

# DEM analysis of the Wolf Rock interlocked masonry lighthouse for extreme wave impacts

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EPICentre: Interdisciplinary Centre for Natural Hazards Resilience





# STORMLAMP

Structural behaviour of rock mounted Lighthouses at the mercy of impulsive waves

**PLYMOUTH  
UNIVERSITY**



UNIVERSITY OF  
**EXETER**

**General Lighthouse Authorities (GLAs)**

Funded by:

**EPSRC**

Engineering and Physical Sciences  
Research Council



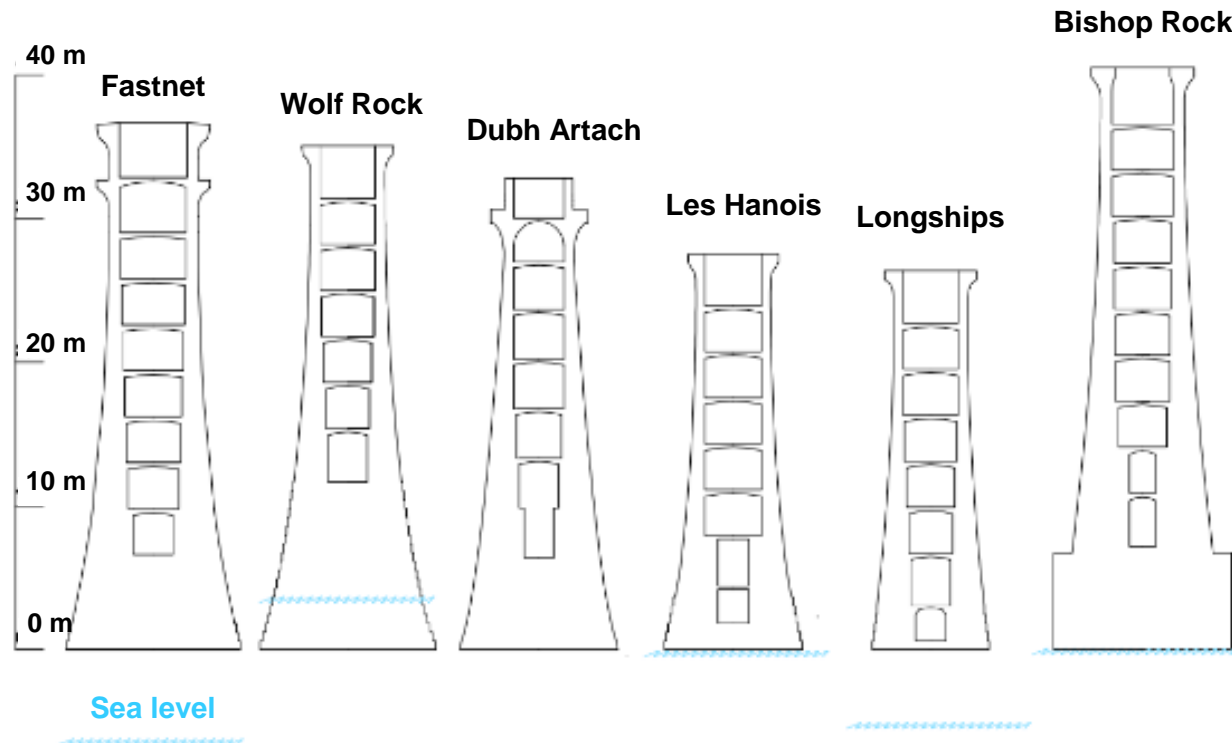
# Why?



## General Lighthouse Authorities (GLAs) – UK & Ireland

- Trinity House (*incorporated in 1514*)
- Northern Lighthouse Board (*incorporated in 1786*)
- Commissioners of Irish Lights (*incorporated in 1786*)

## GLAs Question: Are our lighthouses safe against extreme wave impacts?

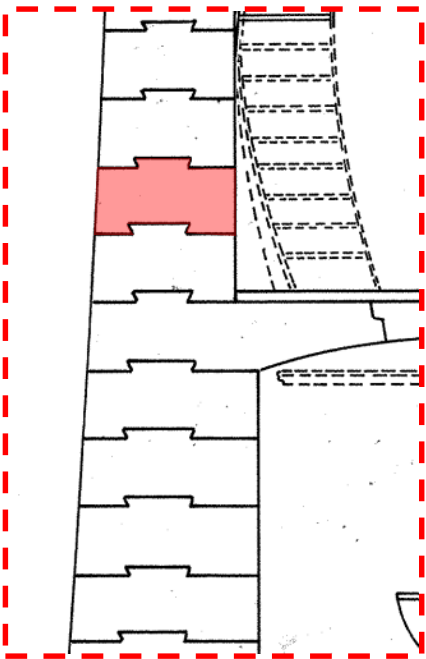
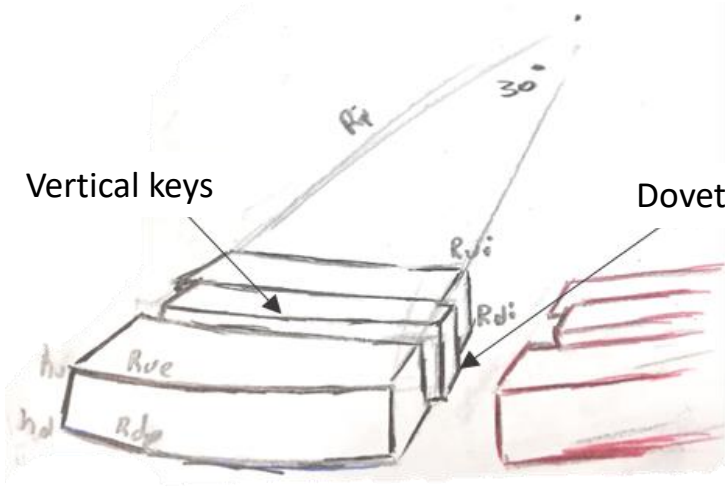




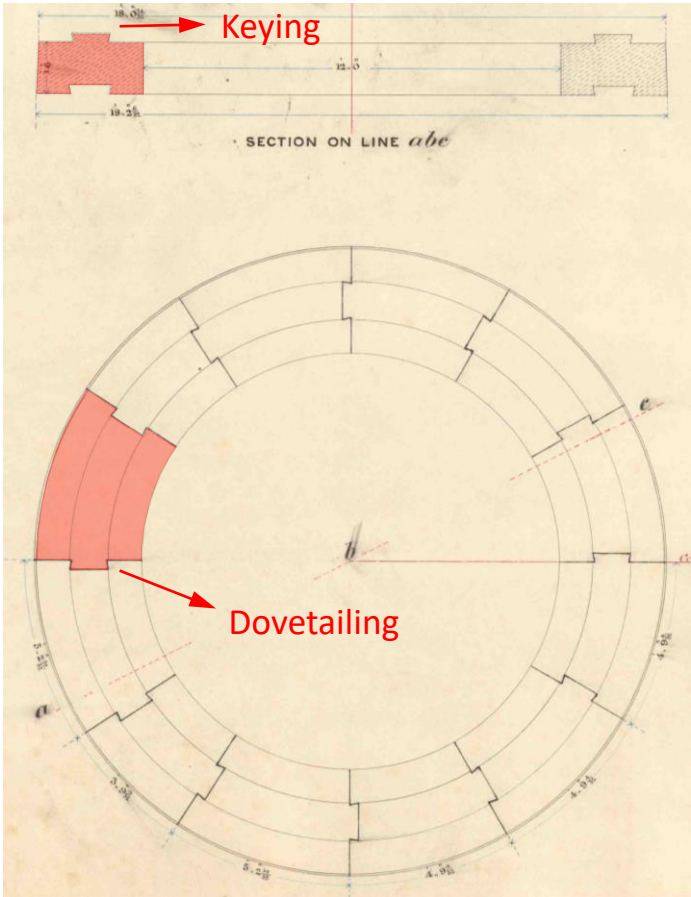
# DESCRIPTION

## Wolf Rock lighthouse

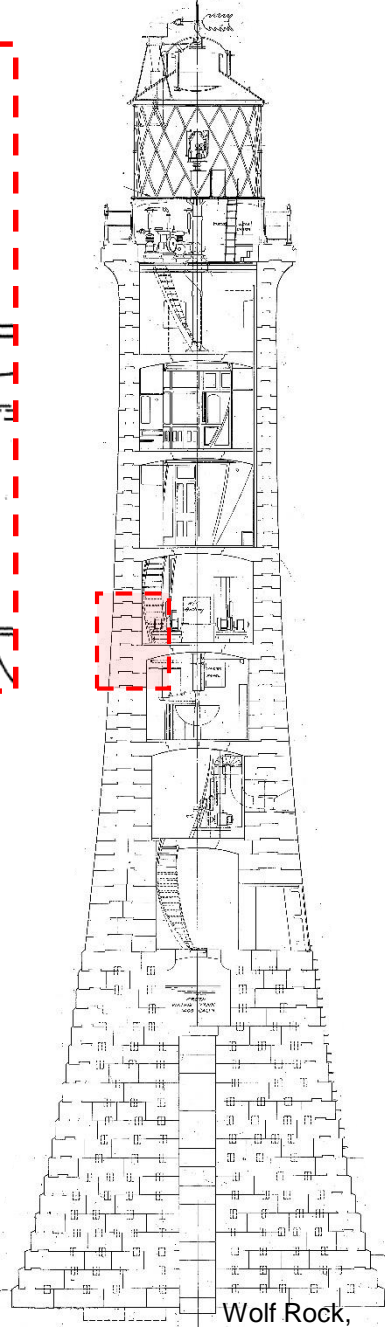
- Construction: 1869
- Height: 35 m
- Typology: Granite interlocked masonry
- Horizontal connections: Dovetailed
- Vertical connections: Keys
- 3570 metric tonnes



Wolf Rock, 22 Feb 2018



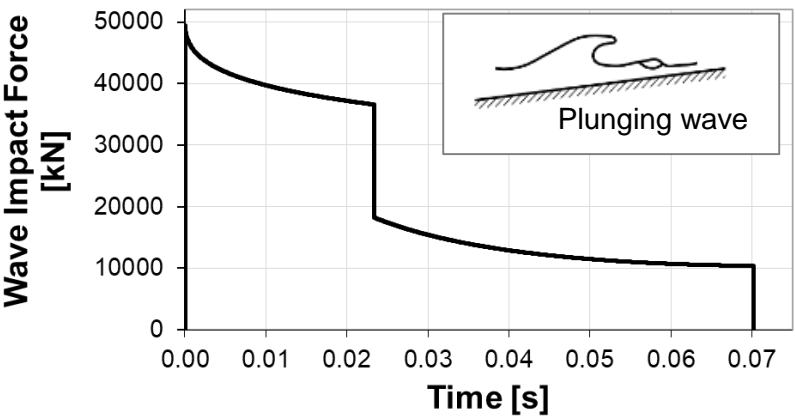
Interlocking prevents sliding but allows uplift



