



# Prediction of Field Sand Cyclic Resistance in terms of Relative State Parameter Index using Numerical Experiments

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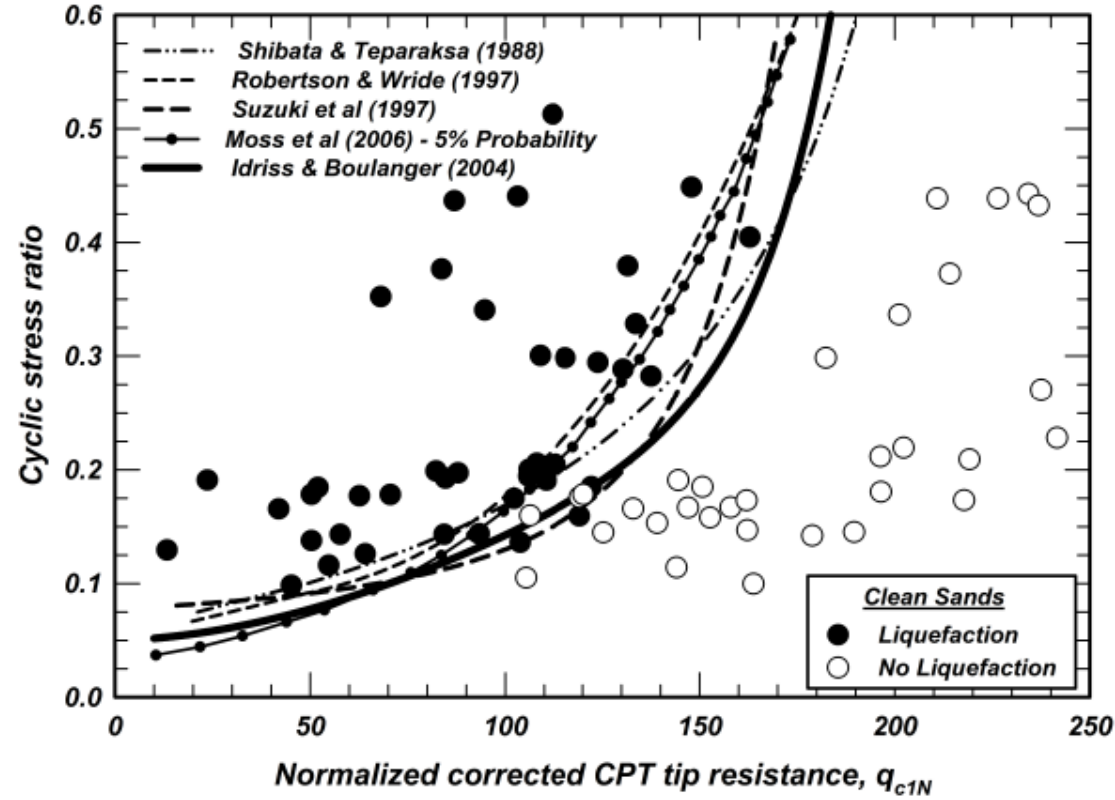
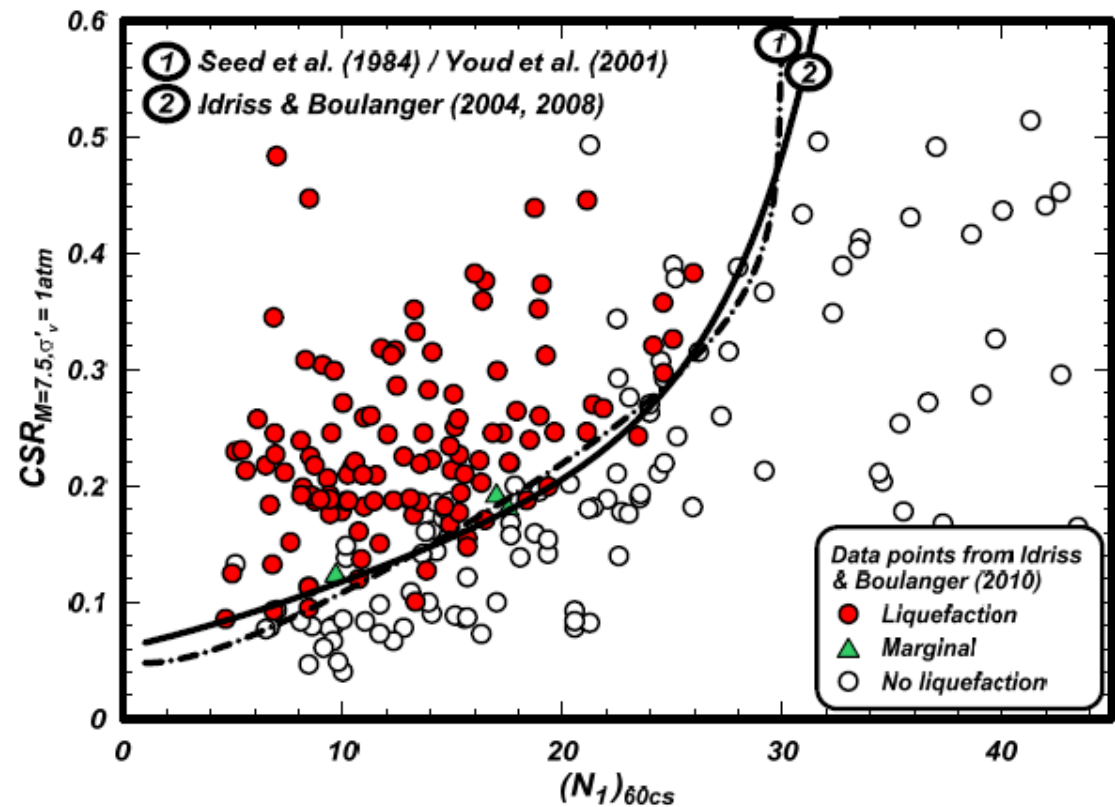
Itasca Consulting Group, Inc  
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# Outline

