



FIFTH INTERNATIONAL  
ITASCA SYMPOSIUM  
**20**  
VIENNA, AUSTRIA

**FIFTH INTERNATIONAL ITASCA SYMPOSIUM  
ON APPLIED NUMERICAL MODELING IN  
GEOMECHANICS — 2020**

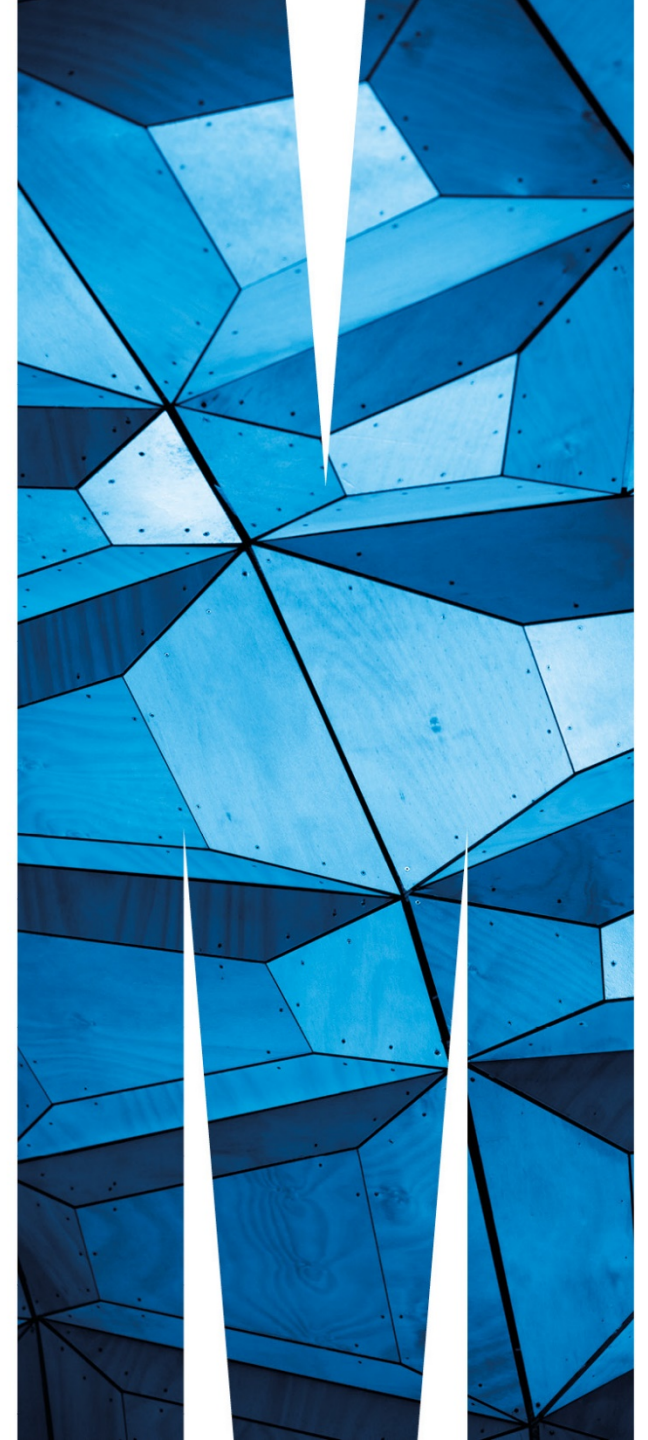
# **FLAC3D-PFC3D Coupled Simulation of Triaxial Hopkinson Bar**

**Wanrui Hu & Dr. Qianbing Zhang**  
*Monash University, Australia*

**Dr. David O. Potyondy**  
*Itasca Consulting Group Inc., USA*



**MONASH**  
University



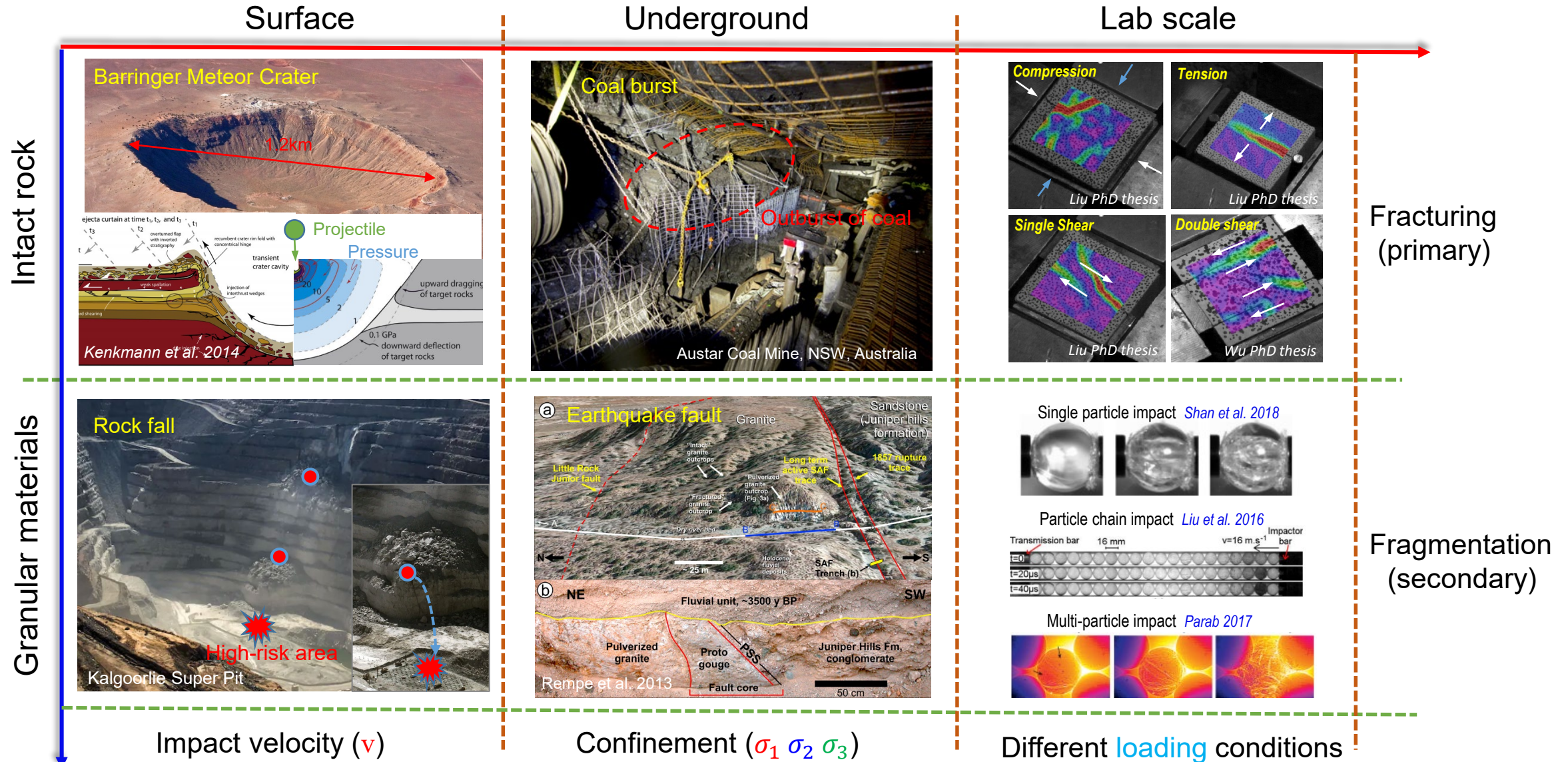
**Wanrui Hu** is a PhD candidate in the Department of Civil Engineering, Monash University in Australia. He received both his Master and Bachelor degrees from Wuhan University in China. His research topic is dynamic fracturing and fragmentation of brittle materials. He is currently focusing on dynamic compression and shear behavior of rock under multiaxial loading using a coupled continuum-discrete modelling method.