# What are the wave forces?

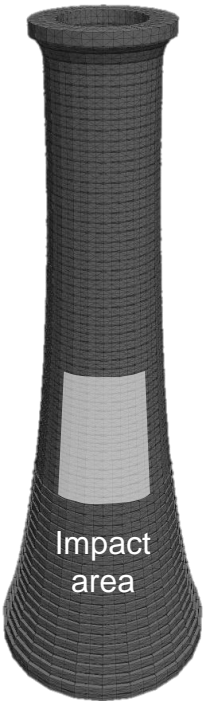


250 years return period wave impact

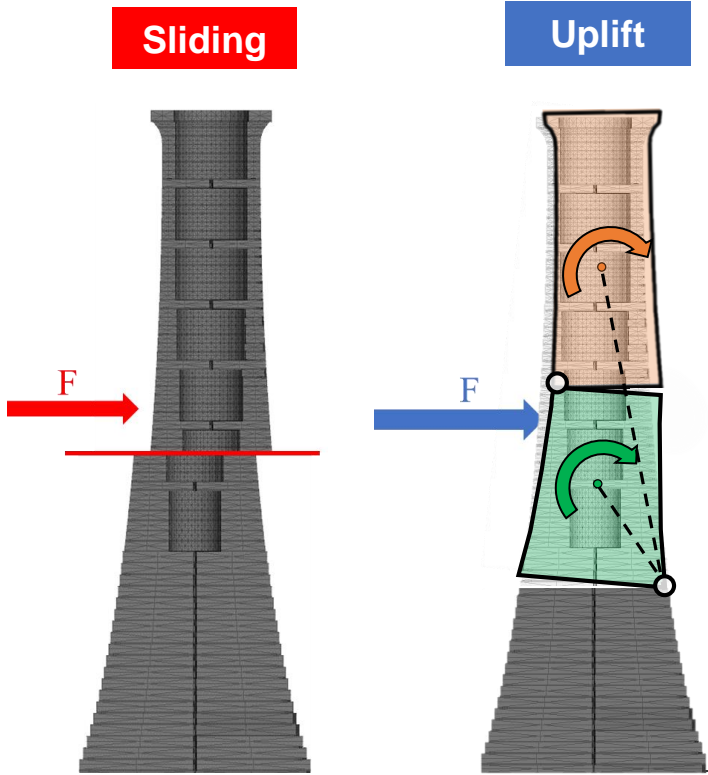


## Impact

- Very short duration (0.07s)
- Very high max force (49510 kN)



# What is the structural response?

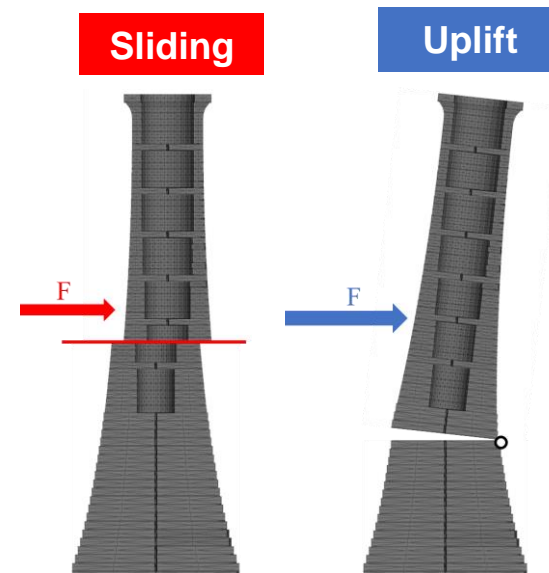


“A lighthouse-tower might be **destroyed in either of two** ways, either by being moved bodily by the **sliding** of the base upon its foundation, or by being fractured at some point in its height, and the **upper portion being overthrown**.”

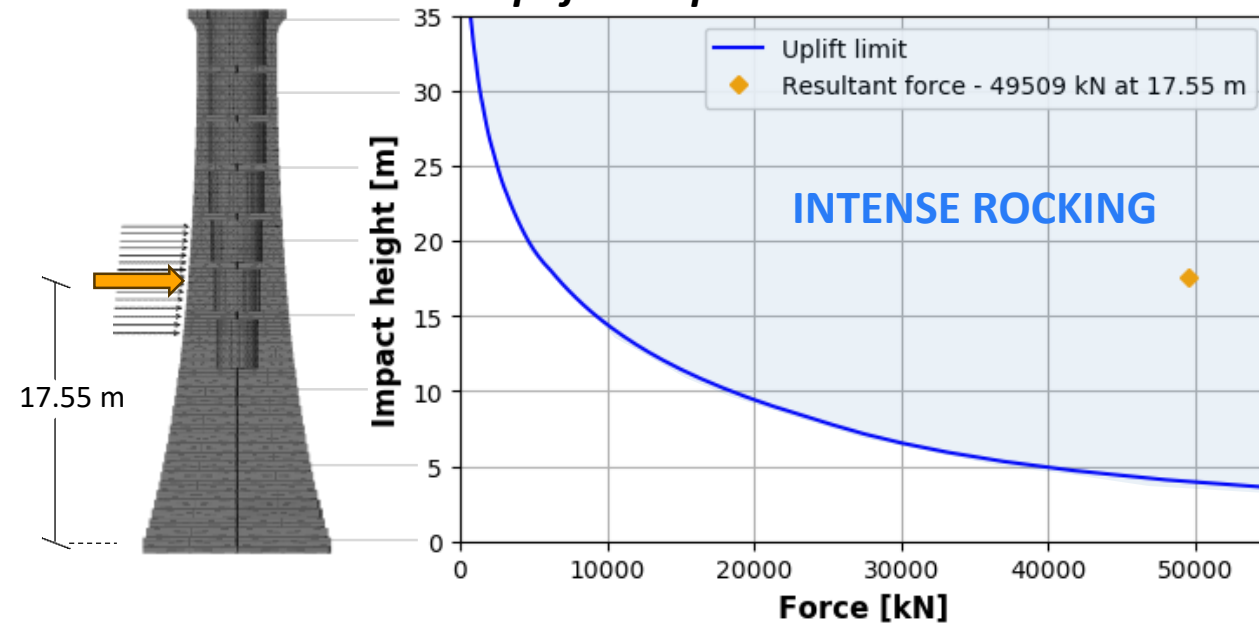
ICE Proceedings, Vol. 75, 1884

# Limit Analysis

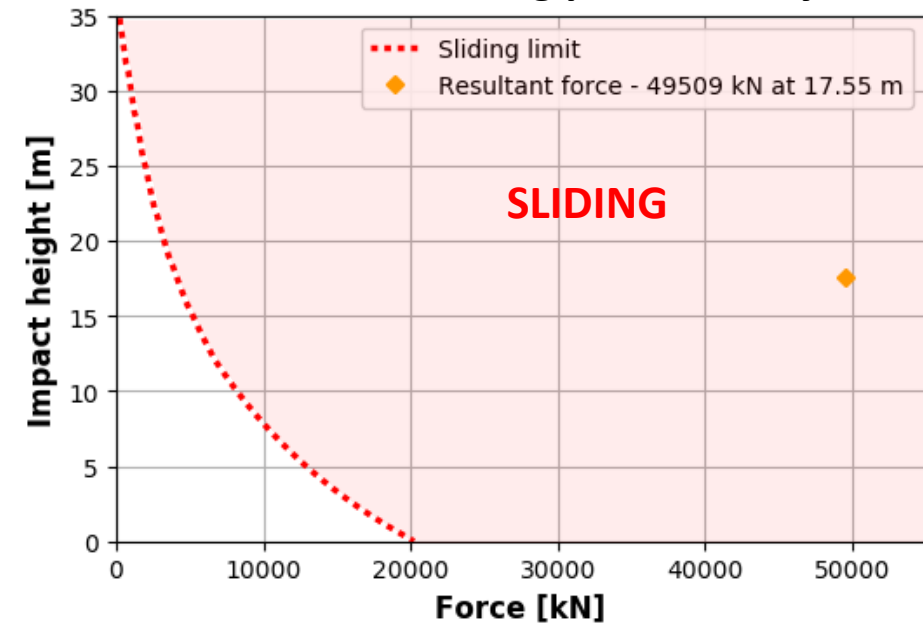
- Calculates the critical **uplift load**
- Calculates the critical **sliding load**
- Useful tool for **preliminary assessment** and **prioritisation** of detailed analysis and interventions



**Resultant force >> Uplift limit**  
**Uplift is expected !**



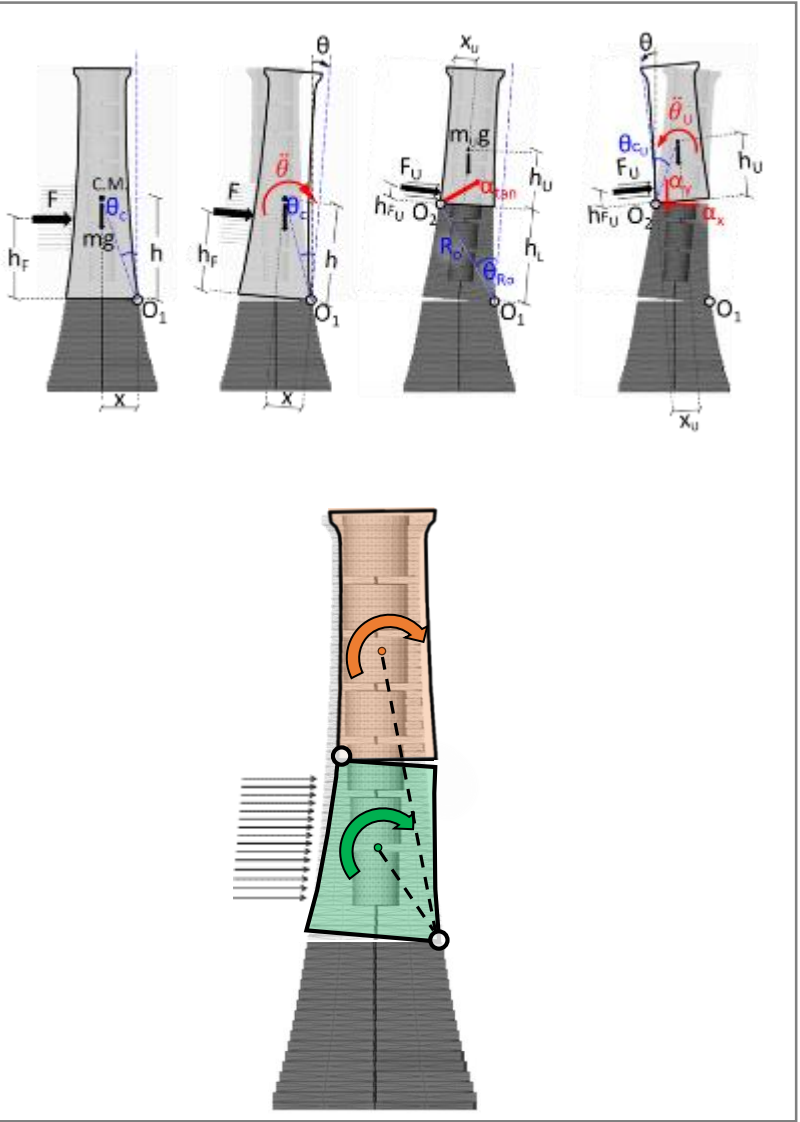
**Resultant force >> Sliding limit**  
**But... the interlocking prevents any sliding !**



