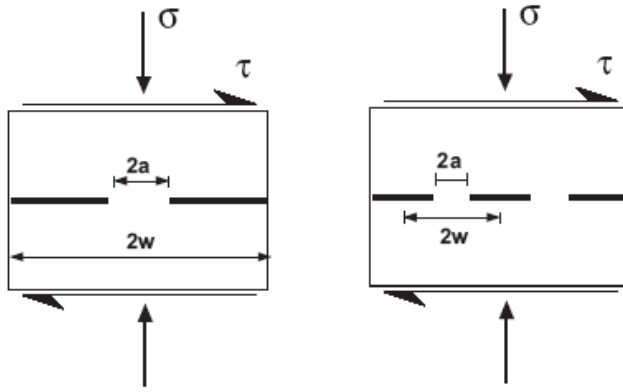
a)



b)



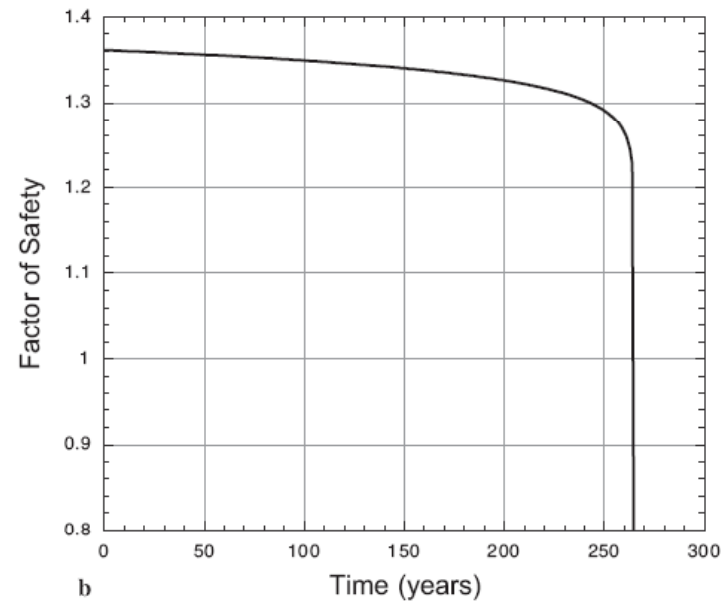
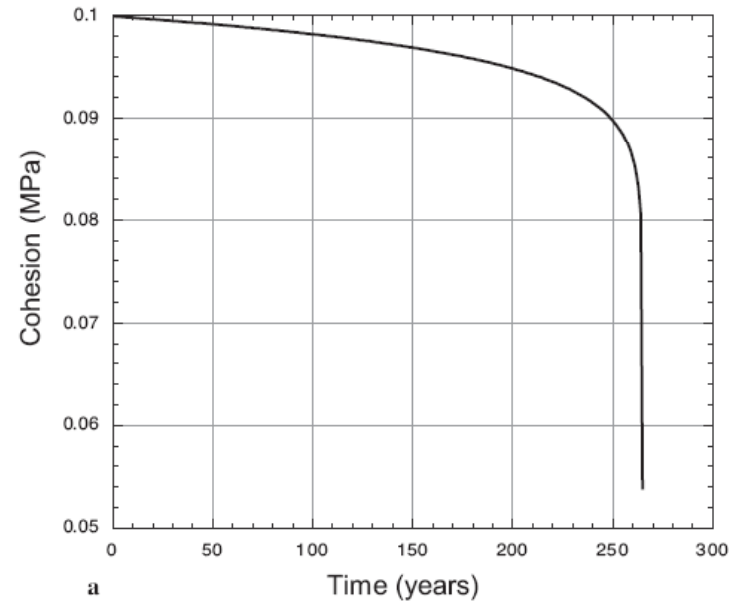
(a) Empirical stand-up time relations for tunnels as a function of span and rock quality defined by the Rock Mass Rating System; (b) Theoretical stand-up time based on joint strength deterioration with time (after Fakhimi 1992).



Fracture mechanics models, a) single rock bridge under far field normal and shear stresses; b) multiple rock bridge under far field normal and shear stresses.

$$C_0 = \frac{\sqrt{\pi} \left[a_0^{1+n/2} - \left(1 + \frac{n}{2} \right) A t \left[\frac{2w(\tau - \sigma_n \tan \phi)}{K_{IIC} \sqrt{\pi}} \right]^n \right]^{1/(2+n)}}{2w}$$

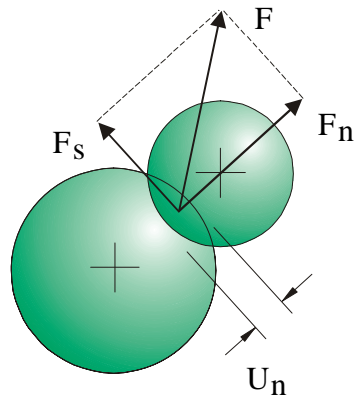
$$FS = \frac{C_0 + \frac{W}{A_s} \cos \theta \tan \phi}{\frac{W}{A_s} \sin \theta}.$$



From Kemeny, 2003

Cohesion and safety factor as a function of time.