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- Why numerical simulations
- Model validations
- Numerical experiments

# “Simplified Procedure for Liquefaction Triggering”



(Boulanger & Idriss 2014)

# “Simplified Procedure for Liquefaction Triggering”

- **CSR** (Cyclic Stress Ratio): seismic demand:

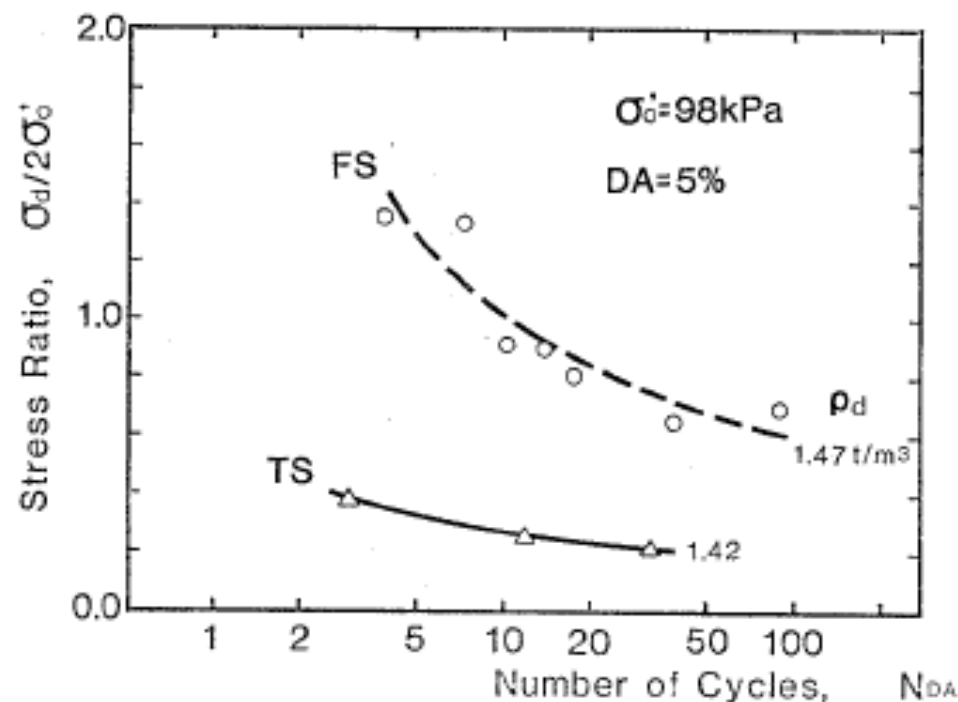
$$CSR = (\tau_{av} / \sigma'_{v0}) = 0.65(a_{max} / g)(\sigma_{v0} / \sigma'_{v0})r_d$$

- **CRR** (Cyclic Resistance Ratio): the capacity of the soil to resist liquefaction:

CRR from field tests (CPT, SPT, Vs) – state-of-practice

- **FS** =  $(CRR_{7.5} / CSR) \times MSF$

# Lab test data, then which sample?



(After Yoshimi et al 1984)

Yoshimi et al (1984) showed that undrained cyclic strength of **triple-tube samples** was ~30%, and **reconstituted samples** was 30~60%, of that of **frozen samples** (supposed close to field conditions).

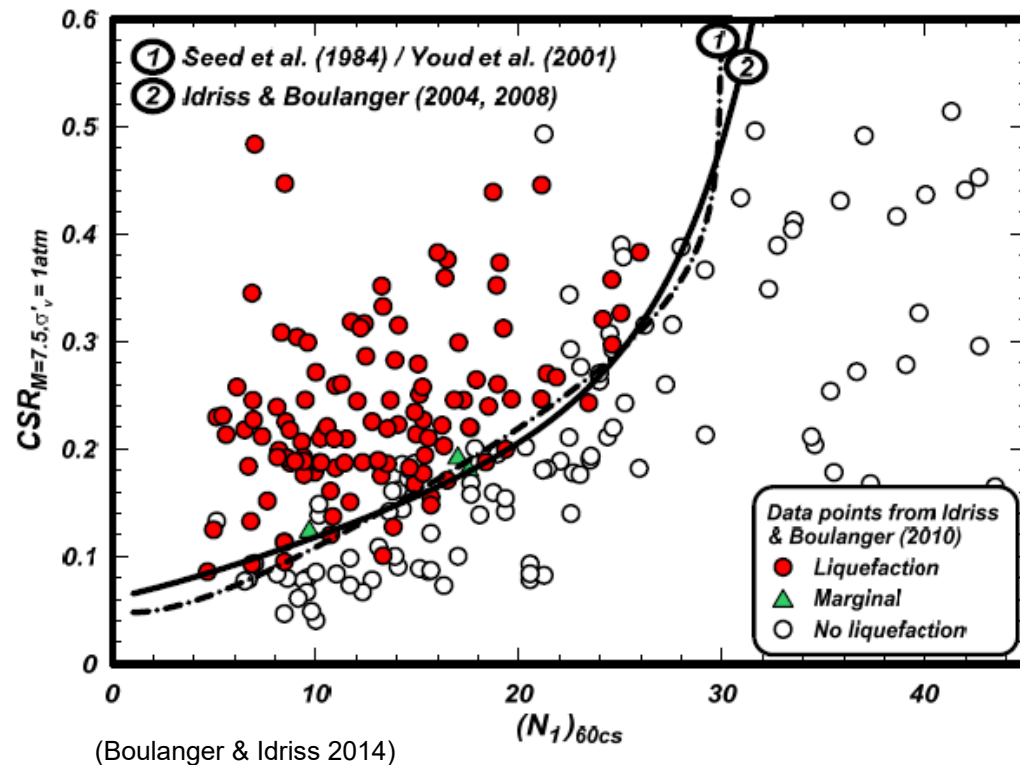
Contrary to rocks, cyclic strength of sands from lab is **lower** than that in field.