# OUTLINE

- Introduction
  - Dynamic loading resources
  - Experimental and numerical methods
- 3D Triaxial Hopkinson Bar
- Numerical Modelling
- Summary and Future Study

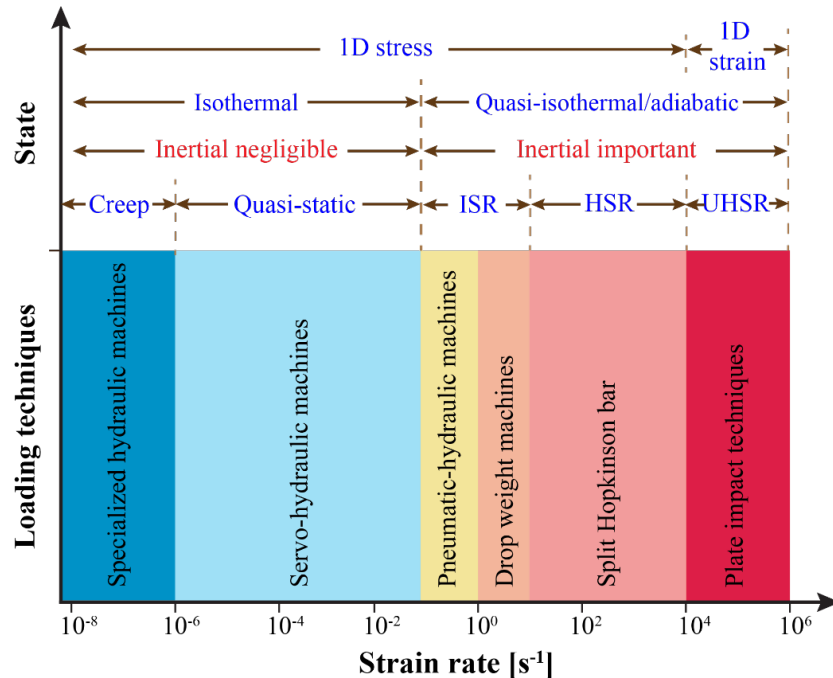
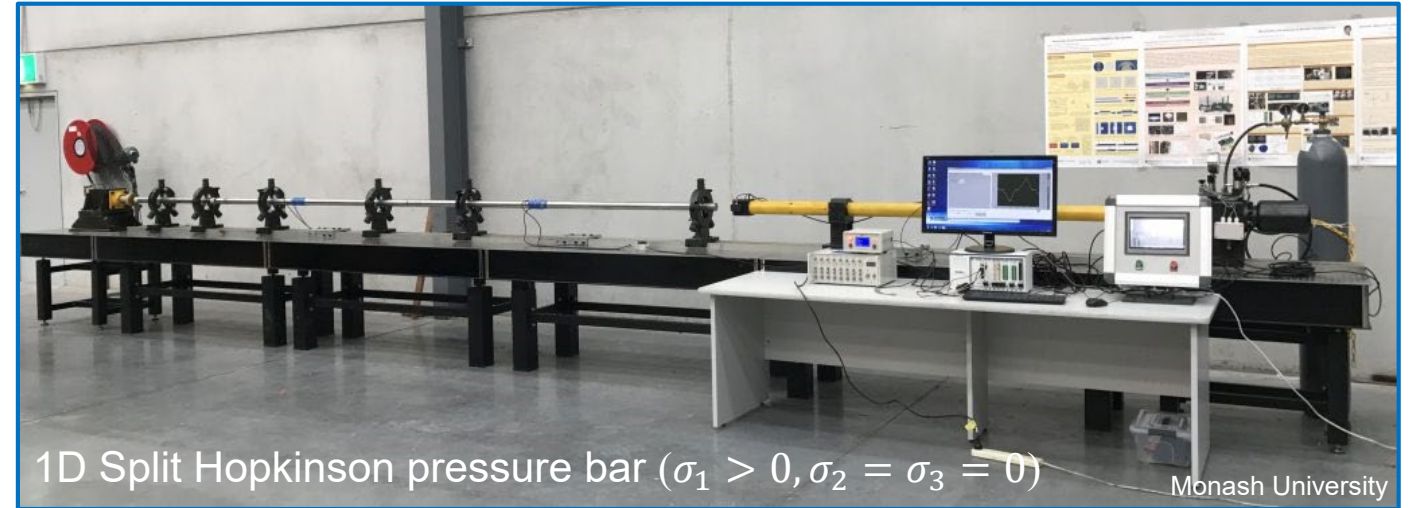


# Natural and Human-induced Hazards: Confinement and Impact



# Dynamic Experimental Techniques

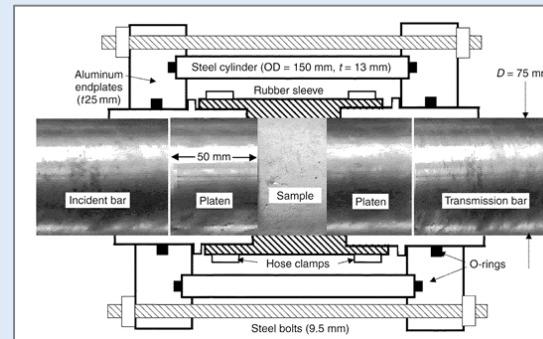
- Pneumatic-hydraulic Machines
- Drop Weight Machines
- **Split Hopkinson Bar**
- Plate Impact Techniques



Zhang et al. 2019, *AREPS*



Conventional confining boundary  
( $\sigma_1 > \sigma_2 = \sigma_3$ )