Linear contact law



Contact law

$$F_n = K_n \cdot U_n$$

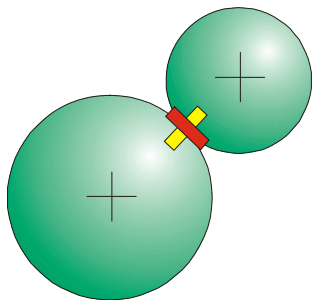
$$\Delta F_s = K_s \cdot \Delta U_s$$

Slip condition

$$F_s = \mu F_n$$

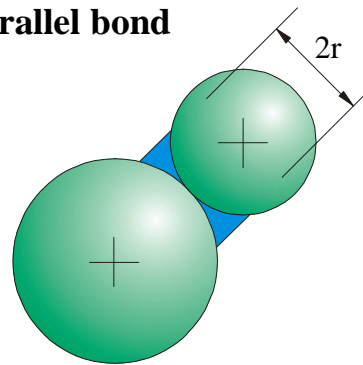
Deformation is assumed to occur at contact point only.

Contact bond



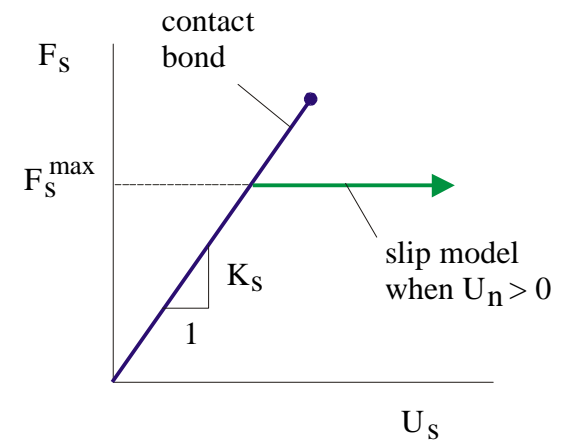
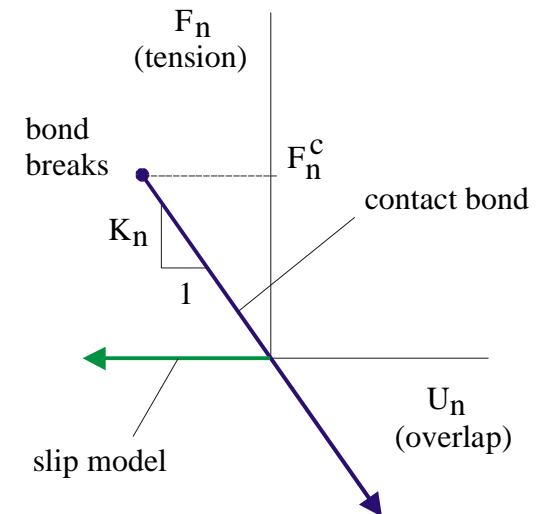
Models adhesion over vanishingly small area of contact point (does not resist bending moment); breaks if normal or shear force exceeds bond strength.

Parallel bond



Models additional material deposited after particles are in contact (resists bending moment); breaks if normal or shear stress exceeds bond strength.

Constitutive behavior at contact between two particles



Parallel-bonded stress corrosion model

- Stress-dependent corrosion reaction occurs at micro-tension sites.

Corrosion reaction occurs at the periphery of parallel bonds and removes bond material

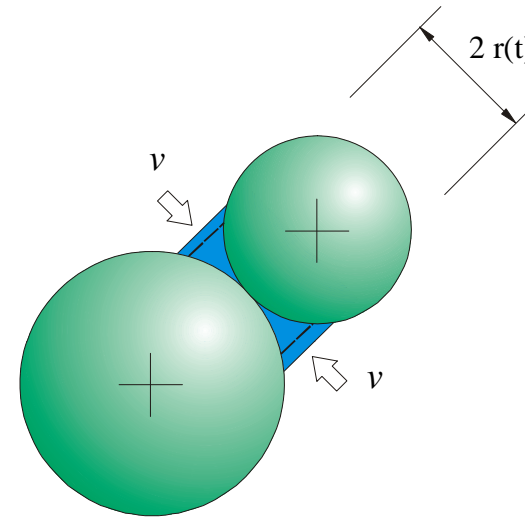
- Reaction rate is determined by local driving force and local energy barrier.

- 1) Driving force: bond stress (σ)
- 2) Energy barrier: micro-activation stress (σ_a)

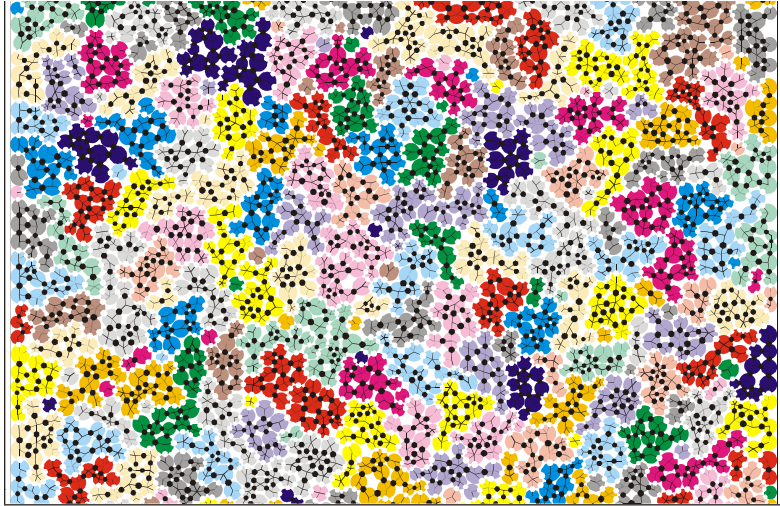
- Express corrosive-front velocity as:

$$v = \beta_1 e^{\beta_2 (\bar{\sigma} / \bar{\sigma}_c)}$$

$$v = 0 \quad \text{if } \sigma < \sigma_a$$

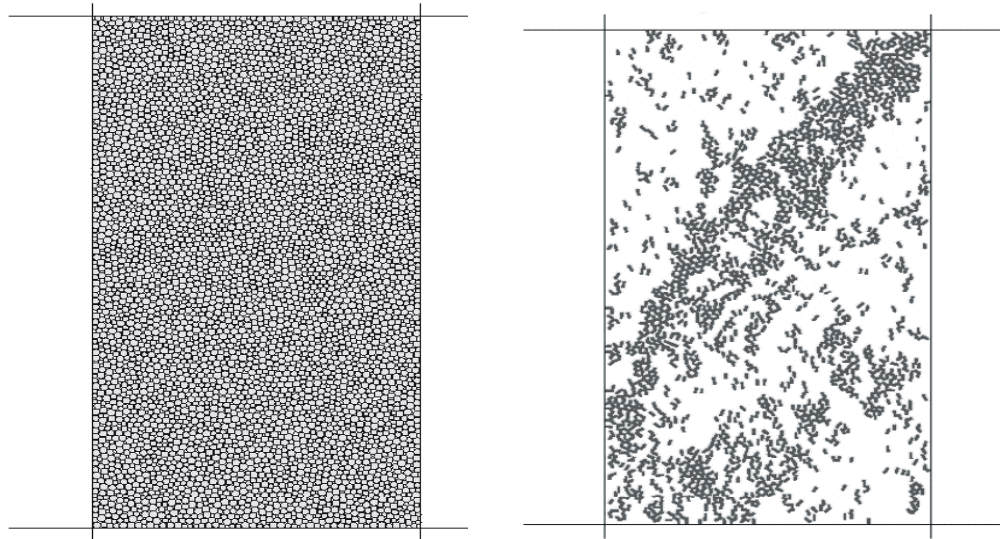


PFC simulation of time dependent weakening of rock

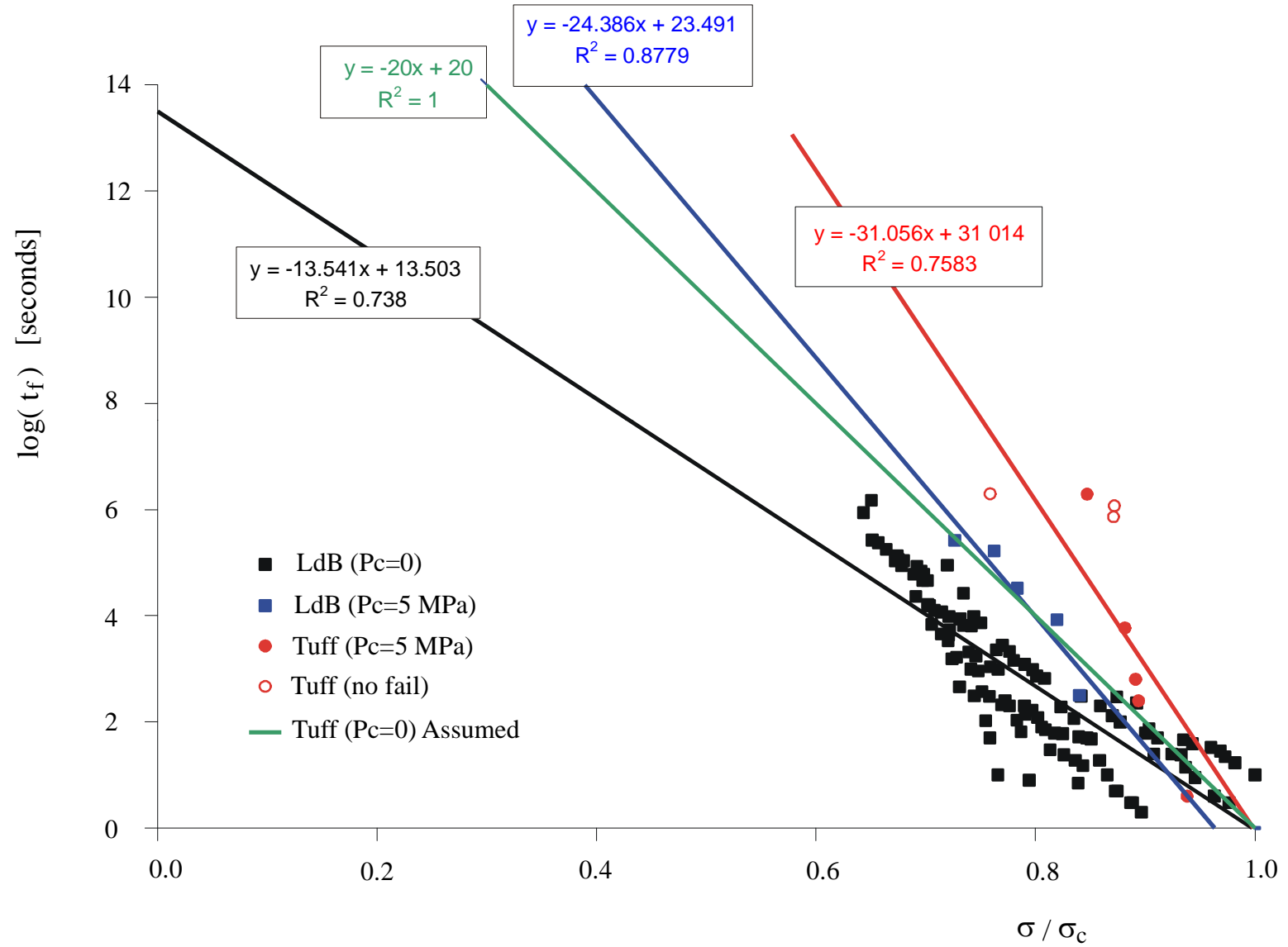


Cluster of particles

Compression test
on assembly of
particles

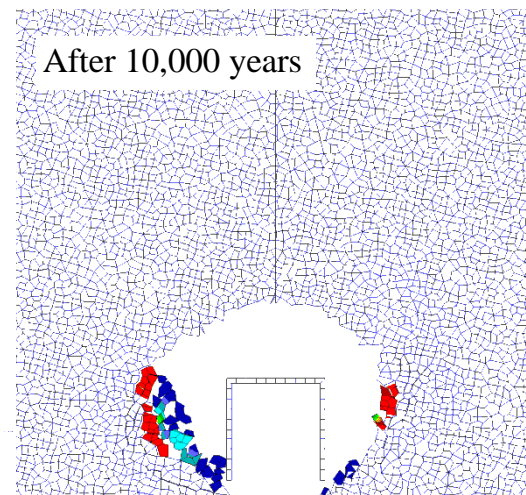
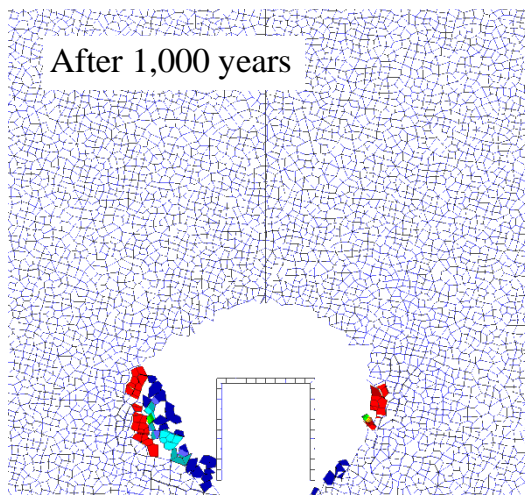
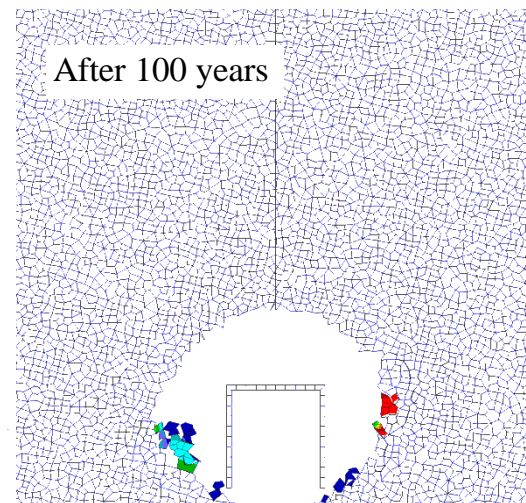