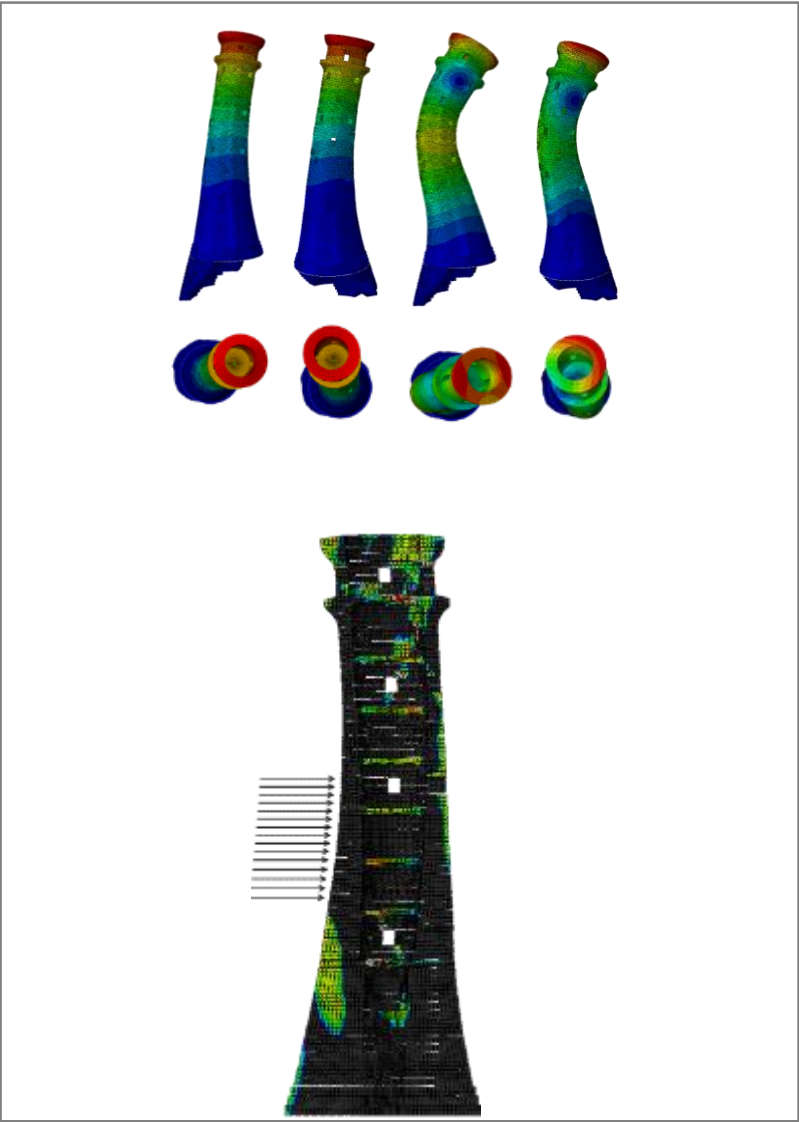


# What structural analysis tool?

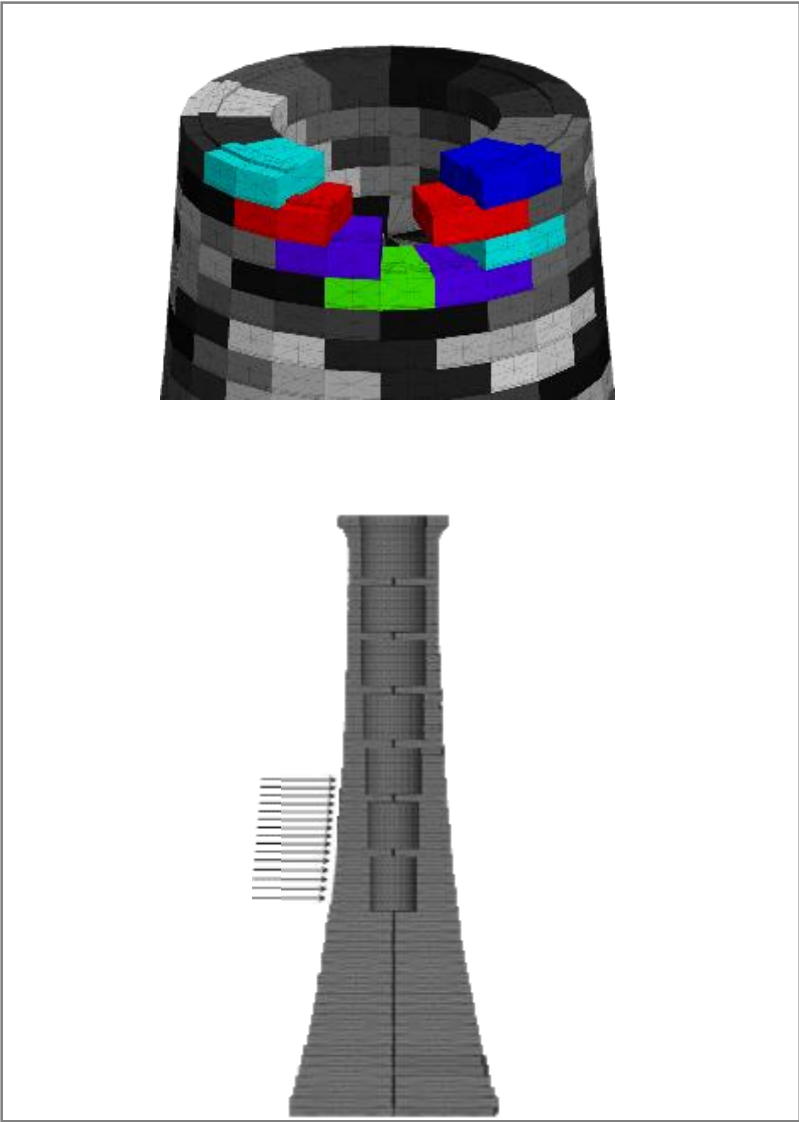
## ROCKING ANALYTICAL FORMULATIONS



## FINITE ELEMENT METHOD (FEM)



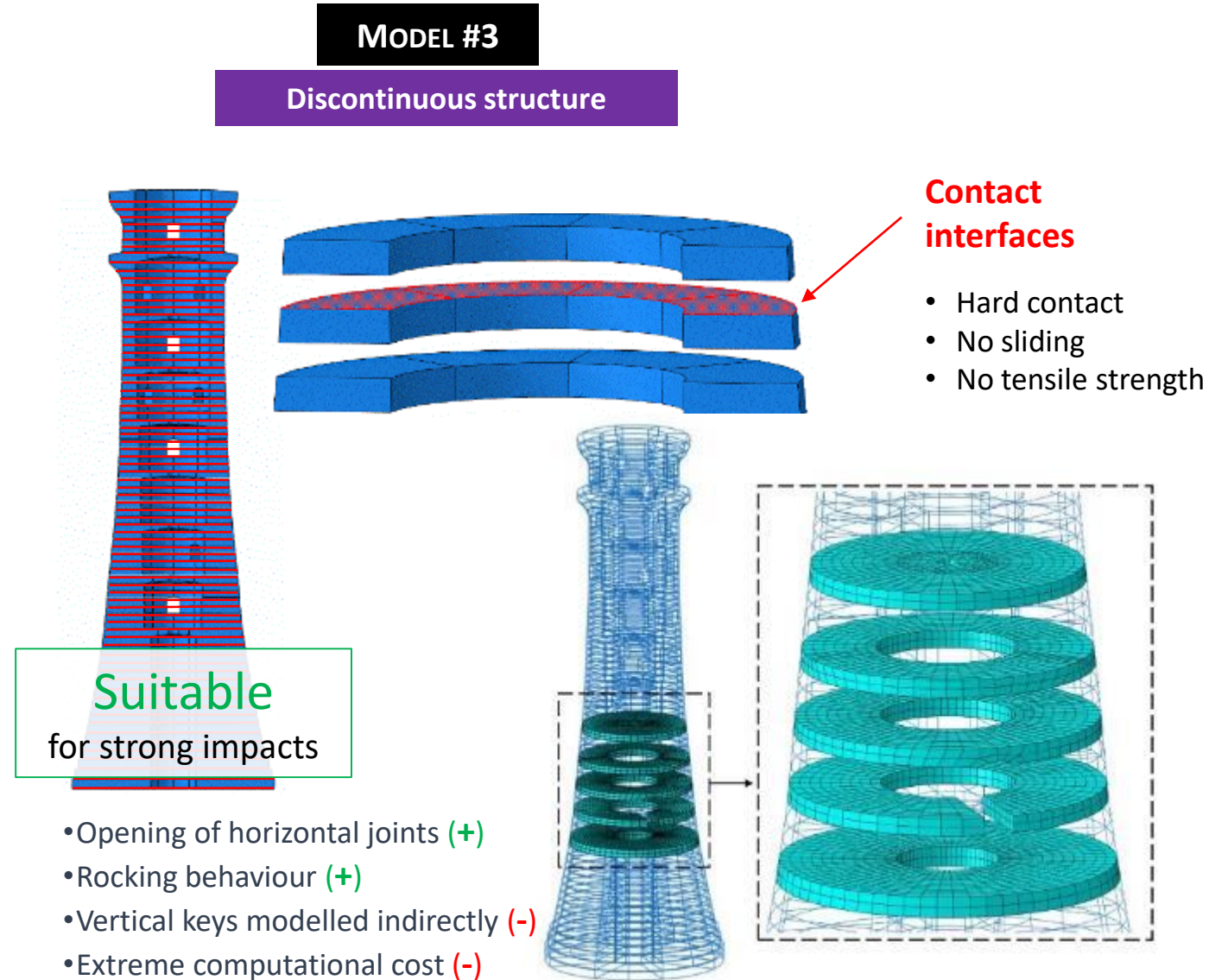
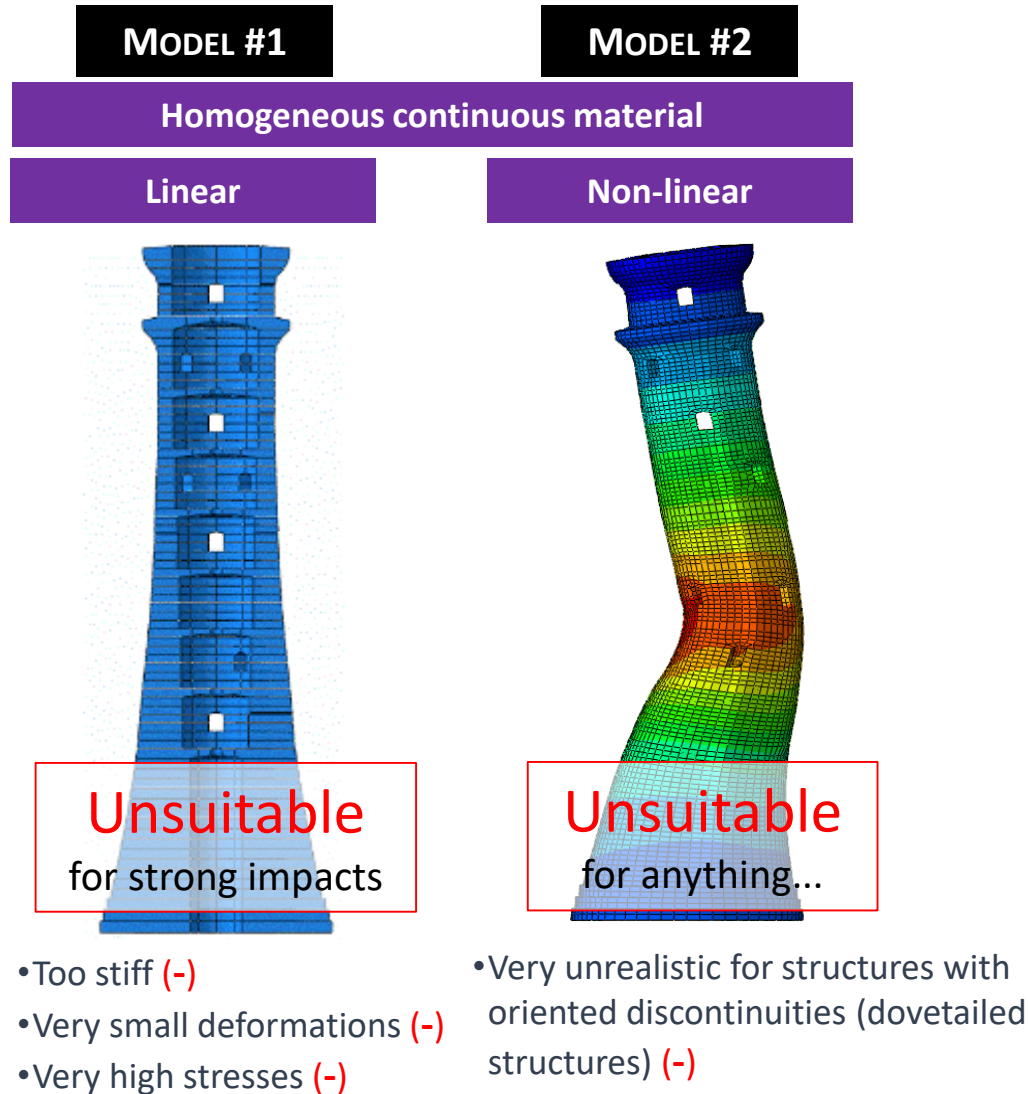
## DISTINCT ELEMENT METHOD (DEM)