Nemat-Nasser et al. 2000

Multiaxial loading boundary  
( $\sigma_1 > \sigma_2 > \sigma_3$ )



Monash University



# Numerical Modelling Methods

## □ Continuum-based methods

- RFPA, AUTODYN, LS-DYNA
- Incorporation of rate-dependent constitutive models
- Phenomenological representation of failure

## □ Discontinuum-based methods

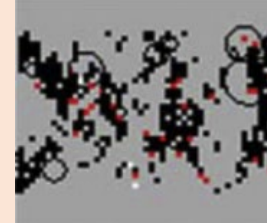
- UDEC, PFC, ESyS-Particle
- Explicitly modelling of fractures formed by microcracks
- Limited scale
- Insufficient strain rate effects

## □ Hybrid Methods

- FDEM, FDM/DEM
- Computational efficiency
- Fracture and fragmentation
- Stress wave propagation

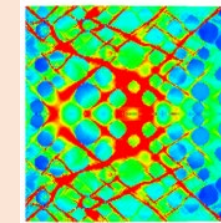
### Continuum-based methods

*RFPA*



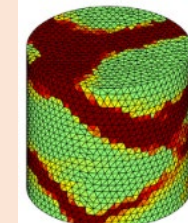
Zhu et al. 2012

*AUTODYN*



Hao et al. 2013

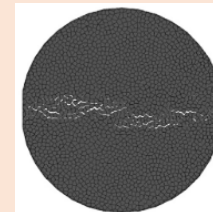
*LS-DYNA*



Saksala et al. 2017

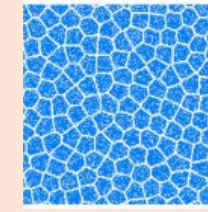
### Discontinuum-based methods

*UDEC*



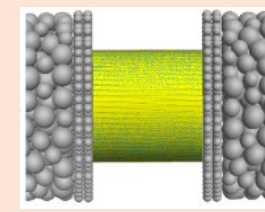
Gui et al. 2016

*PFC*



Li et al. 2018

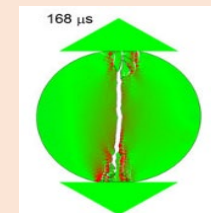
*ESyS-Particle*



Du et al. 2018

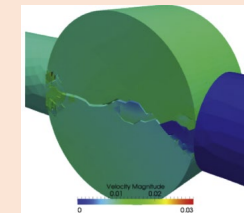
### Hybrid Methods

*2D FDEM*



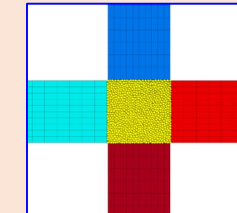
Mahabadi et al. 2010

*3D FDEM*



Rougier et al. 2014

*FDM/DEM*



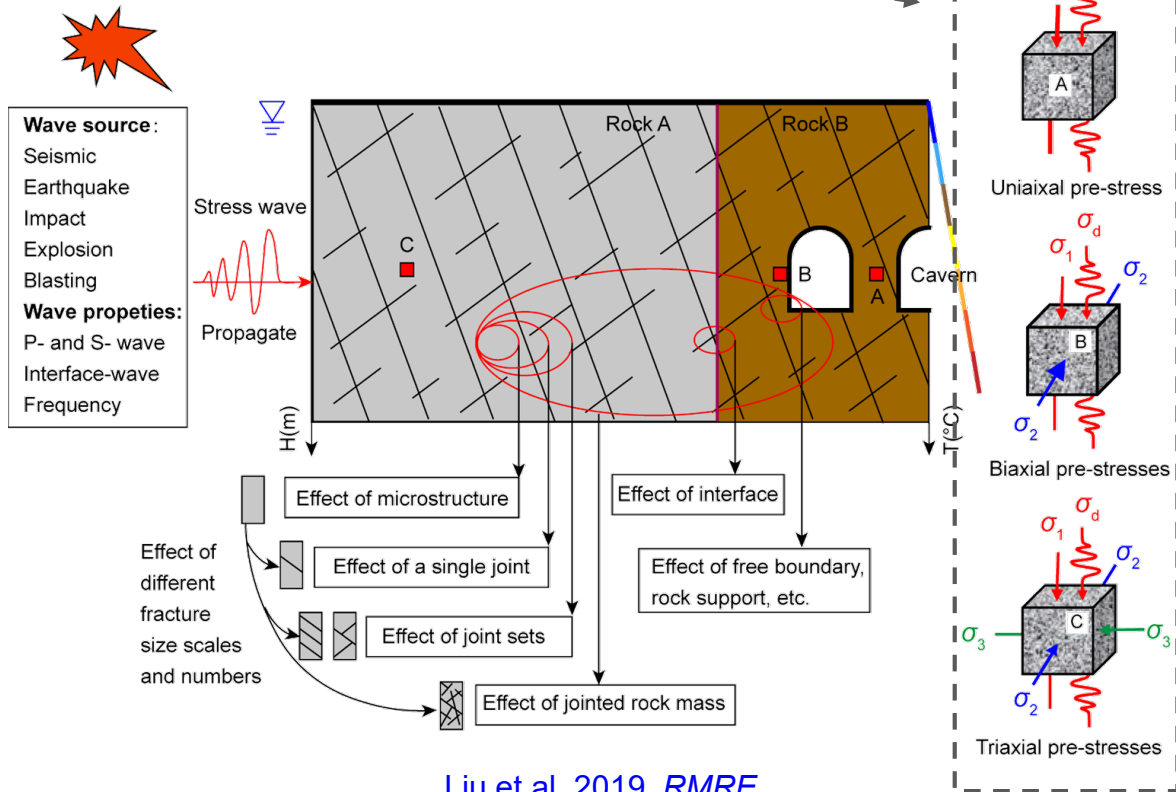
This study

# OUTLINE

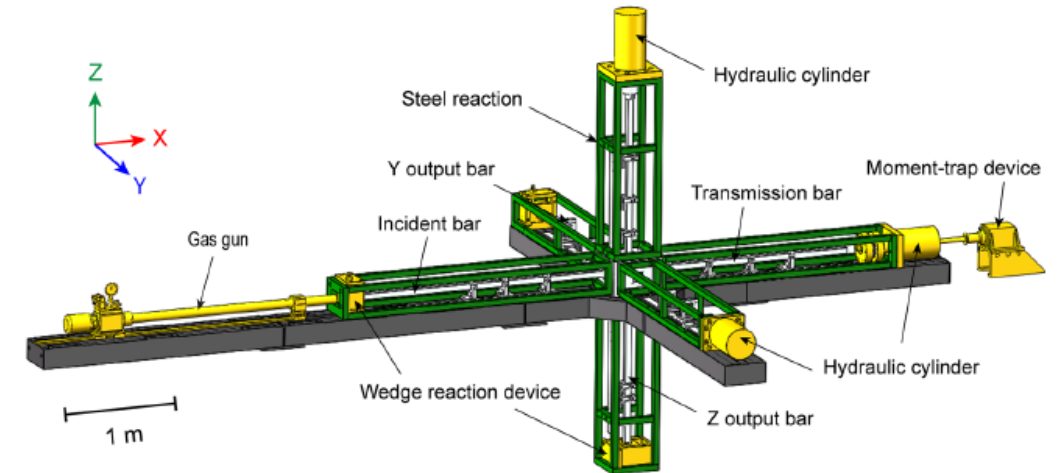
- Introduction
- 3D Triaxial Hopkinson Bar
  - Components and Capabilities
  - High-Speed Imaging and Micro-CT Scan
- Numerical Modelling
- Summary and Future Study