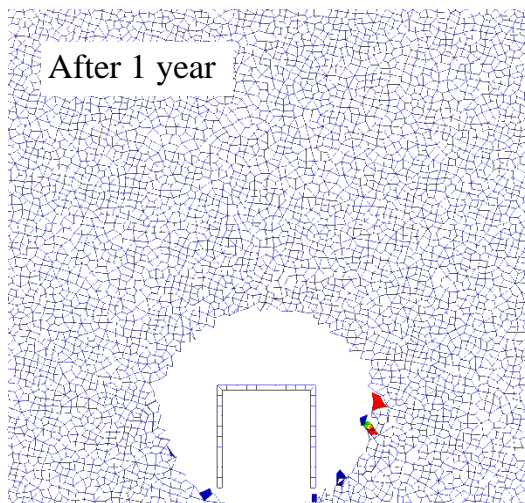
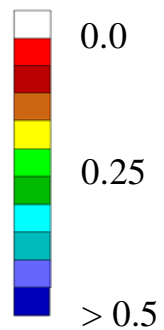


PFC model of a particulate assembly (rock) and compression loading



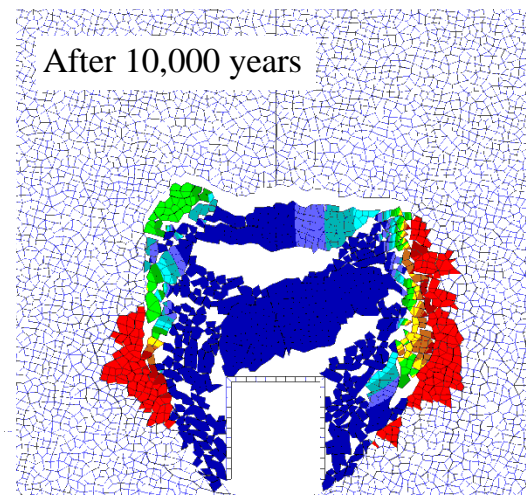
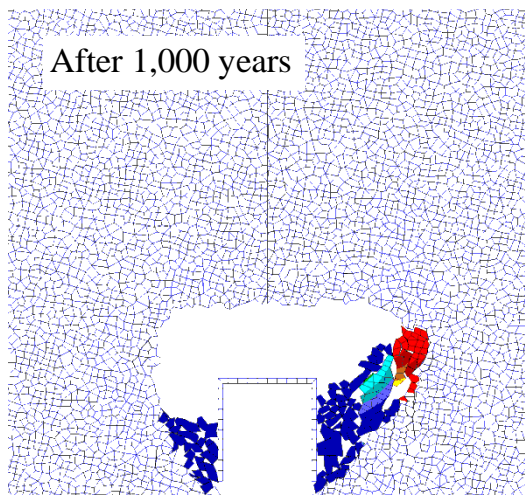
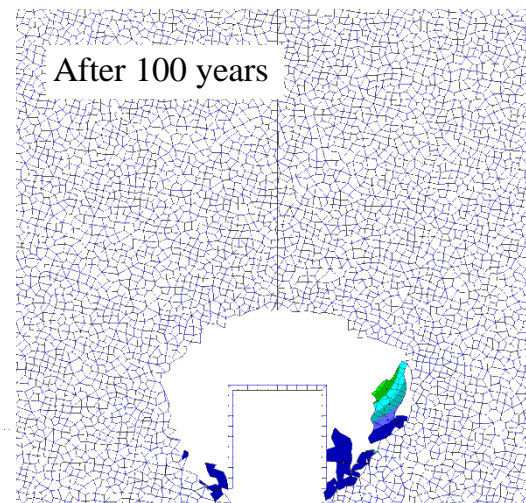
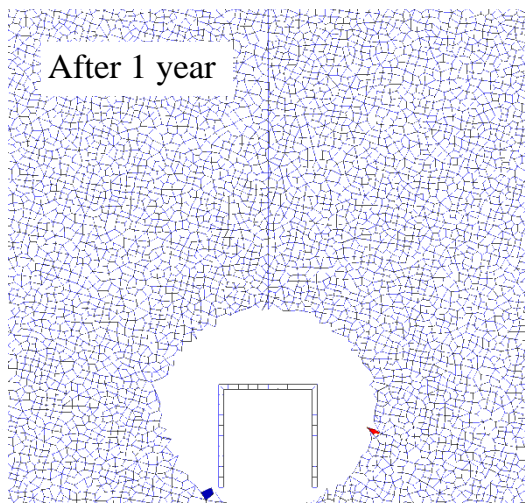
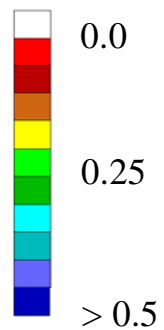
Static Fatigue Curves used as input to the UDEC analysis of collapse over time at Yucca Mountain