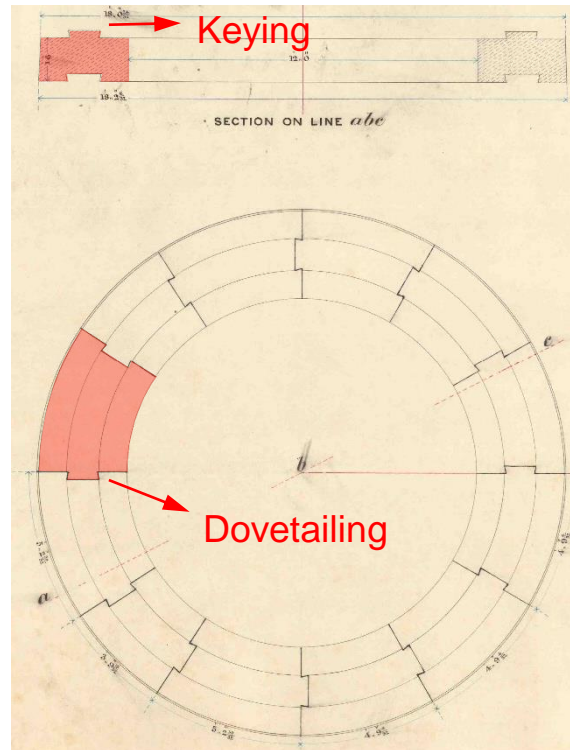
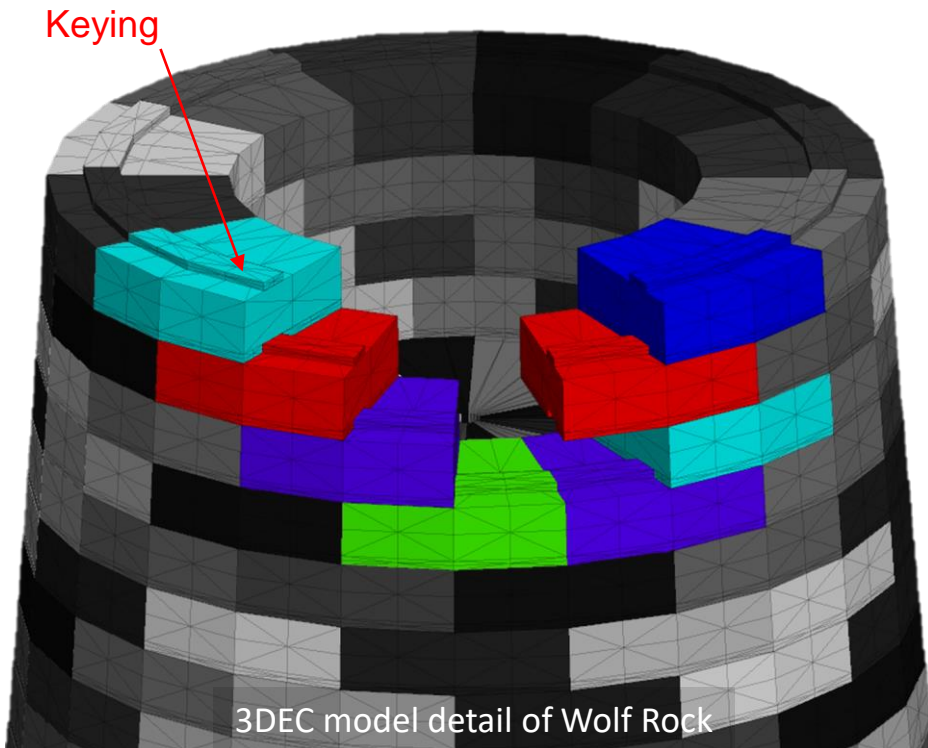


# FEM Software: **Abaqus 6.14** (Dassault Systèmes)

- The discontinuous structure has a highly nonlinear behaviour.
- Different FEM modelling approaches were tested.



- Allows **detachment and separation** of blocks → Essential for this **non-continuous** structure
- Detailed geometry based the **archive drawings** → **Python script** was developed
- The courses created as rings with '**drum**' and '**tunnel**' commands
- Only the **vertical keys** were modelled (no dovetails) → Sliding is prevented; Uplift is allowed
- The model was simplified to **12 blocks** per course



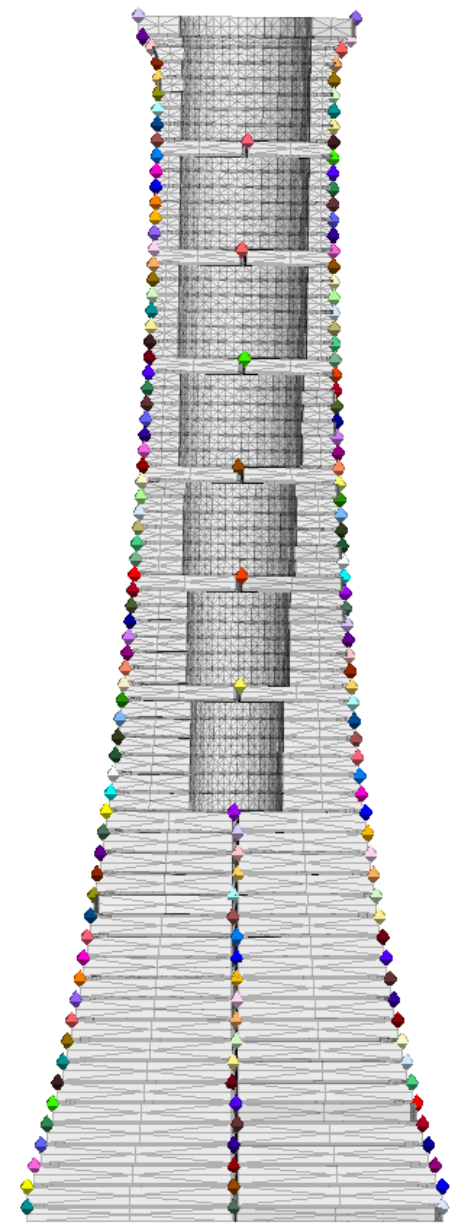


## Model properties

- **Joint normal stiffness** =  $7.31 \cdot 10^{10}$  Pa/m  $\rightarrow$  equivalent compressive Young's modulus of 37 GPa (accounted as 69 in-row springs).
- **Joint shear stiffness** =  $5.48 \cdot 10^{10}$  Pa/m.
- Friction angle =  $30^\circ$
- **Mass proportional Rayleigh damping 0.75% at 4.67 Hz**  $\rightarrow$  based on field modal tests (Brownjohn et al. 2017).