# Dynamic Behaviours under Multiaxial Loading

Rock dynamic problems in underground engineering: multiaxial loading



- Impact velocity up to 50 m/s
- Specimen size from 50 mm
- Triaxial quasi-static loads up to 100 MPa

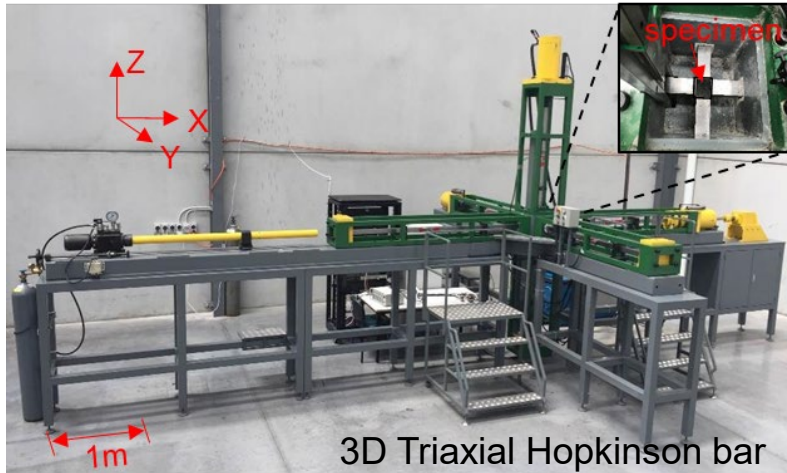


Schematic of 3D Triaxial Hopkinson bar

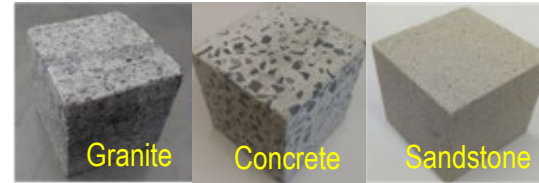




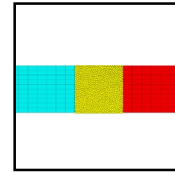
# Dynamic Behaviours under Multiaxial Loading



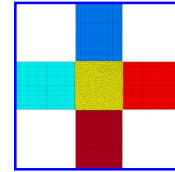
Polycrystals Composites Porous media



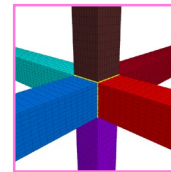
Uniaxial (UC)



Biaxial (BC)



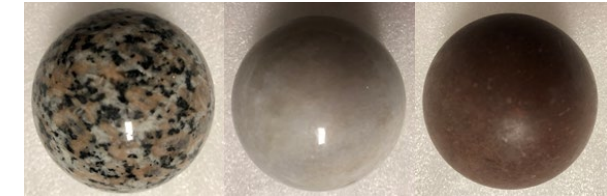
Triaxial (TC)



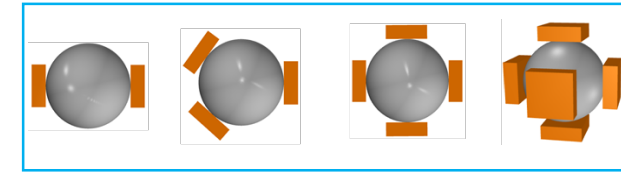
Granite

Marble

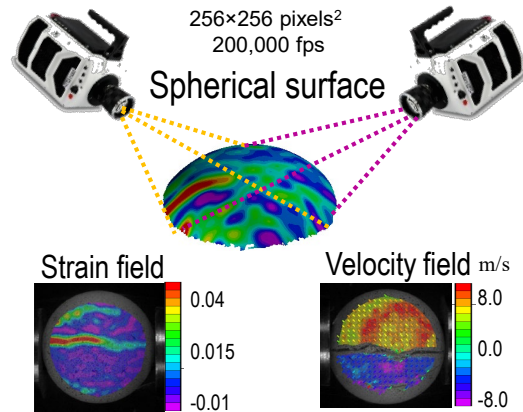
Sandstone



Multiple contacts



Surface (3D DIC)



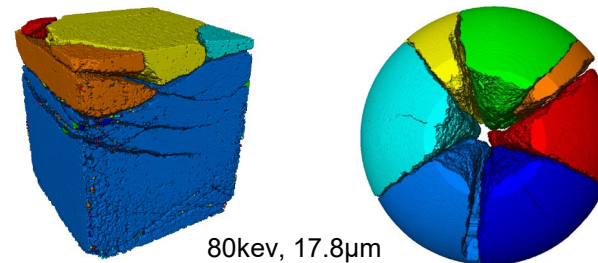
- kinetic energy of the flying fragments

$$E_k = \frac{1}{2}mv^2 + \frac{1}{2}I\omega^2$$

Internal (X-ray CT)

Cube

Sphere

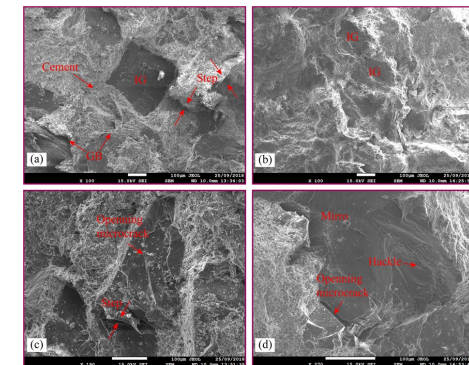


- Fracture surface energy

$$E_s = W_{In.} - W_{Re.} - W_{Tr.} - E_k$$

$$G = E_s/A$$

Micro scale (SEM)