# Why **CRR** not from lab experiments?

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- “In-situ stress states generally cannot be re-established in the lab, and **sampling techniques are too disturbed to yield meaningful results**” (Youd et al 2001).
- Specialized sampling technique, i.e. ground freezing, is high-costed and not practical.
- So it should not be assumed that lab-based parameters are directly applicable to in-situ soil conditions.

# How to represent the field sand:



The CRR curve based on the “simplified procedure” does not correspond to a **specific** field sand but is **statistically** derived from many field cases.

It is possible to simulate numerically a **SCRF Sand** (Standard Cyclic Resistance Field sand) that liquefies exactly in 15 uniform cycles under DSS (direct simple shear) loading with an initial overburden stress of 100 kPa.

# Practice-orientated constitutive model:

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- Models heavily relying on high-quality lab-tests (or apparent discrepancies to field-based empirical formula) are not practical.
- In recent years, practice-oriented constitutive models consistent with this simplified procedure are increasingly appealing to engineers.
- General 3D: **P2PSand** (available from FLAC3D v7).



# How to represent the field sand:

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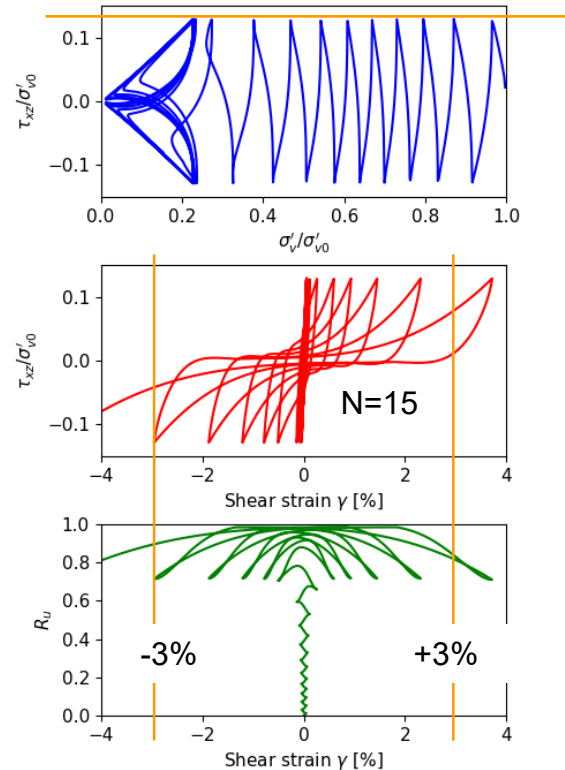
In P2PSand Model, the default parameters are calibrated for the **SCRF Sand** ) :

- Undrained DSS single-zone simulations
- Initial  $\sigma'_{v0} = 100$  kPa,  $K_0 = 0.5$  and no static shear stress.
- 15 cycles are required to reach liquefaction when CSR is equal to a selected standard CRR, see e.g., Youd et al. (2001).
- Liquefaction occurs when the peak shear strain first reaches a 3% amplitude.

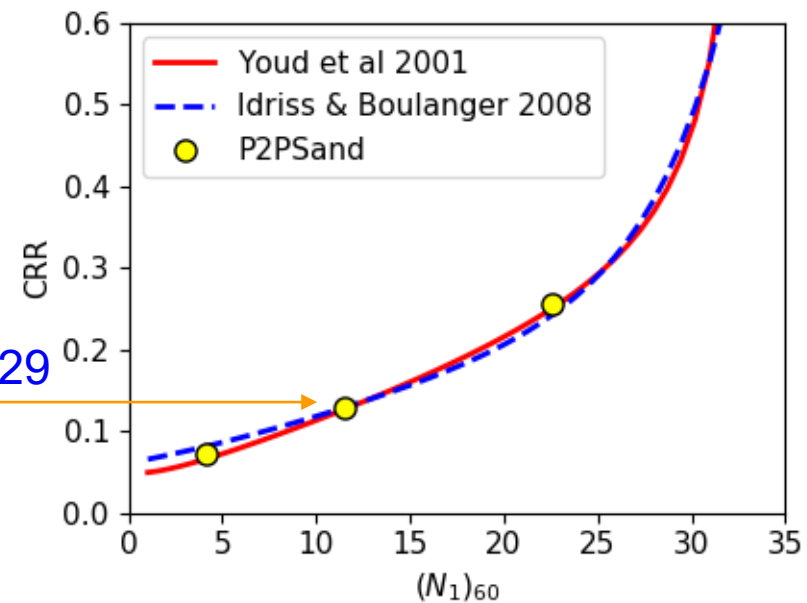
# “Standard” single-zone numerical example