## Outputs

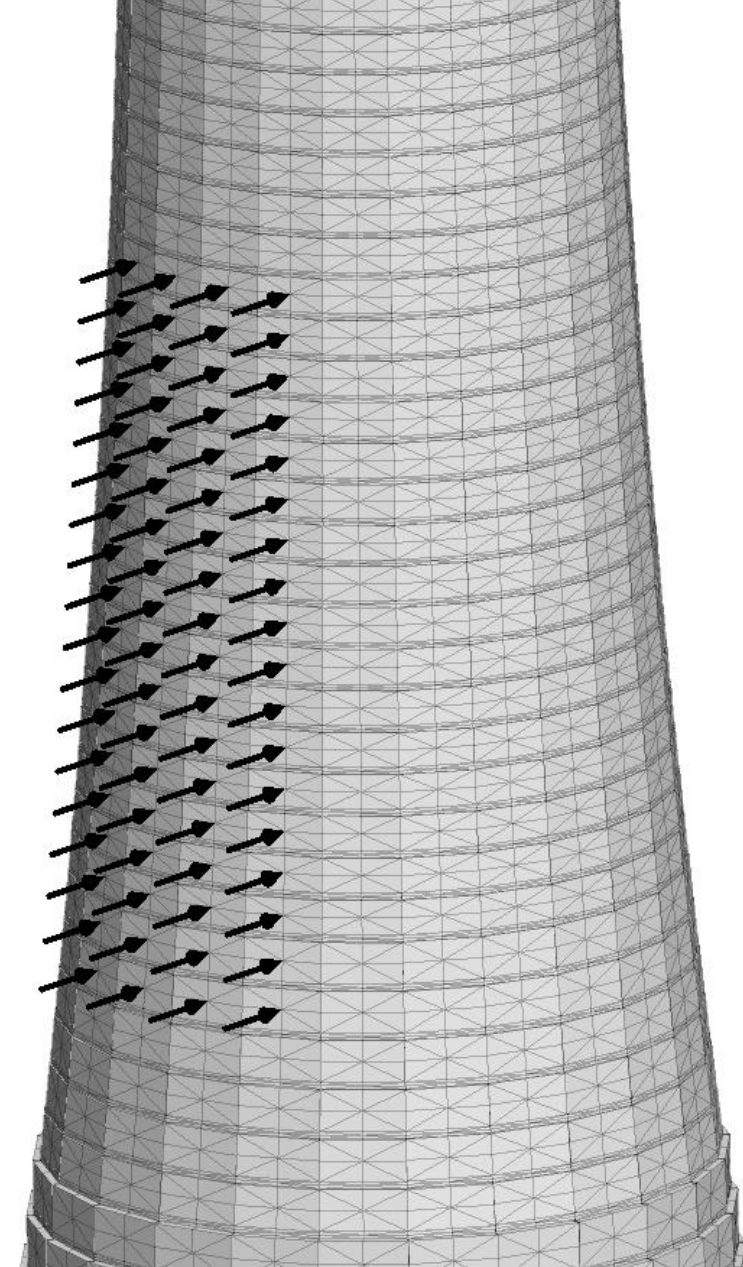
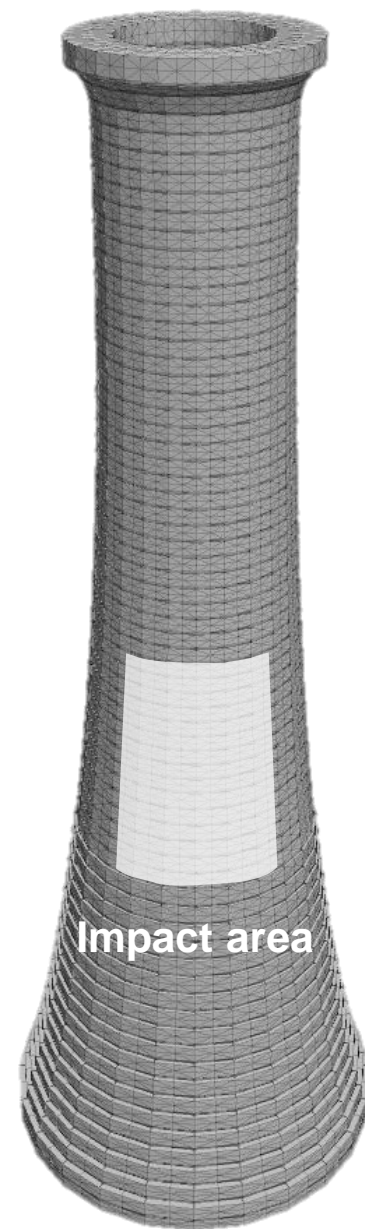
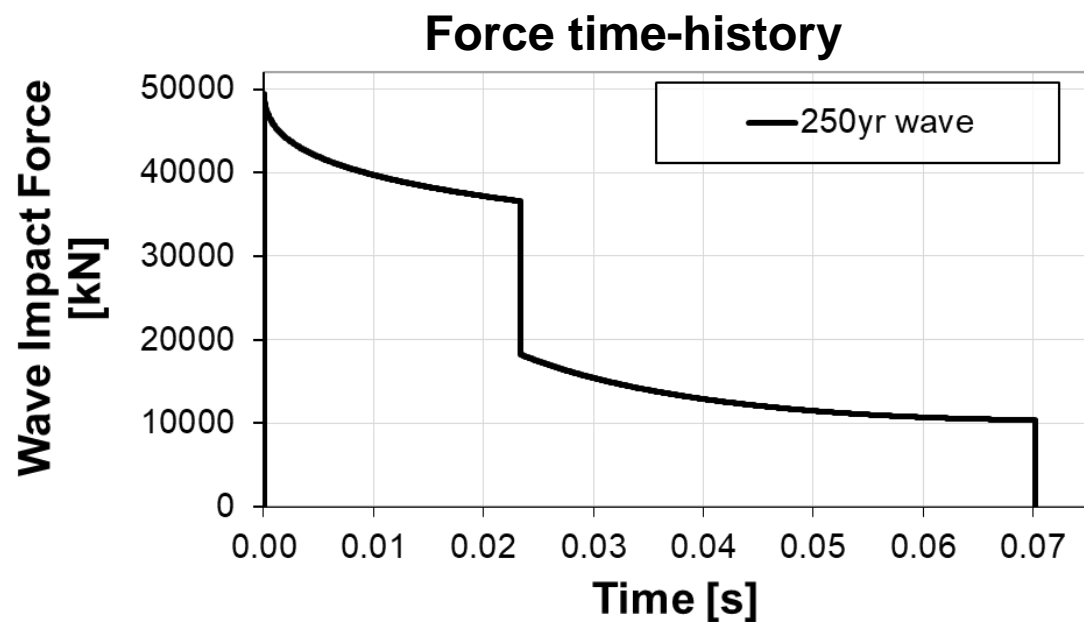
- Horizontal & vertical displacements
- Horizontal & vertical velocities
- 385 histories



Control points

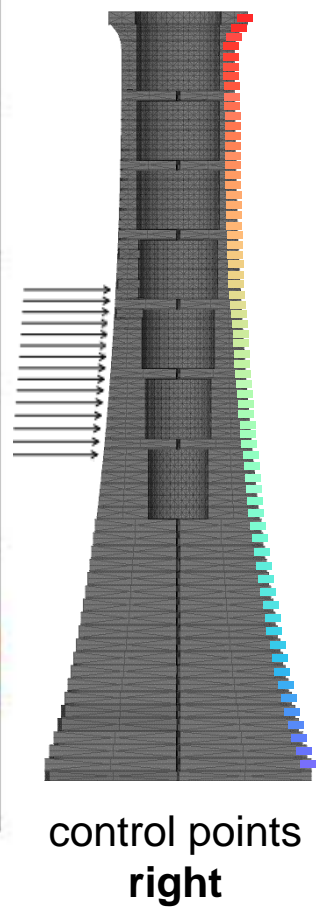
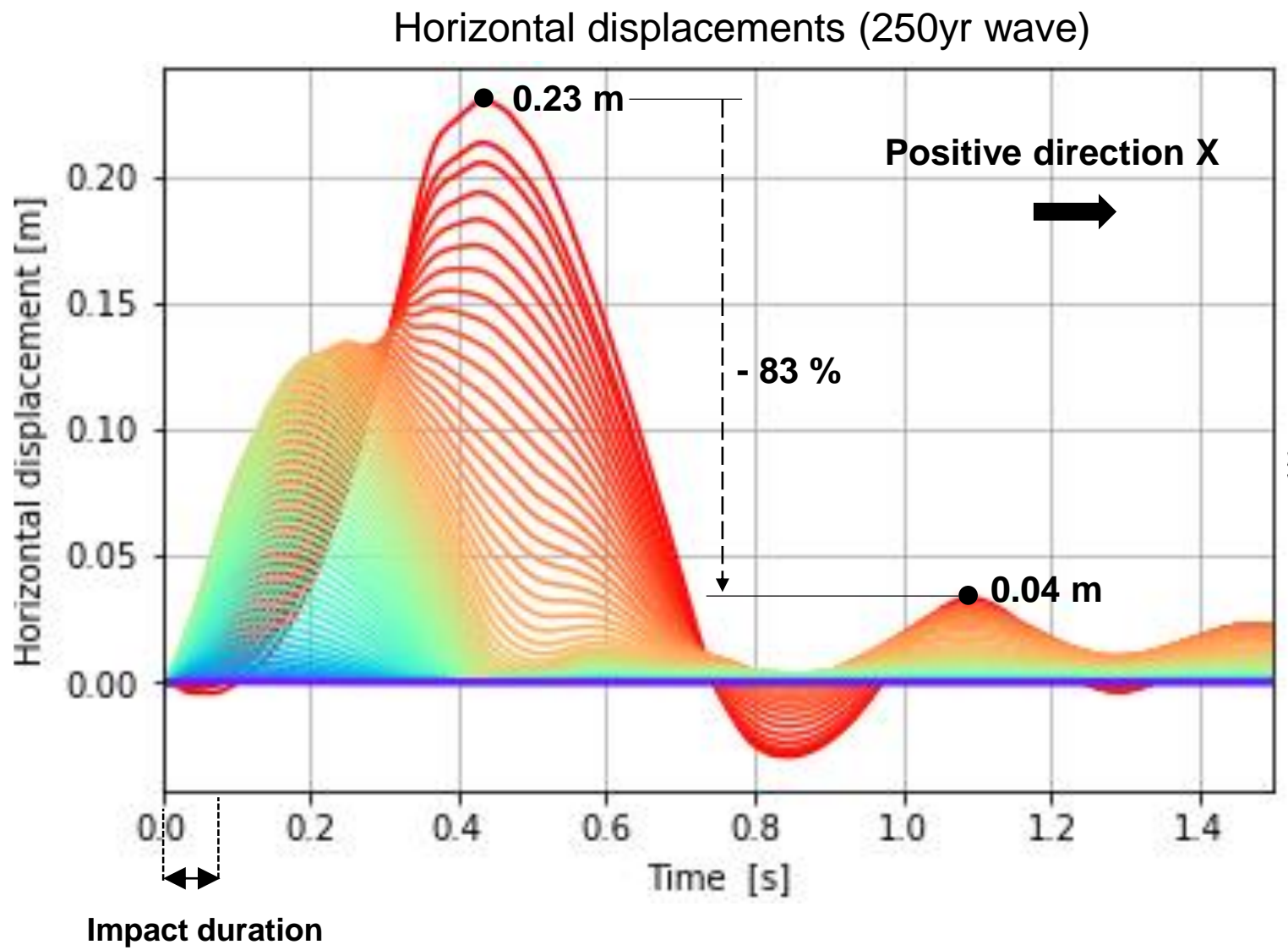
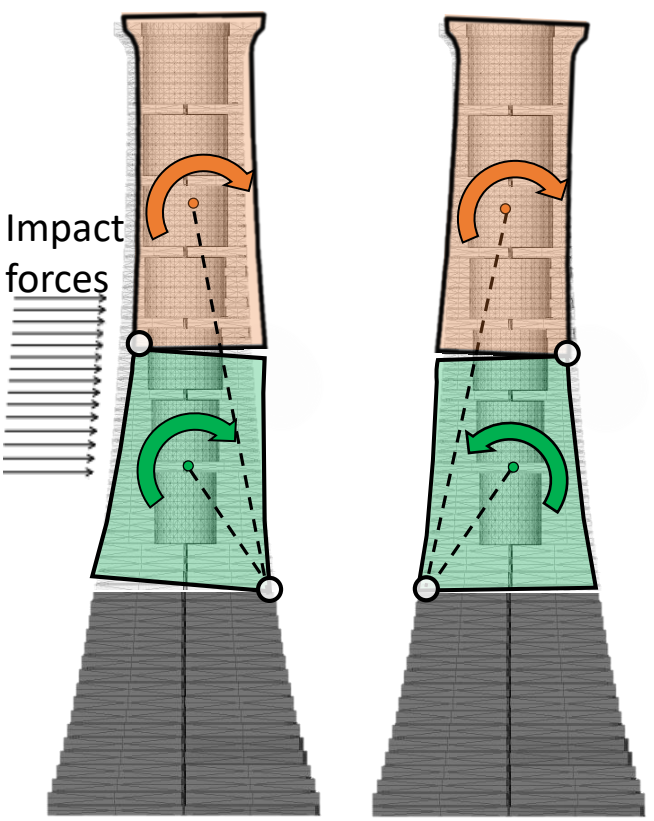
## Wave impact load