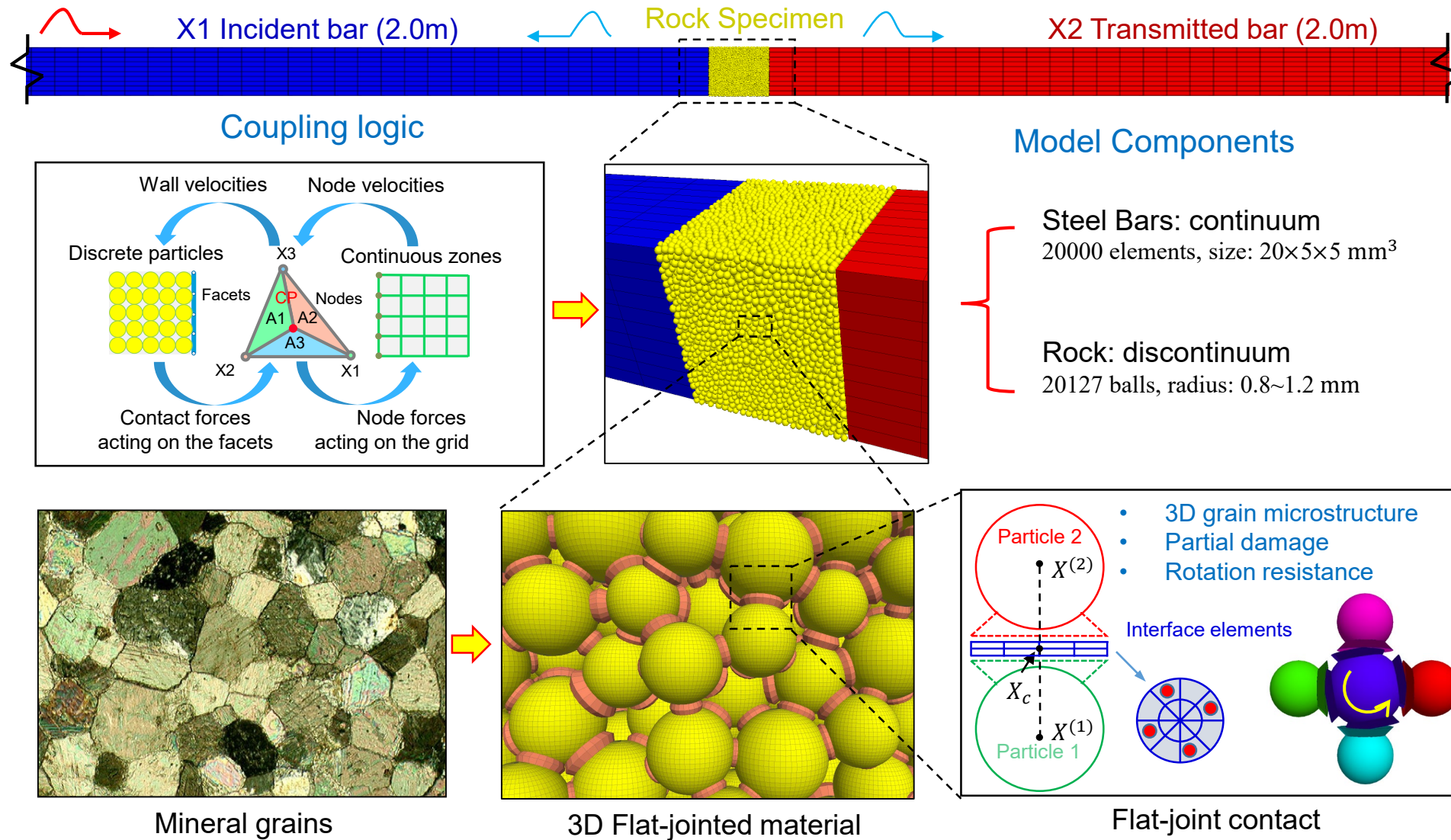


- Microstructure
- Failure mechanism

# OUTLINE

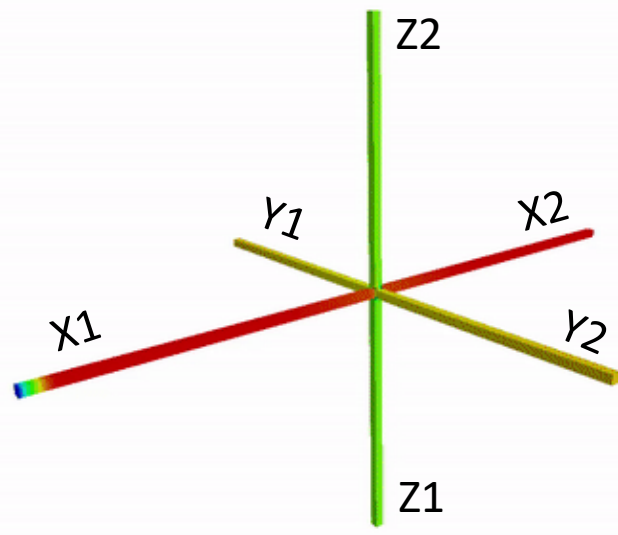
- Introduction
- 3D Triaxial Hopkinson Bar
- Numerical Modelling
  - A coupled continuum-discrete method
  - Flat-jointed model
  - Verification and comparison
- Summary and Future Study