- An example in FLAC3D v7 manual: Dynamic\CyclicUndrainedDirectSimpleShear

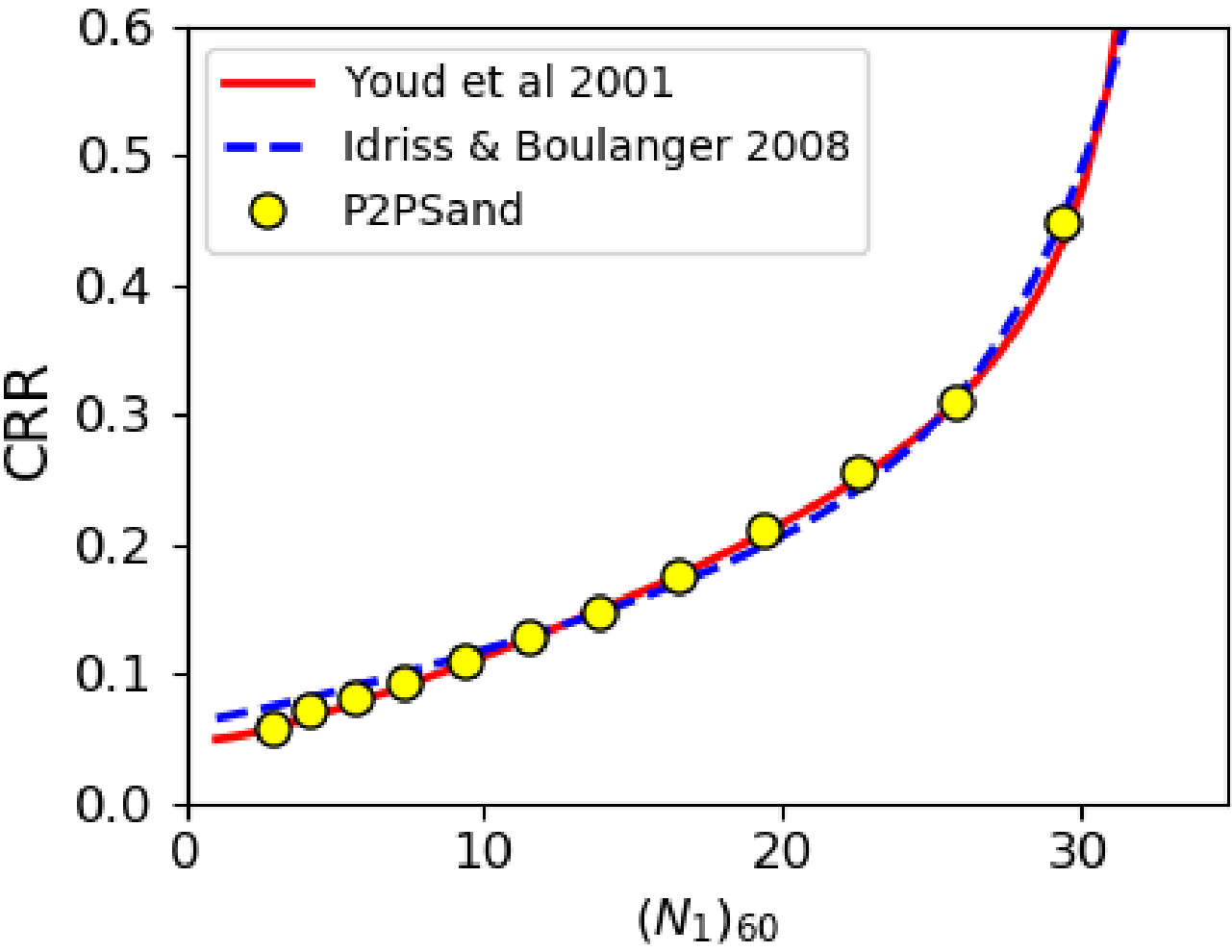
CSR=0.129



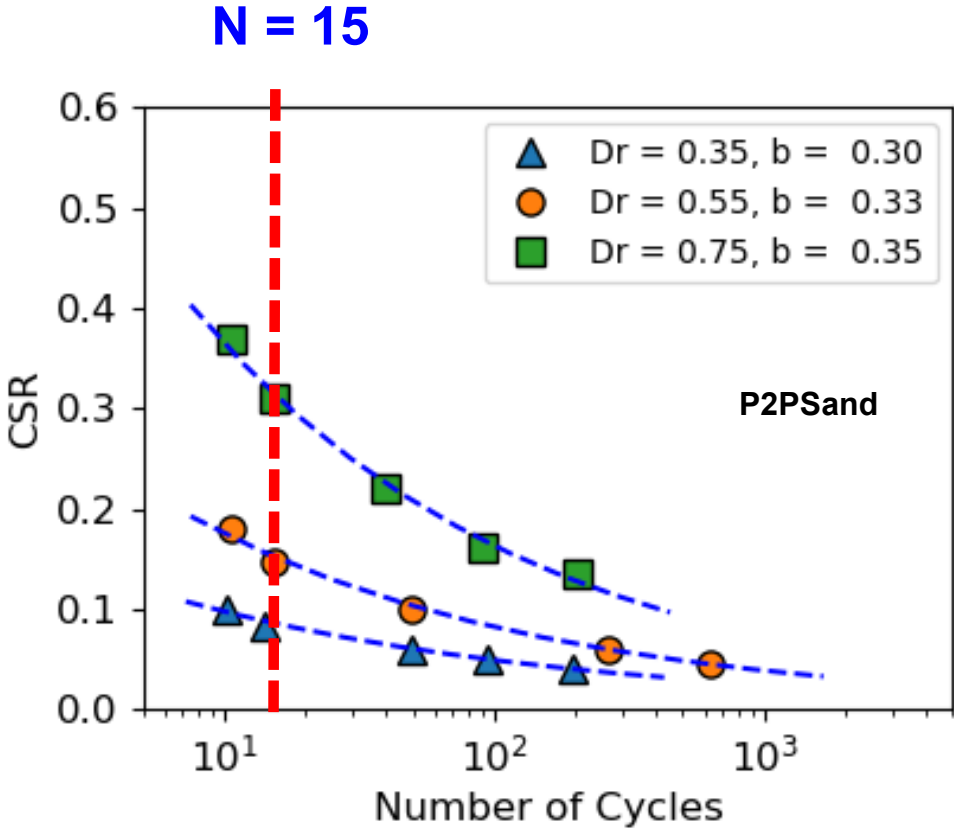
CSR=0.129