Magnitude
of displacements
[meters]

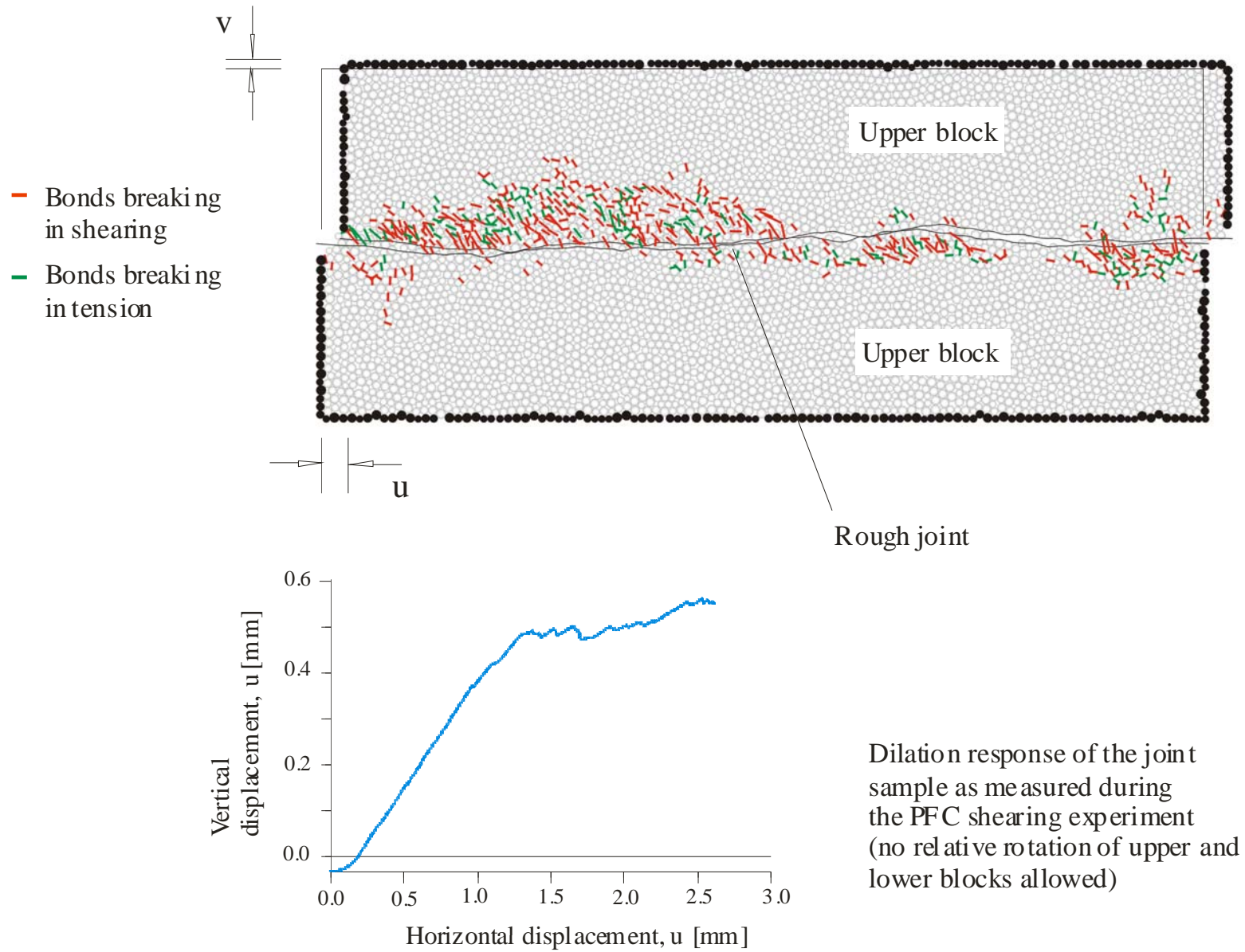


Collapse predicted around drifts over 10,000 years at Yucca Mountain assuming Category 2 Tuff Static Fatigue Curve.
Note: thermal and seismic effects have not been considered.