- Applied as **force time-history**
- Distributed **uniformly** in 68 points
- Frontal section of **60°**
- Resultant Force at **17.55 m** from the base

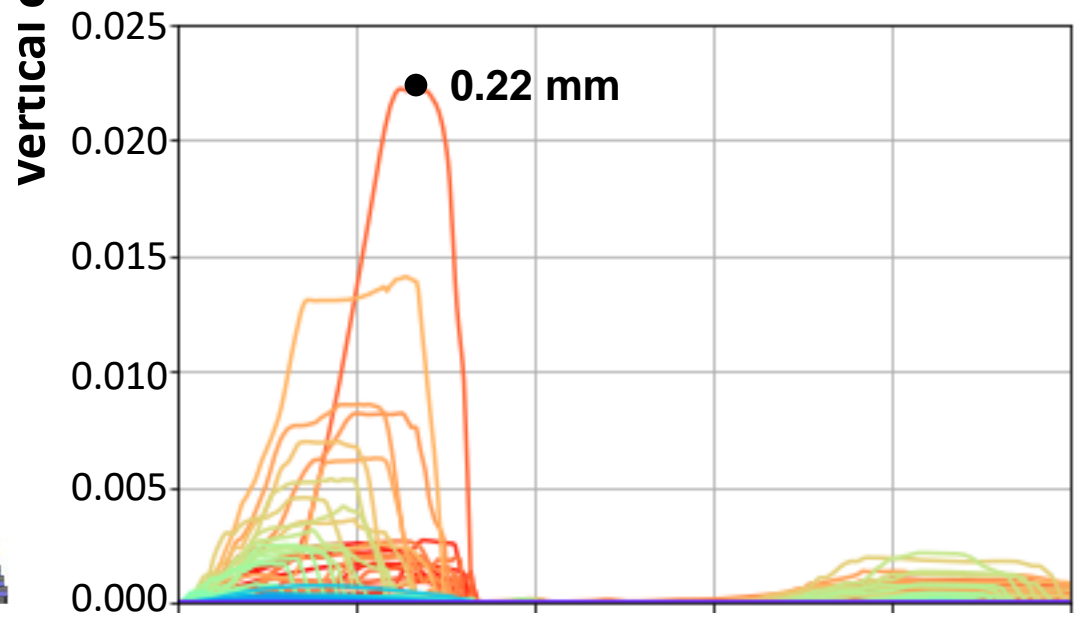
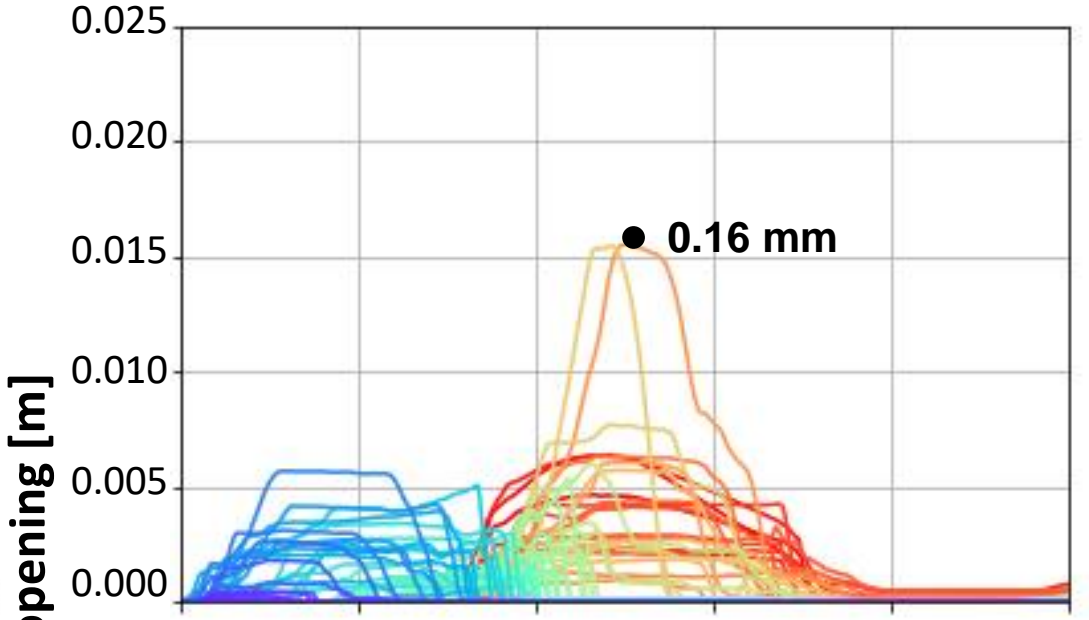
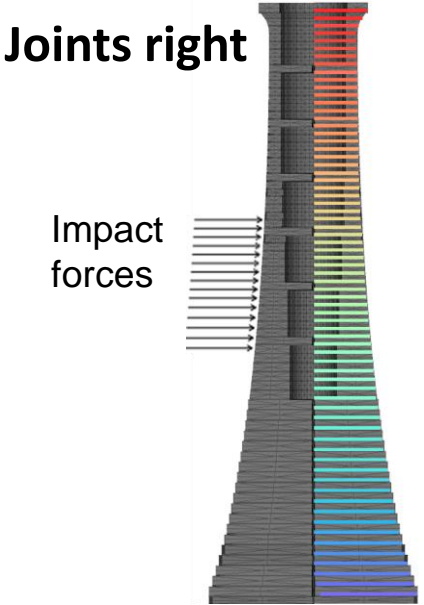
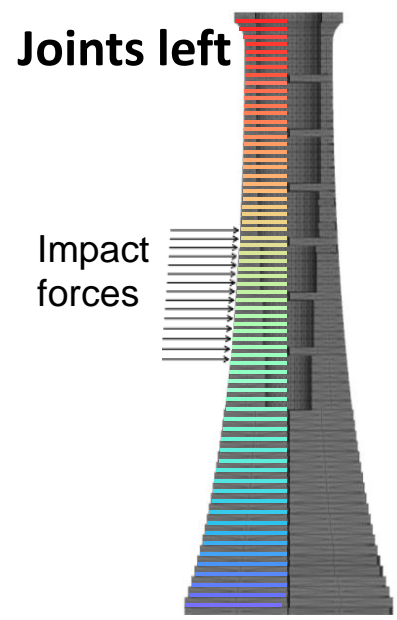
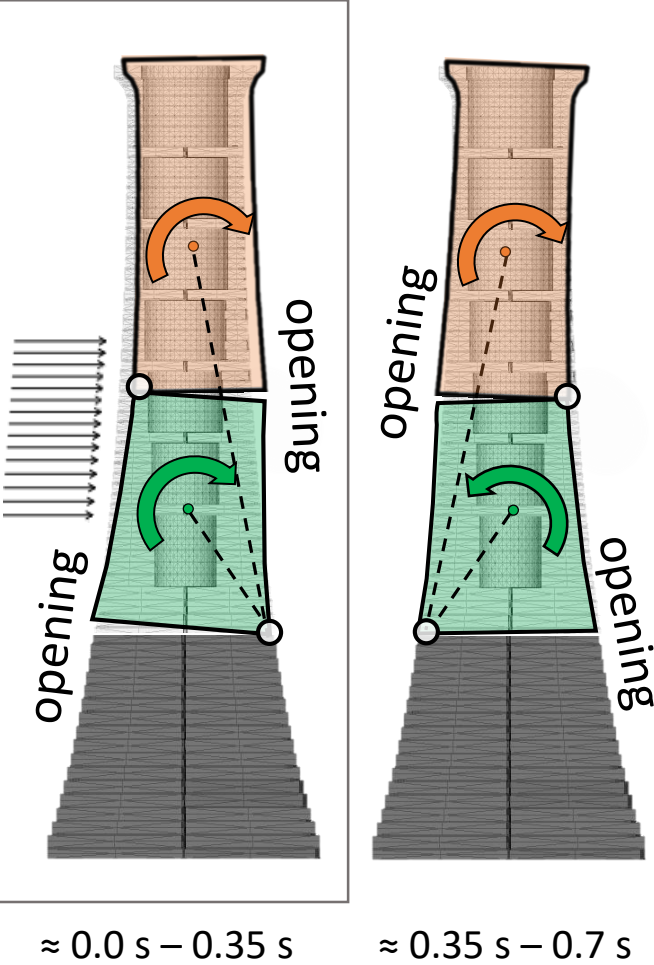