# A Coupled Continuum-discrete Model for 3D SHPB

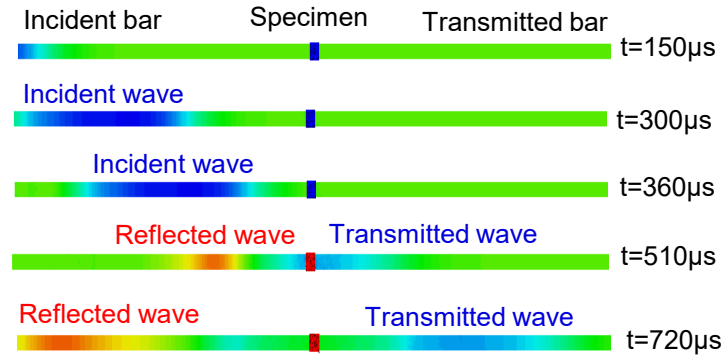




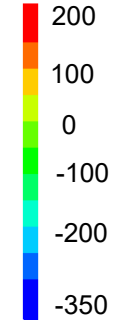
# Verification and Comparison



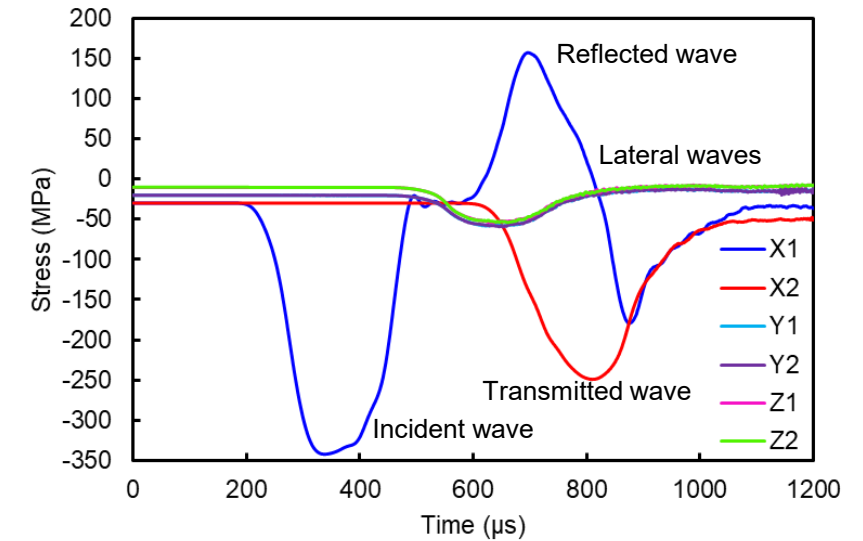
## Wave propagation in X direction



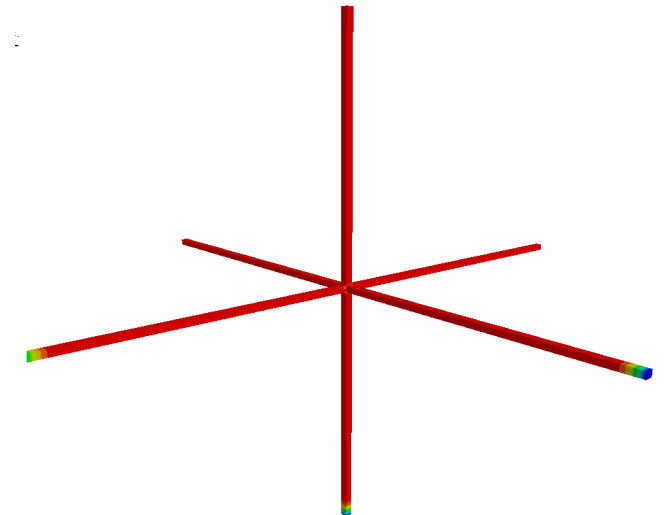
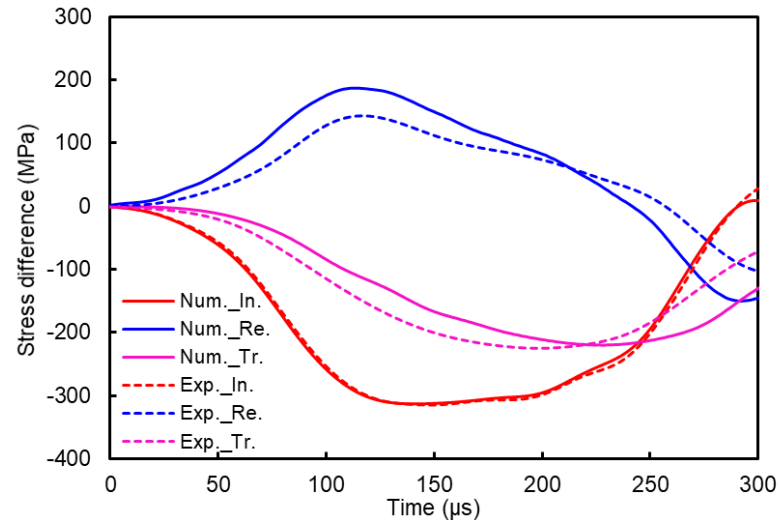
Unit: MPa



## Stress-time history

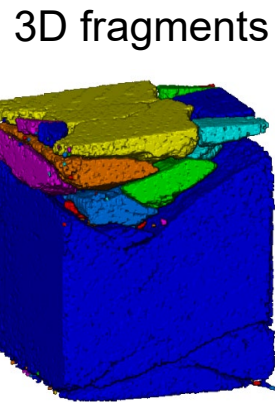
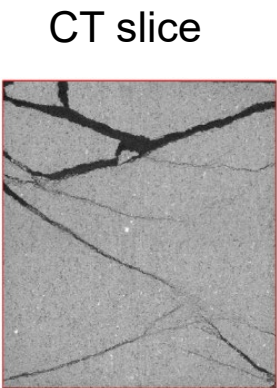
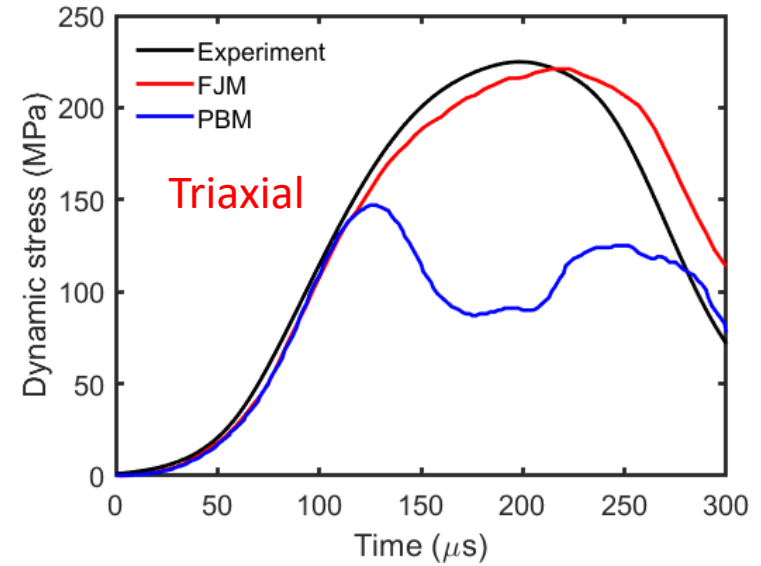
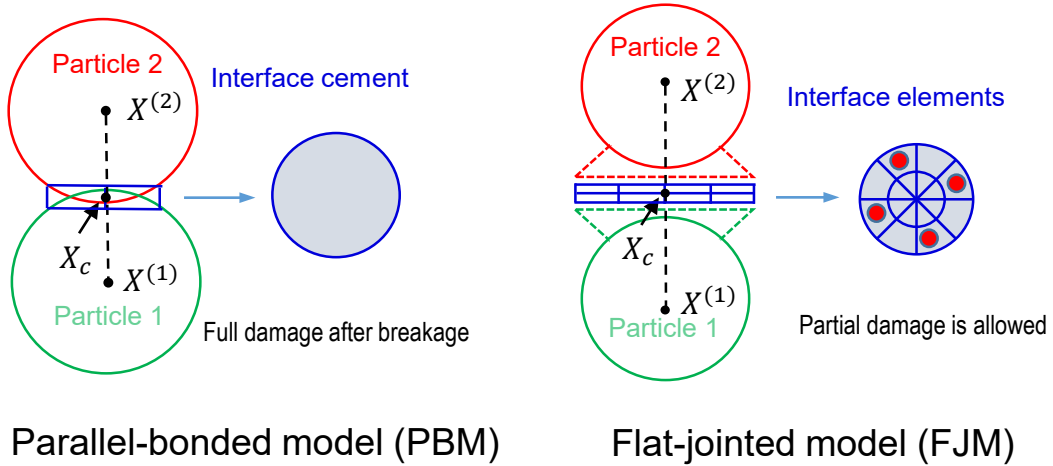