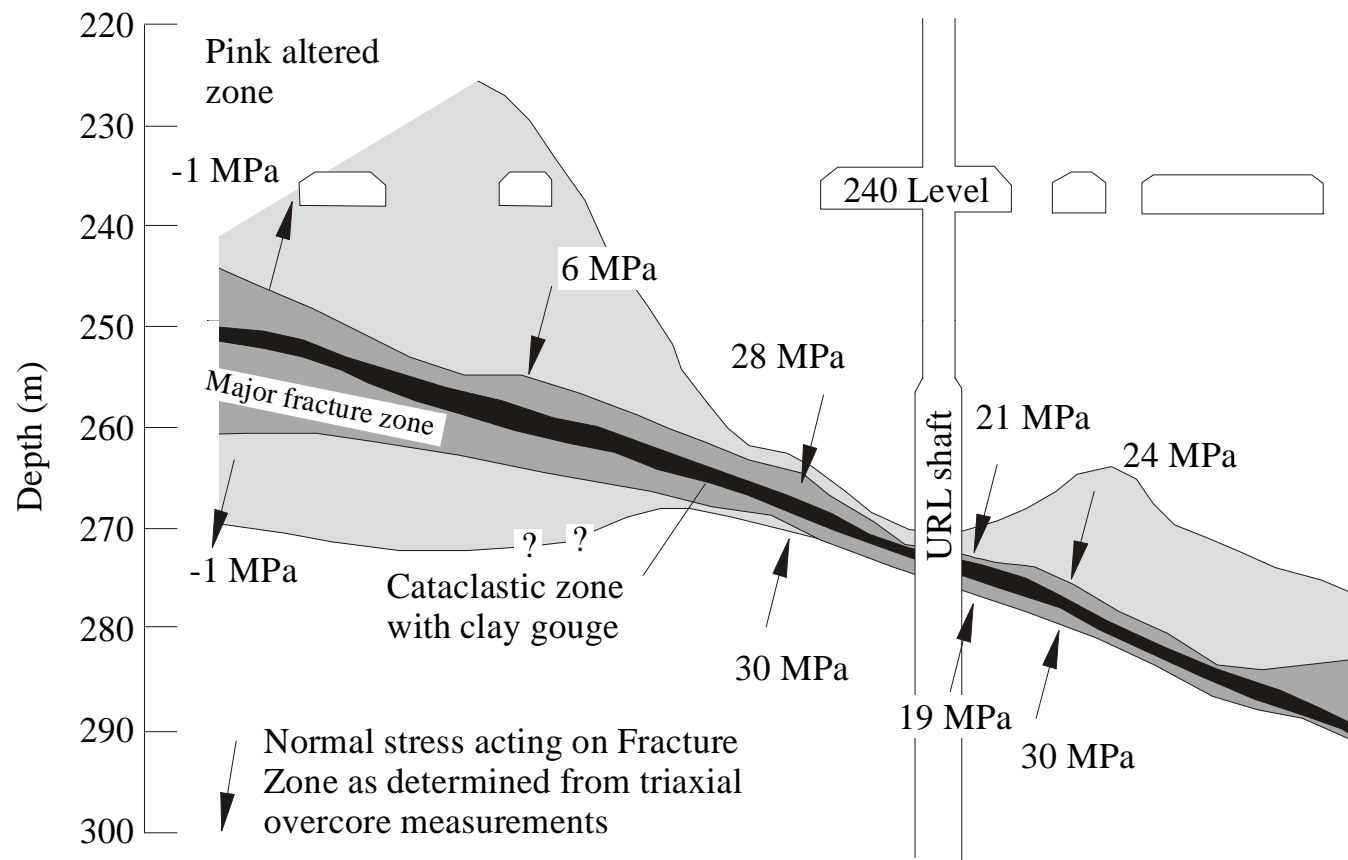
Magnitude
of displacements
[meters]