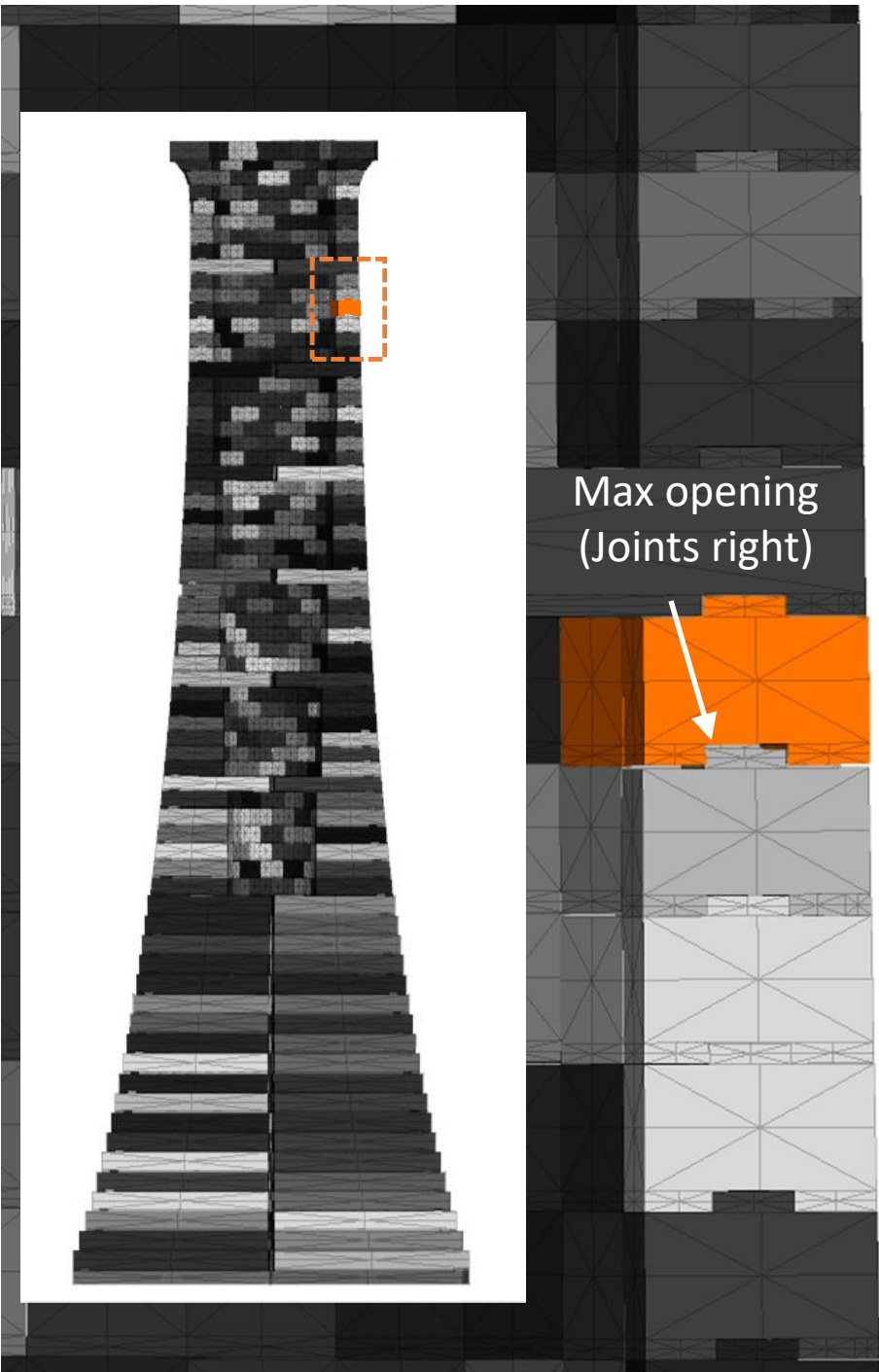
# Horizontal displacements



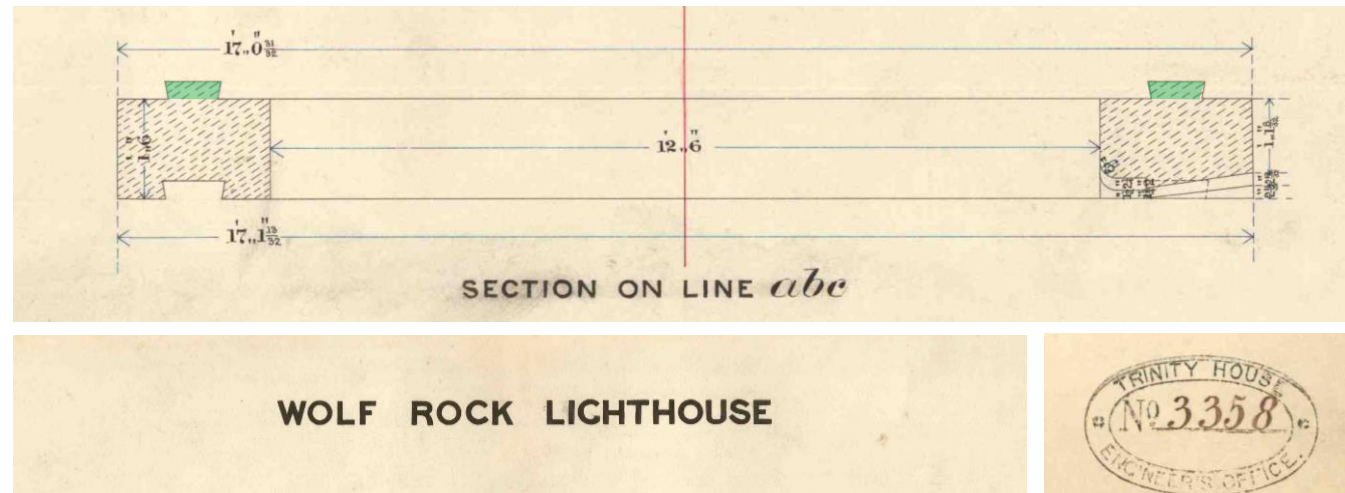
# Joint opening







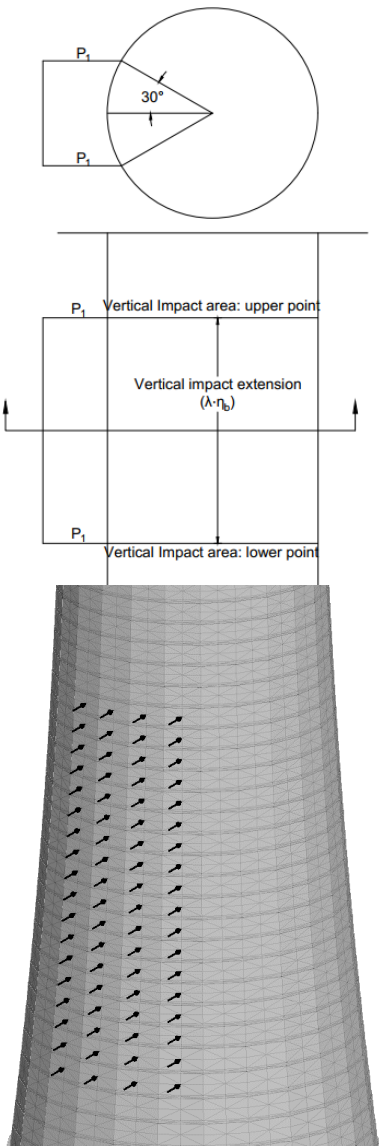
Max joint opening: 22 mm < Vertical key (76 mm)