# CRR

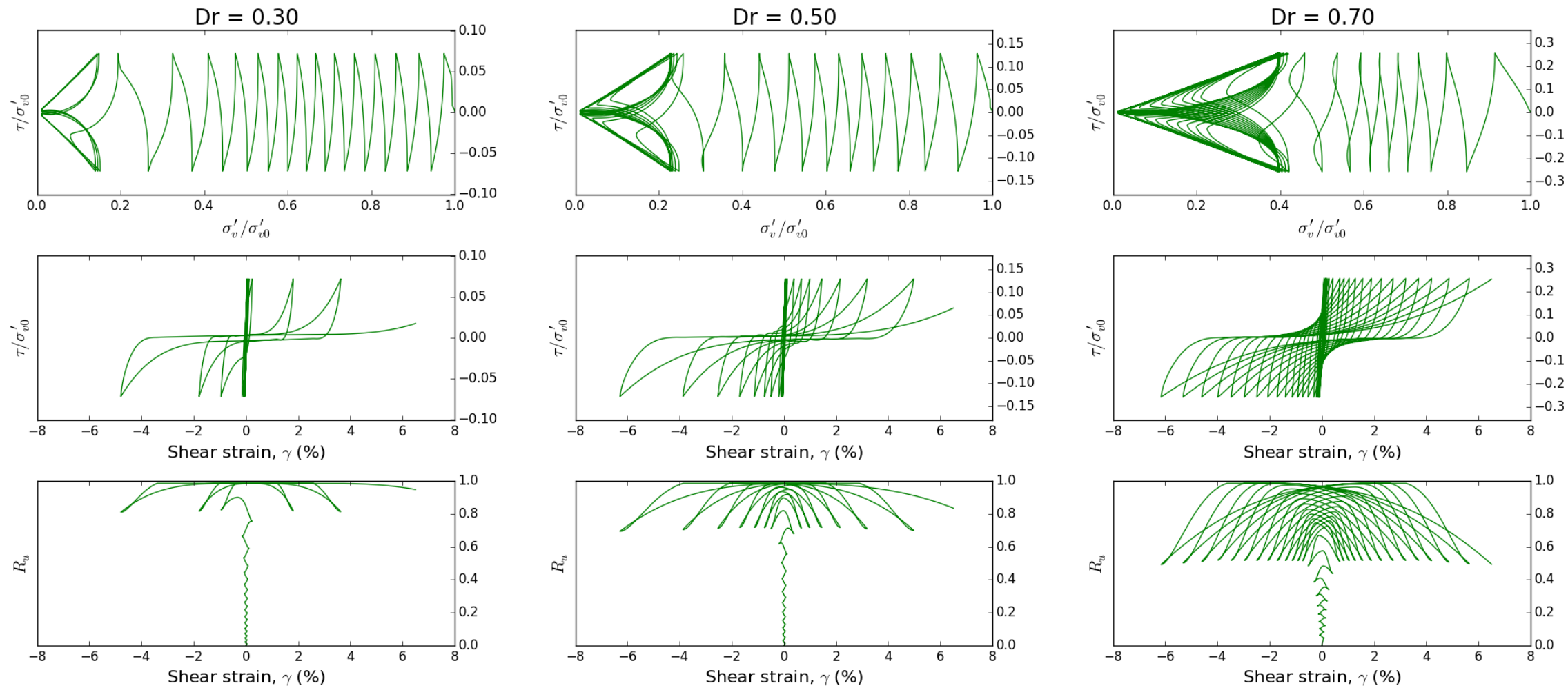


# CSR-N (Number of Cycles)



If too steep, it over-estimates CSR for  $M > 7.5$  (not conservative) & under-estimates CSR for  $M < 7.5$  (overly-conservative).