## Comparison in X direction

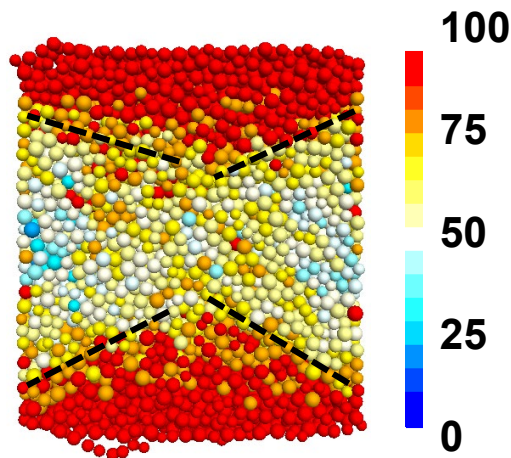


## Impact from multiple directions

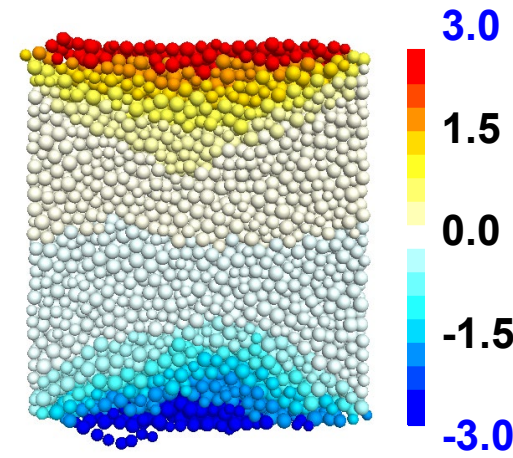
# Damage Pattern



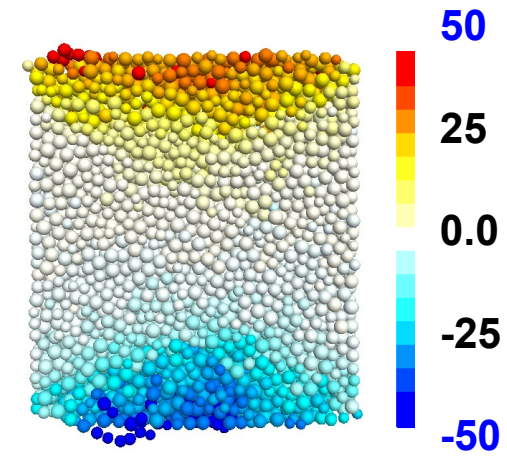
Damage ratio (%)



Z displacement (mm)

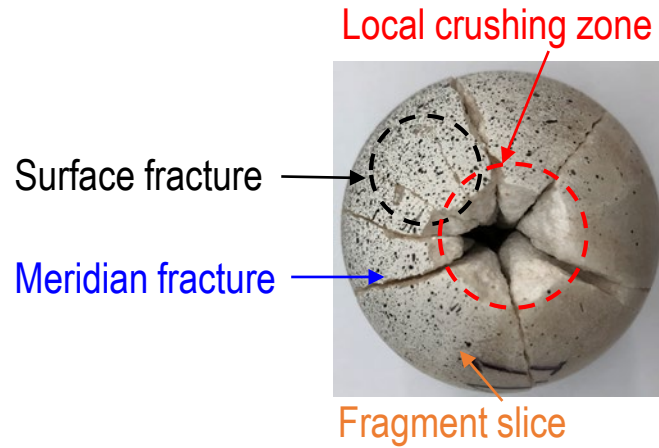


Z velocity (mm)

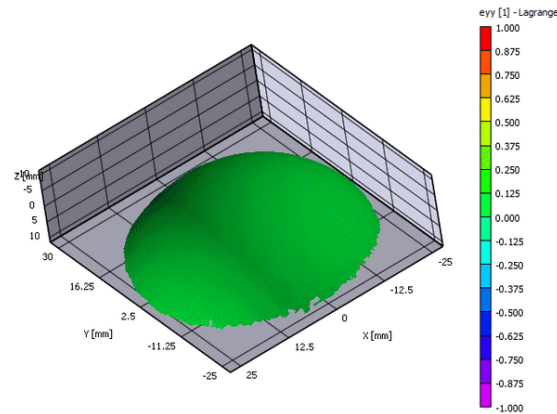
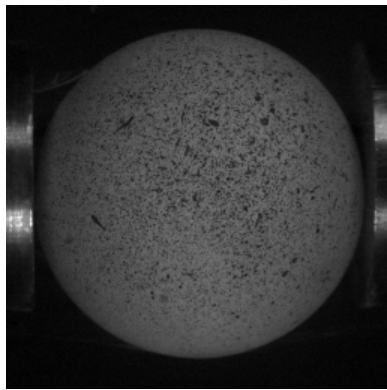


$$\text{Damage ratio} = \frac{\text{Broken contact elements}}{\text{All contact elements}} \times 100\%$$