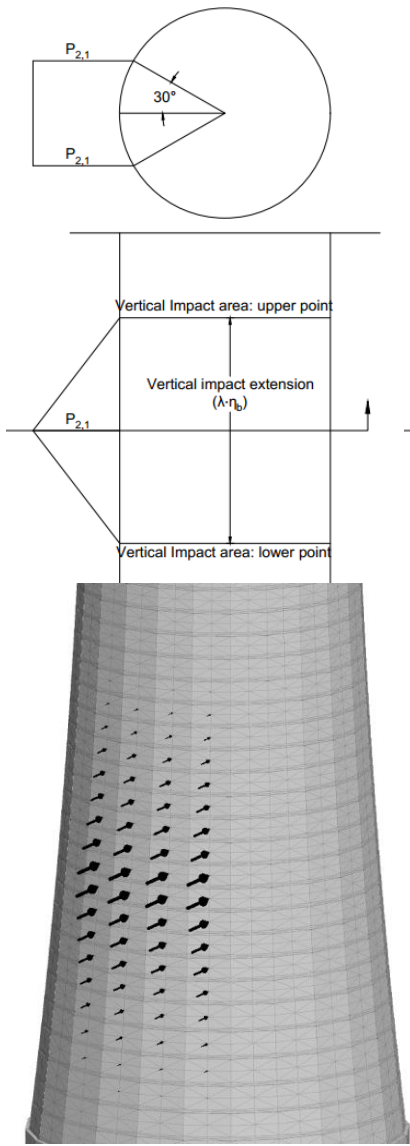
Sliding failure is prevented

# How does the wave force **spatial distribution** influence the lighthouse response?

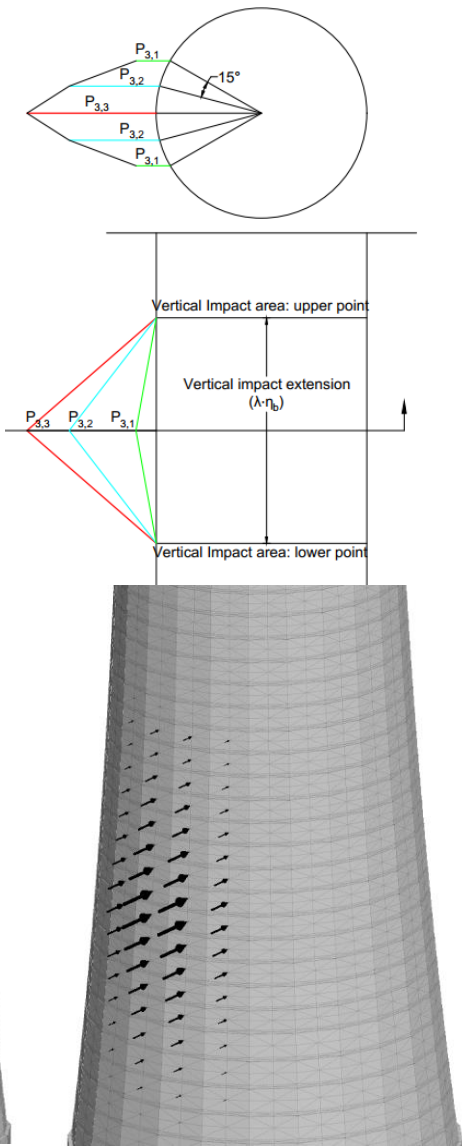
DISTRIBUTION #1



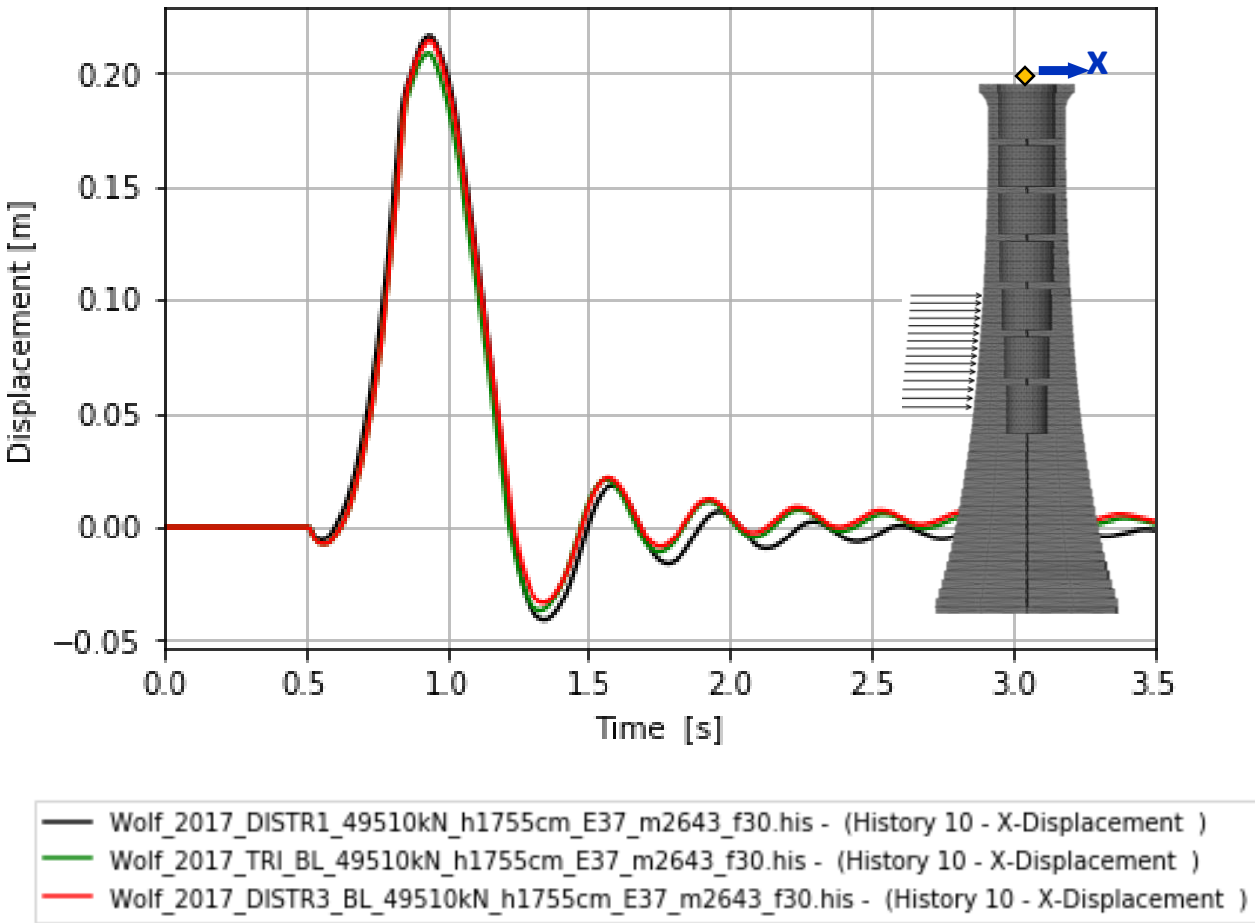
DISTRIBUTION #2



DISTRIBUTION #3



Horizontal displacement on top  
Wolf Rock



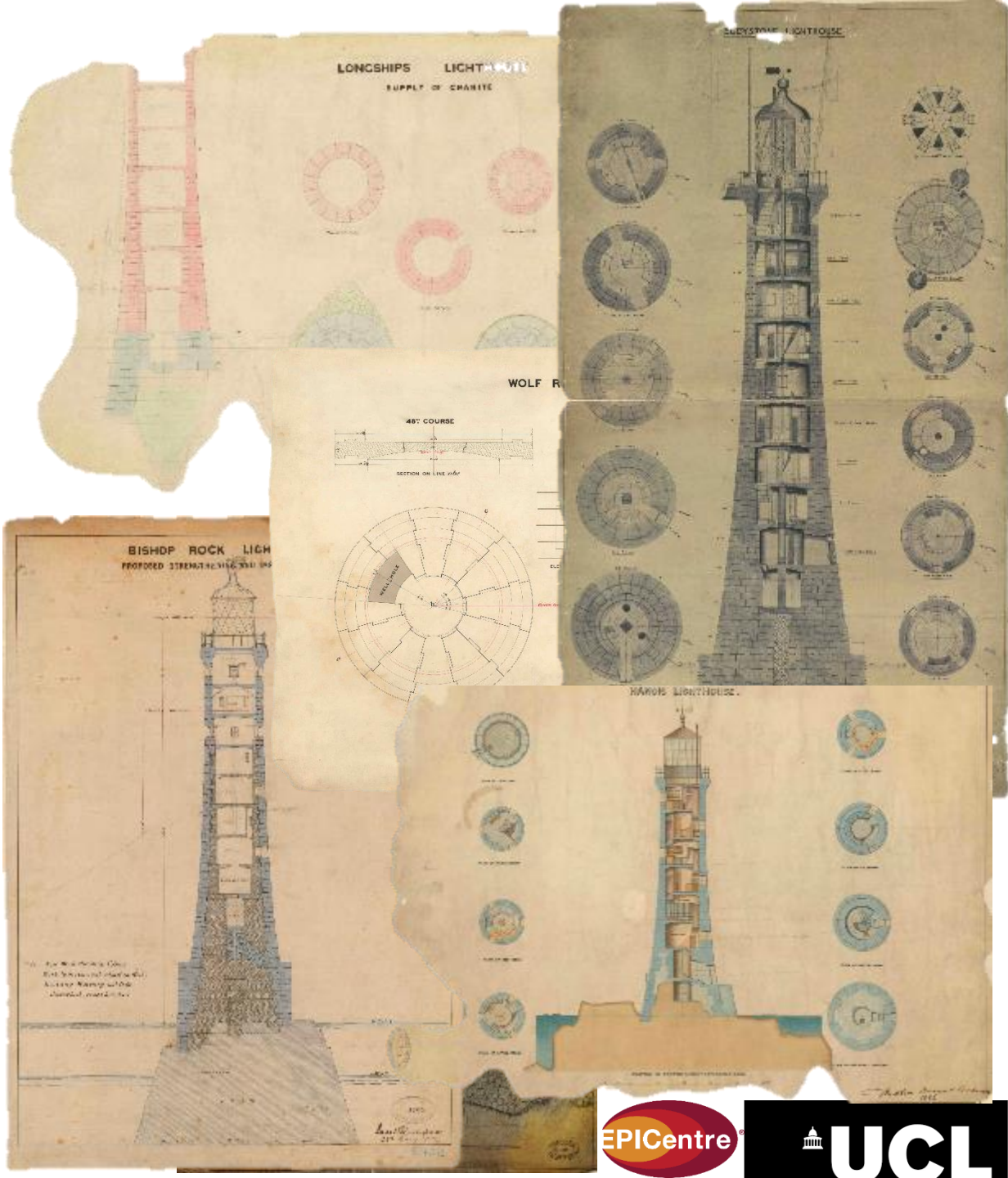


# CONCLUSIONS

- Detailed structural analysis needs **discontinuous model**, i.e. FEM with interface contacts or DEM
- The wave force **time-history type** influences the structural response far more than the **pressure distribution**
- The lighthouses have survived till now to a great extent thanks to the **vertical keys**
- Wolf Rock will **vibrate intensely** for the calculated **250 years** return period wave, but it **will not fail**.

## Acknowledgments to:

- The Engineering and Physical Sciences Research Council (EPSRC) for the financial support of the STORMLAMP project EP/N022947/1, EP/N023285/1
- The Trinity House for the provision of detailed drawings and for physical access to the Wolf Rock lighthouse



# STORMLAMP project

More resources at: <https://stormlamp.org.uk/>

## (Some) Publications

- Brownjohn, J., Raby, A., Bassitt, J., Hudson, E., & Antonini, A. (2017). Modal testing of offshore rock lighthouses around the British Isles. *Procedia Engineering*, 199, 3326–3331. <http://doi.org/10.1016/j.proeng.2017.09.440>
- Pappas, A., D'Ayala, D., Antonini, A., Brownjohn, J., & Raby, A. (2017). Numerical modelling of Fastnet lighthouse based on experimental dynamic identification. In *International Conference on Advances in Construction Materials and Systems ICACMS-2017*. Chennai.
- Antonini, A., Raby, A., Brownjohn, J., Pappas, A., & D'Ayala, D. (2018). Survivability assessment of Fastnet lighthouse. In *36th International Conference on Coastal Engineering ICCE-2018*. Baltimore
- Antonini, A., Raby, A., Caputo, P., Brownjohn, J., Pappas, A., & D'Ayala, D. (2018). An integrated approach for marine structures survivability assessment: the Fastnet lighthouse within the STORMLAMP project. *XXXVI Convegno Nazionale di Idraulica e Costruzioni Idrauliche Ancona, 12-14 September 2018*
- Brownjohn, J., Au S., Wang X., Zhu Z., Raby, A., & Antonini, A. (2018). Bayesian operational modal analysis of offshore rock lighthouses for Structural Health Monitoring. *The 9th European Workshop on Structural Health Monitoring, 10-23 July 2018*. United Kingdom
- Pappas, A., D'Ayala, D., Antonini, A., & Raby, A. (2018). Rock mounted iconic lighthouses under extreme wave impacts: Limit Analysis and Discrete Element Method. *The 9th International Conference on Computational Methods (ICCM2018) – Rome, Italy*.
- Pappas, A., D'Ayala, D., Antonini, A., & Raby, A. (2018). Finite element modelling and limit analysis of Fastnet lighthouse under impulsive ocean waves. *The International Conference on Structural Analysis of Historical Constructions (SAHC 2018) – Cusco, Peru*.
- Brownjohn, J., Raby, A., Bassitt, J., Antonini, A., Hudson, E., & Dobson, P. (2018). Experimental modal analysis of British rock lighthouses. *Marine Structures*, 62, 1–22. <https://doi.org/10.1016/j.marstruc.2018.07.001>
- Antonini, A., Raby, A., Brownjohn, J. M. W., Pappas, A., & D'Ayala, D. (2019). Survivability assessment of Fastnet lighthouse. *Coastal Engineering*. <https://doi.org/10.1016/j.coastaleng.2019.03.007>
- Raby, A., Antonini, A., Pappas, A., Dassanayake, D., Brownjohn, J., D'Ayala, D., (2019). Wolf Rock lighthouse: past developments and future survivability under wave loading. *Philosophical Transactions of the Royal Society A: Mathematical Physical and Engineering Sciences*, 377(2155), <http://dx.doi.org/10.1098/rsta.2019.0027>
- Raby, A., Antonini, A., Brownjohn, J., D'Ayala, D., (2019). Environmental loading of heritage structures. *Philosophical Transactions of the Royal Society A: Mathematical Physical and Engineering Sciences*, 377(2155), <https://doi.org/10.1098/rsta.2019.0276>
- Dassanayake, D.T., Raby, A. and Antonini, A. (2019), Physical Modelling of the Effect of Shoal Geometry on Wave Loading and Runup on a Cylinder, In: *Proceedings of ASCE Coastal Structures Conference*, Hannover, Germany.
- Dassanayake, D.T., Raby, A. and Antonini, A. (2019), Efficacy of Analysis Techniques In Assessing Broken Wave Loading On A Cylinder Upon A Shoal, In: *Proceedings of the 38th International Conference on Ocean, Offshore and Arctic Engineering – OMAE 2019*, Glasgow, Scotland, UK.



# Questions ?

STORMLAMP project

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