# DSS cyclic simulation



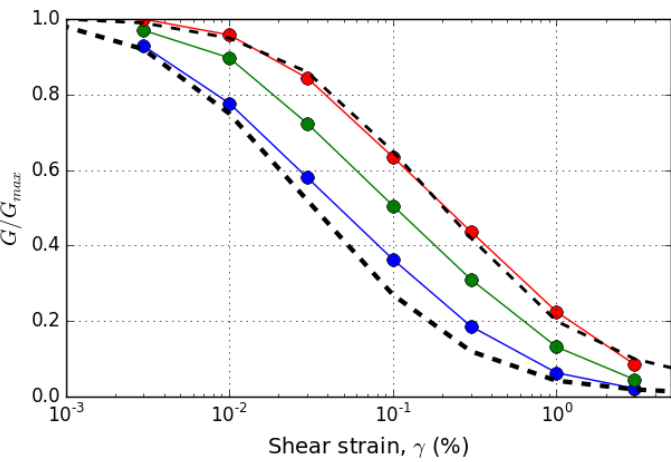
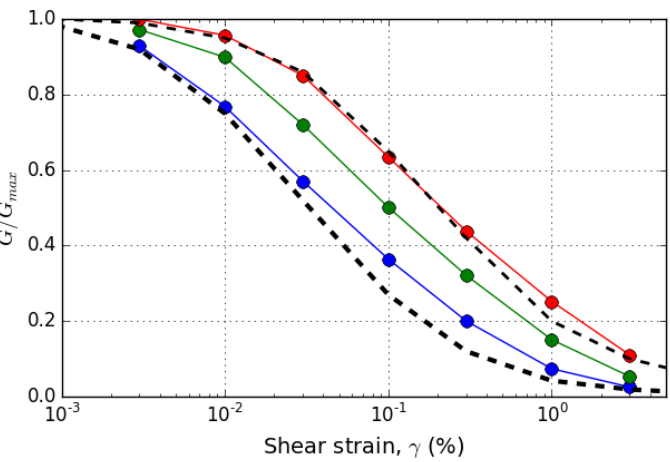
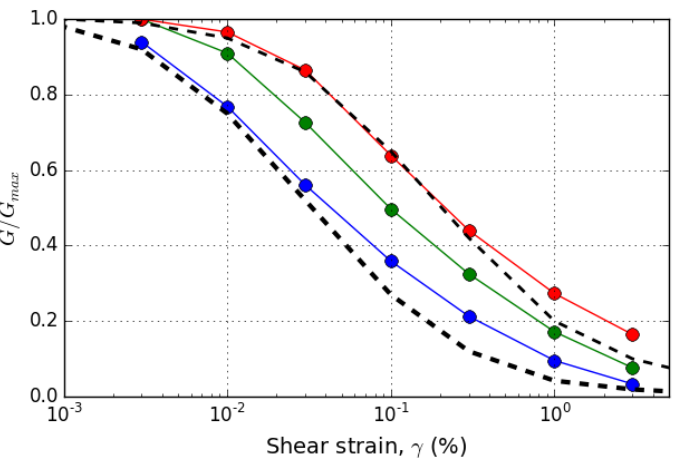
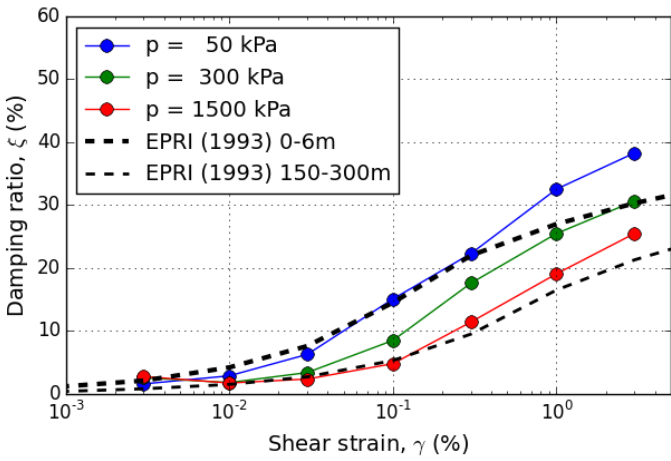
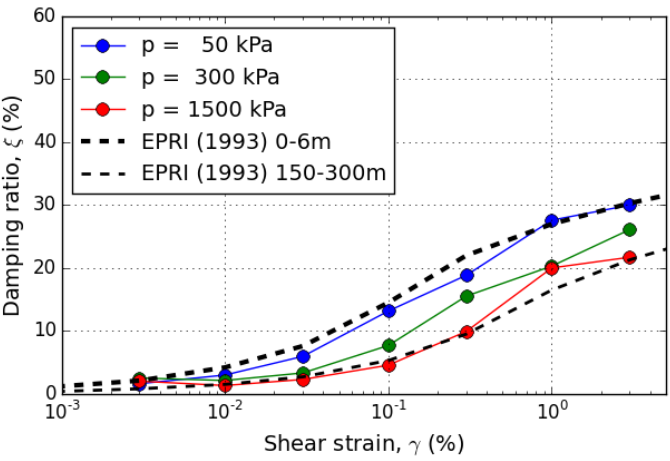
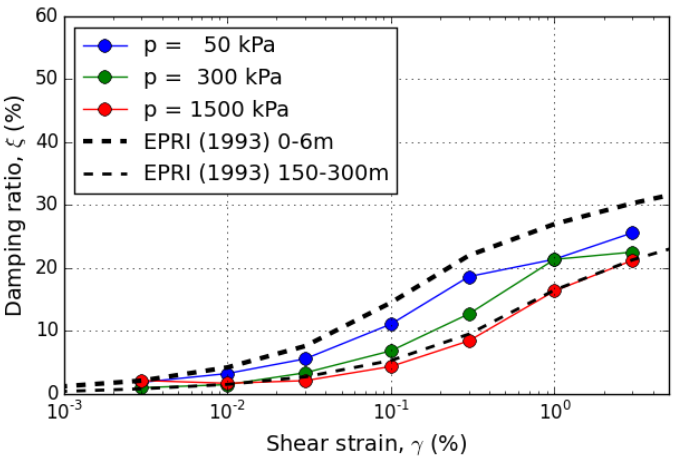
# $G/G_{max}$ & damping