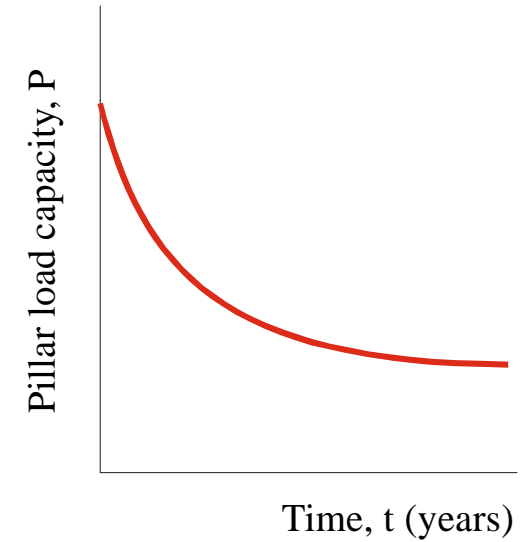
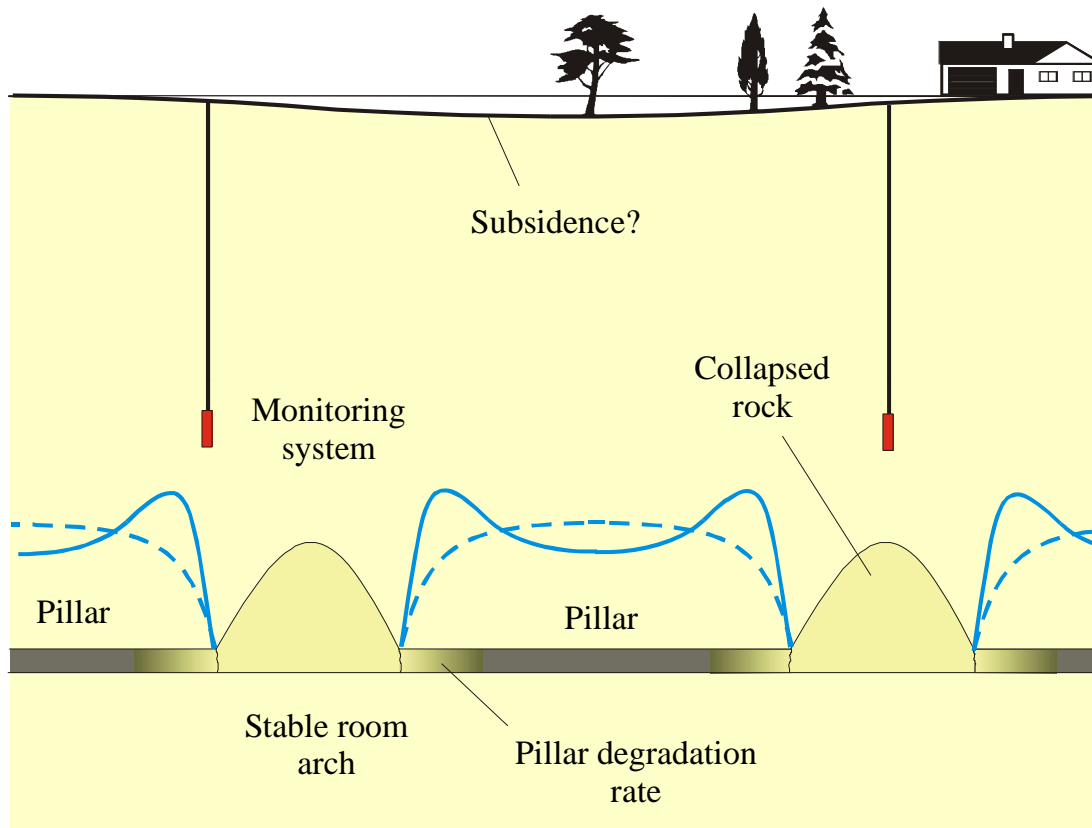
Collapse predicted around drifts over 10,000 years at Yucca Mountain assuming Category 2 Lac du Bonnet Static Fatigue Curve. Note: thermal and seismic effects have not been considered.



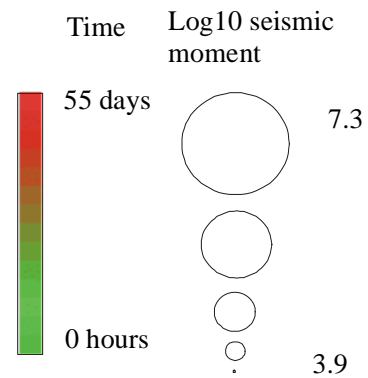
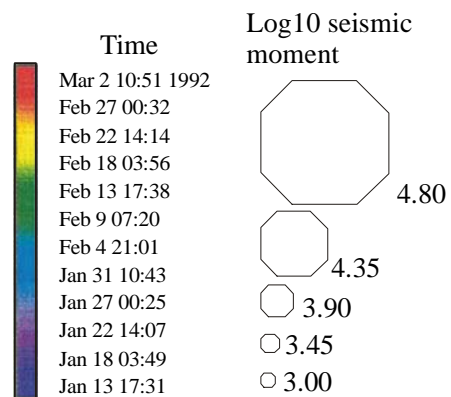
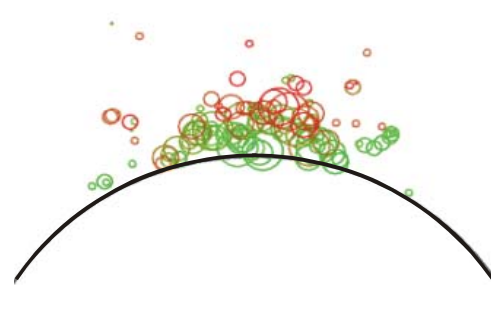
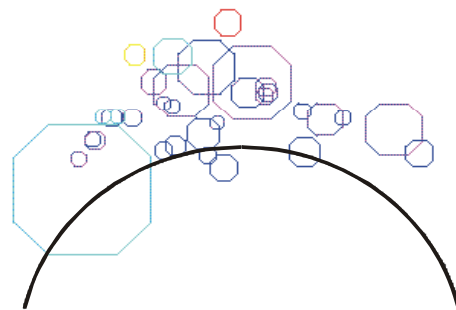
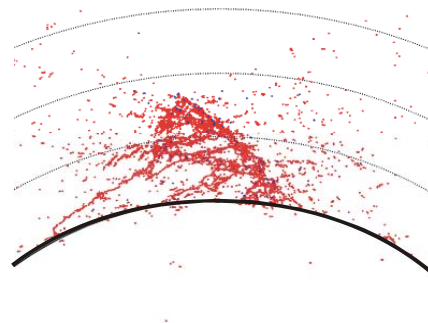
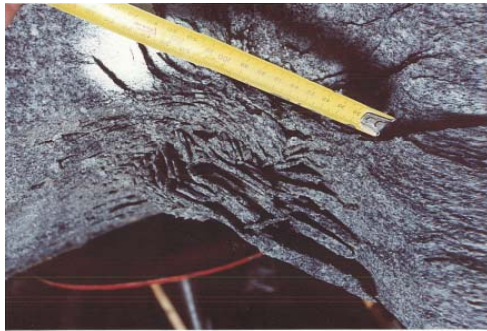
Use of PFC to examine the shear behavior of a rough joint.