# Double Impact on Rock Spheres

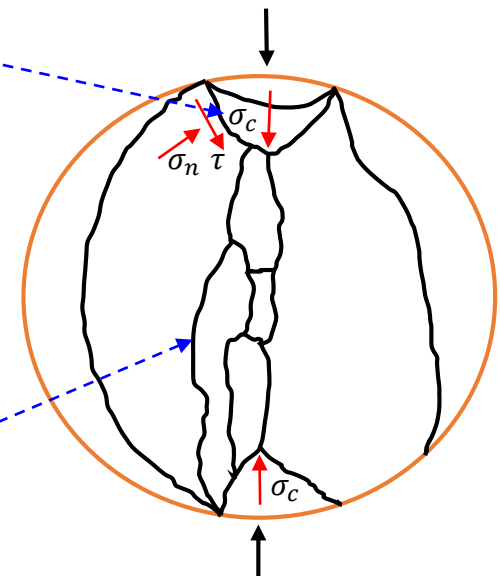
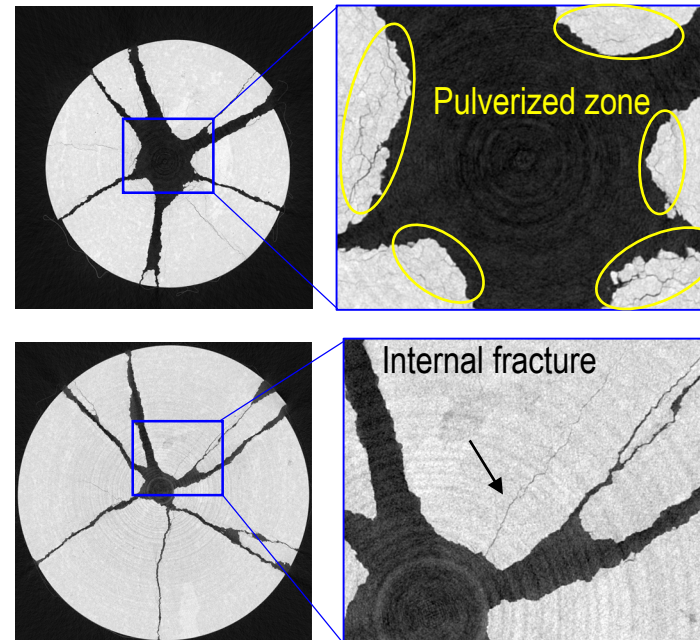


❖ High speed cameras and DIC techniques



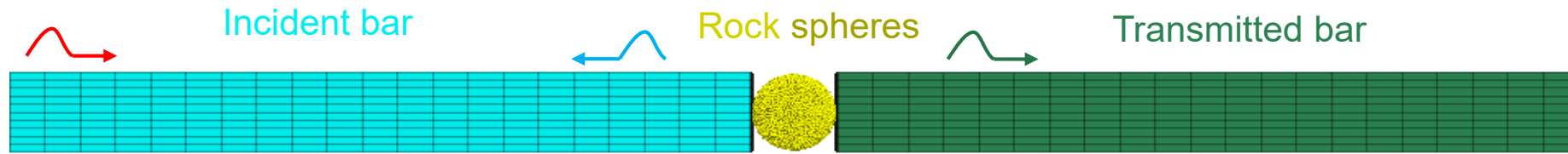
Marble - impact velocity = 9.17m/s

❖ CT slices characterizing fracture and damage



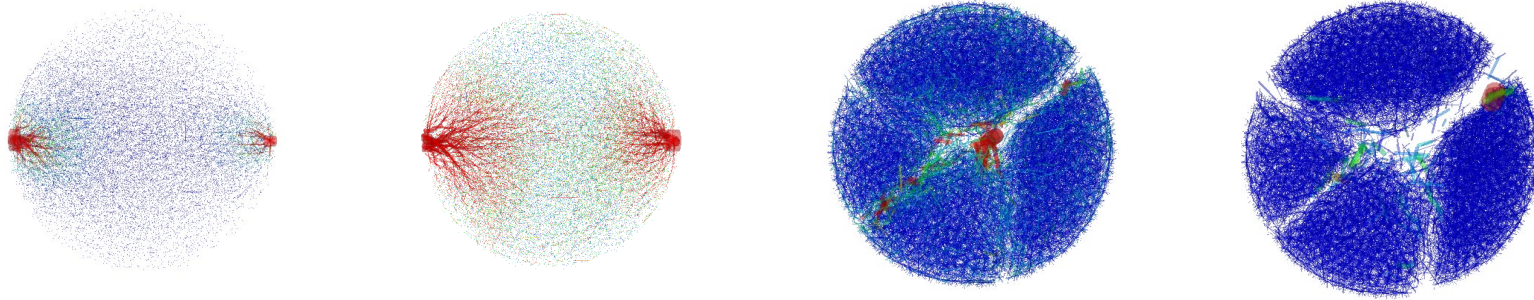


# Numerical Modelling of Double Impact Test on Sandstone

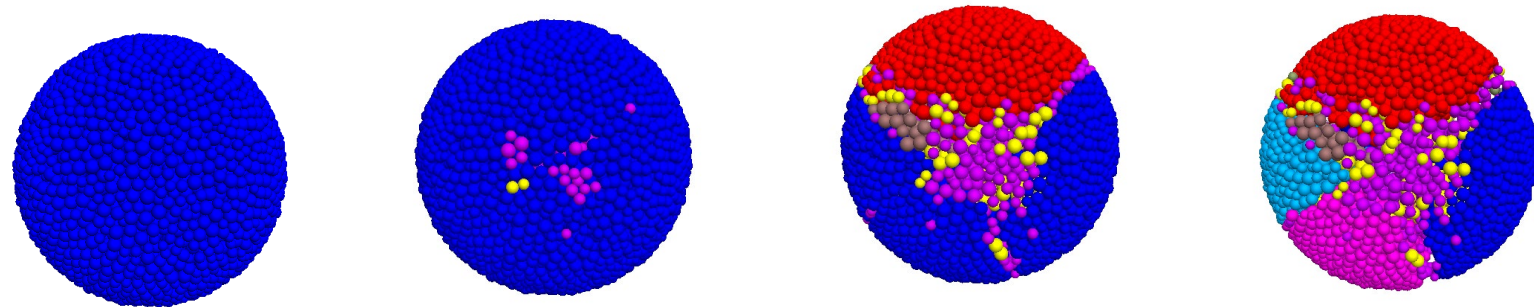


Different loading stages

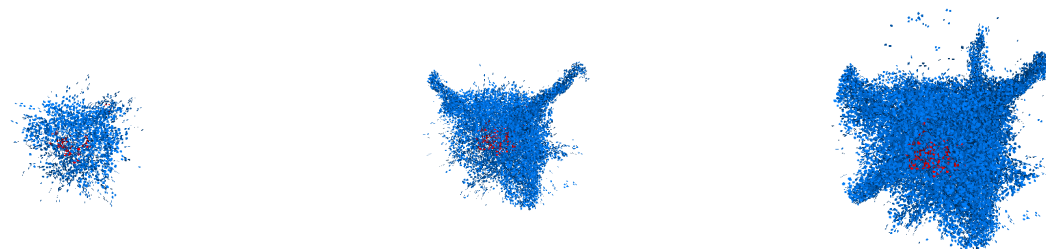
Contact force chain



Fragments



Tensile/Shear Cracks



# Summary and Future Studies

## □ Summary

- The coupled continuum-discrete method can be used to simulate the triaxial Hopkinson bar
- Consideration of rock microstructure represented by 3D FJM contributes to an enhanced dynamic strength
- Similar V-shaped and orange-slice failure pattern of cubic and spherical rock can be observed

## □ Future Studies

- Dynamic constitutive relationship under true triaxial loading condition
- Dynamic fragmentation models considering rock heterogeneity
- Application in prediction of blasting and crushing during mining operations