## constant-p triaxial test simulation

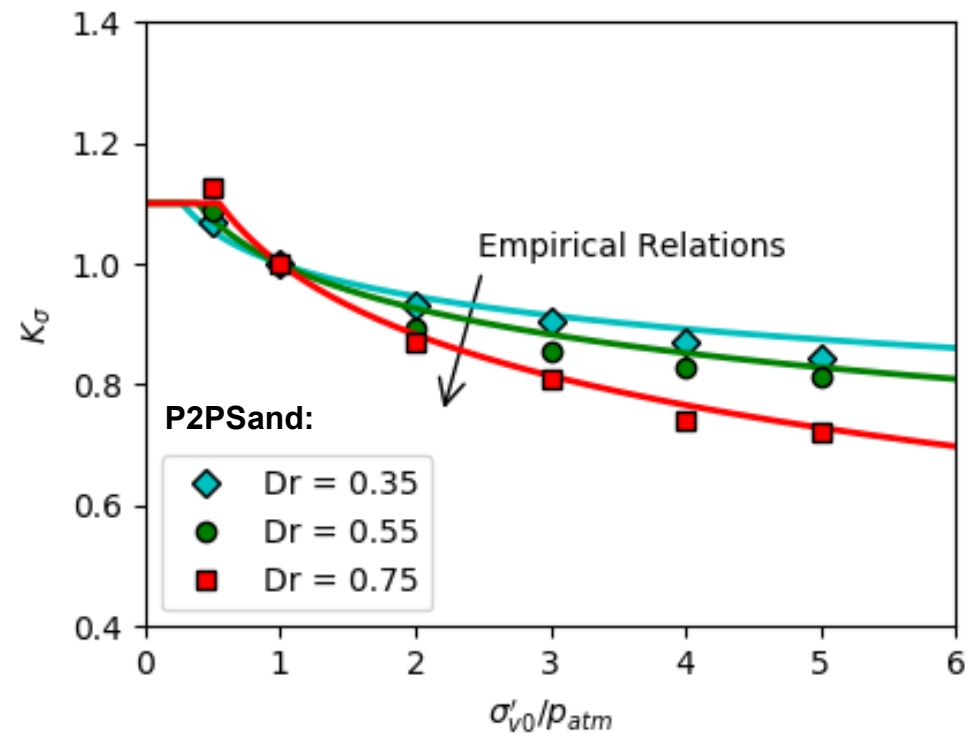
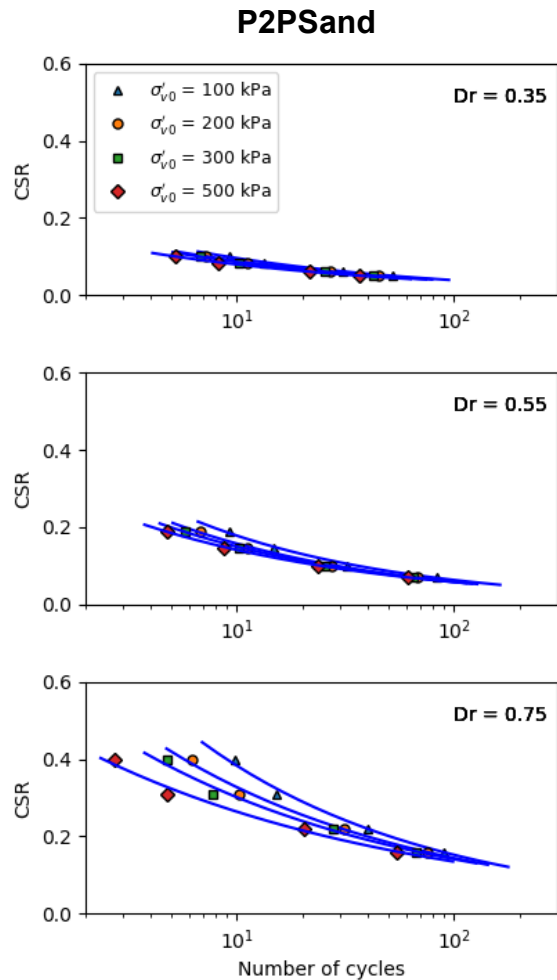
Dr = 0.35

Dr = 0.55

Dr = 0.75



# K $\sigma$ effect



# SCRF Sand **statistically** stands for field sand:

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Calibrated parameters are good for:

- CRR
- CSR vs N
- General Cyclic Curves
- G/Gmax & Damping vs Shear Strain
- $K_\sigma$  Effect

Can we predict something else meaningful for SCRF Sand purely by numerical experiments?



# 120 numerical DSS experiments:

```
csrdict = {0.75 : [0.400, 0.311, 0.220, 0.160],
           0.65 : [0.280, 0.212, 0.160, 0.110],
           0.55 : [0.190, 0.147, 0.100, 0.070],
           0.45 : [0.130, 0.109, 0.080, 0.060],
           0.35 : [0.100, 0.084, 0.060, 0.050]}
```

```
pv0list = [50, 100, 200, 300, 400, 500]
```

```
for dr0, csrlist in sorted(csrdict.items()) :
    for pv0 in pv0list :
        for csr in csrlist :
            it.command("model new")
            it.fish.set('dr0', dr0)
            it.fish.set('csr', csr)
            it.fish.set('Sv0', pv0)
            it.command("call 'dss_cyc_ud_n.f3dat' ")
```