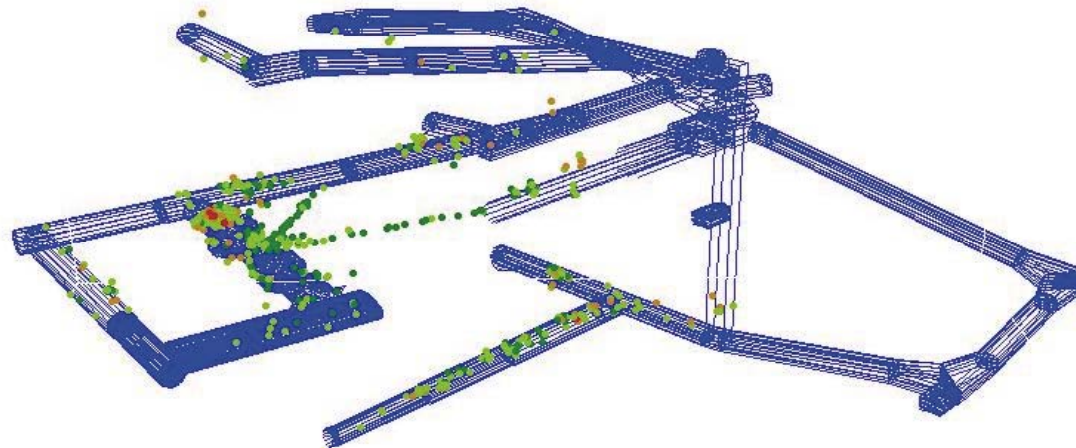
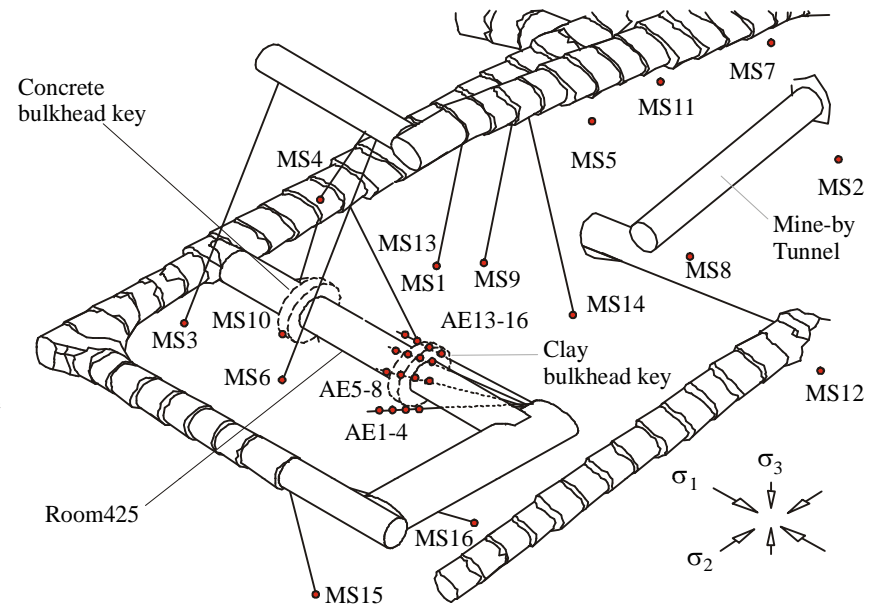
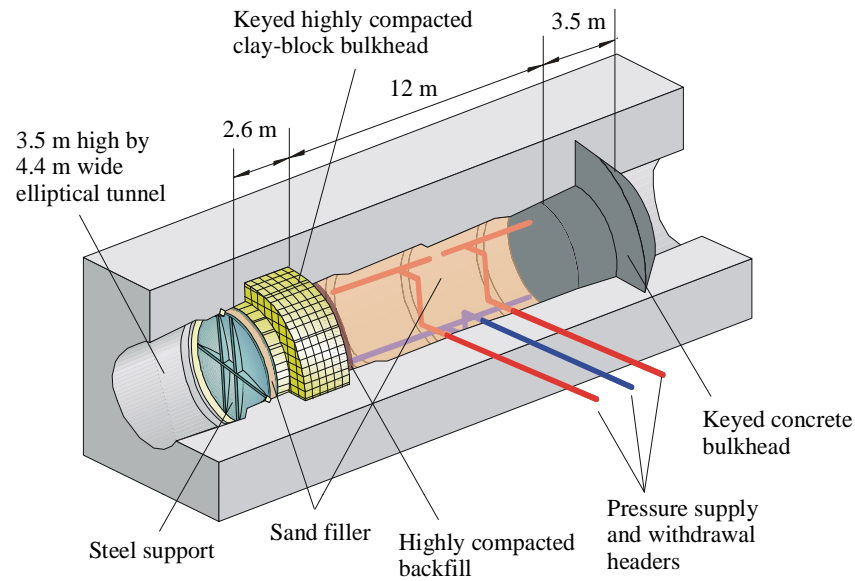
Observed variability of normal stress across a thrust fault at the URL, Pinawa, Canada.



Prediction of long-term (50~100 yr) behaviour of Pillars and Large Excavations in abandoned mines



Breakout PFC analysis



Transparent Earth. URL TSX AE (Courtesy of Professor Paul Young, University of Toronto)

Conclusions

- Remarkable and continuing computational and observational advances.
- Predictive models should build from empirical rules; rationalize and extend them.
- Advances will benefit all of rock mechanics.
- Waste isolation offers unprecedented opportunity to “know” the rock mass —Professor Müller’s prime concern.

Slides left out