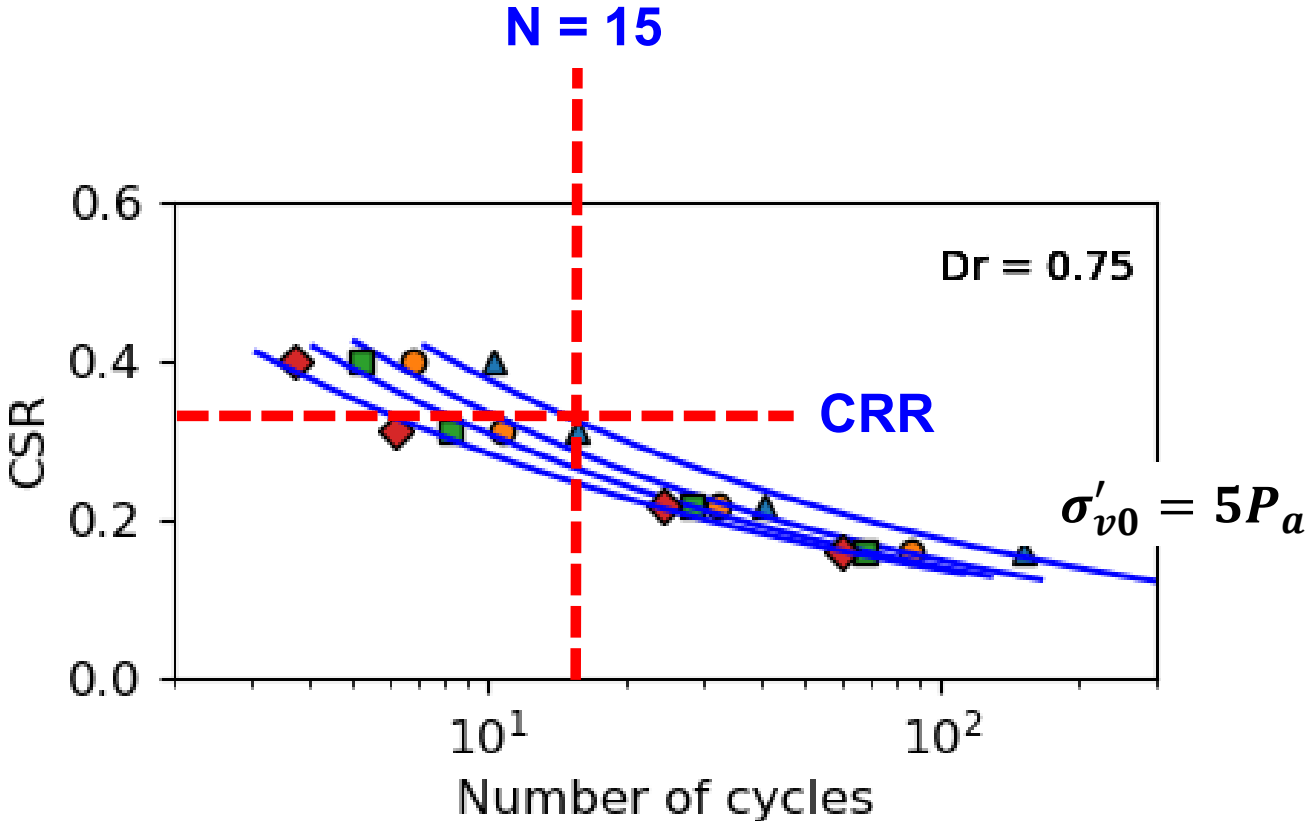
- **5** relative densities:  $Dr = 0.35, 0.45, 0.55, 0.65, 0.75$
- **6** initial over-burden stresses:  
 $\sigma'_{v0}/P_{atm} = 0.5, 1, 2, 3, 4 \text{ and } 5$
- **4** CSRs

Python scripts in FLAC3D  
do the job easily!



# Post-processing numerical data :

5×6 CRR vs ( $D_r$ ,  $\sigma'_{v0}$ )

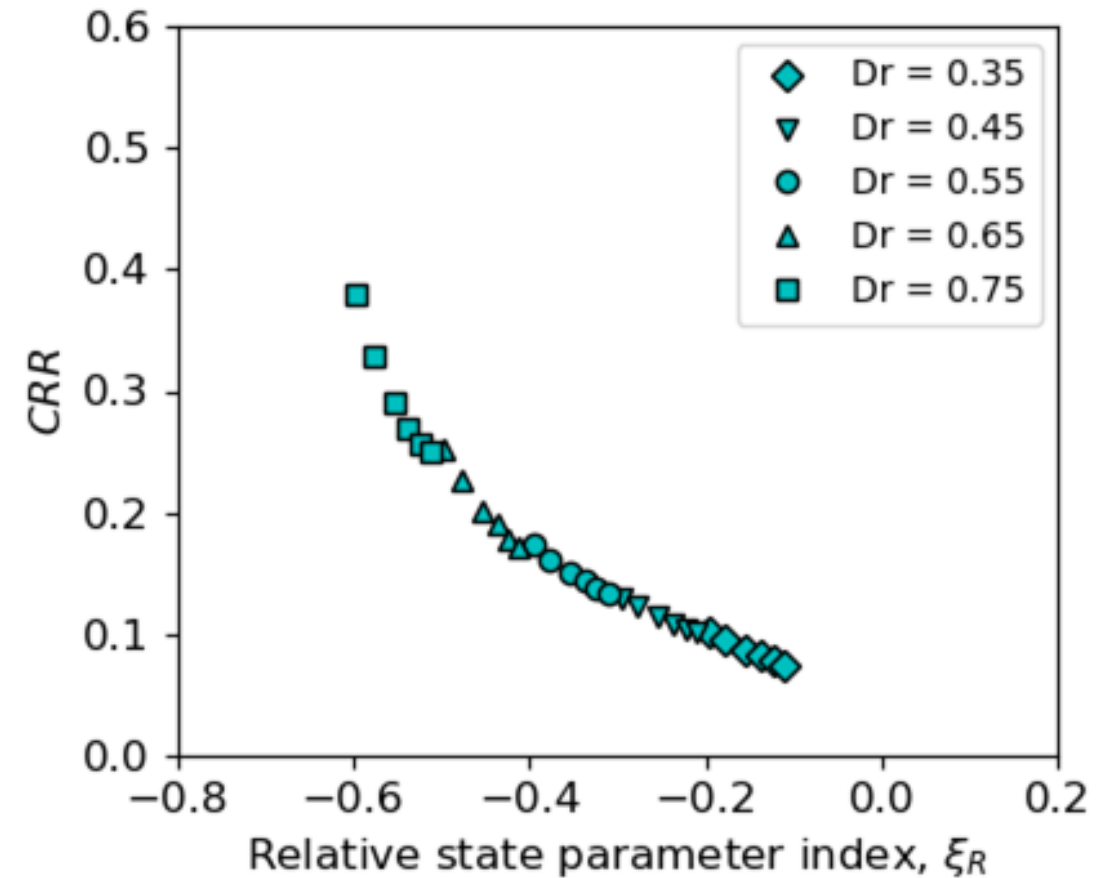


## Post-processing numerical data :

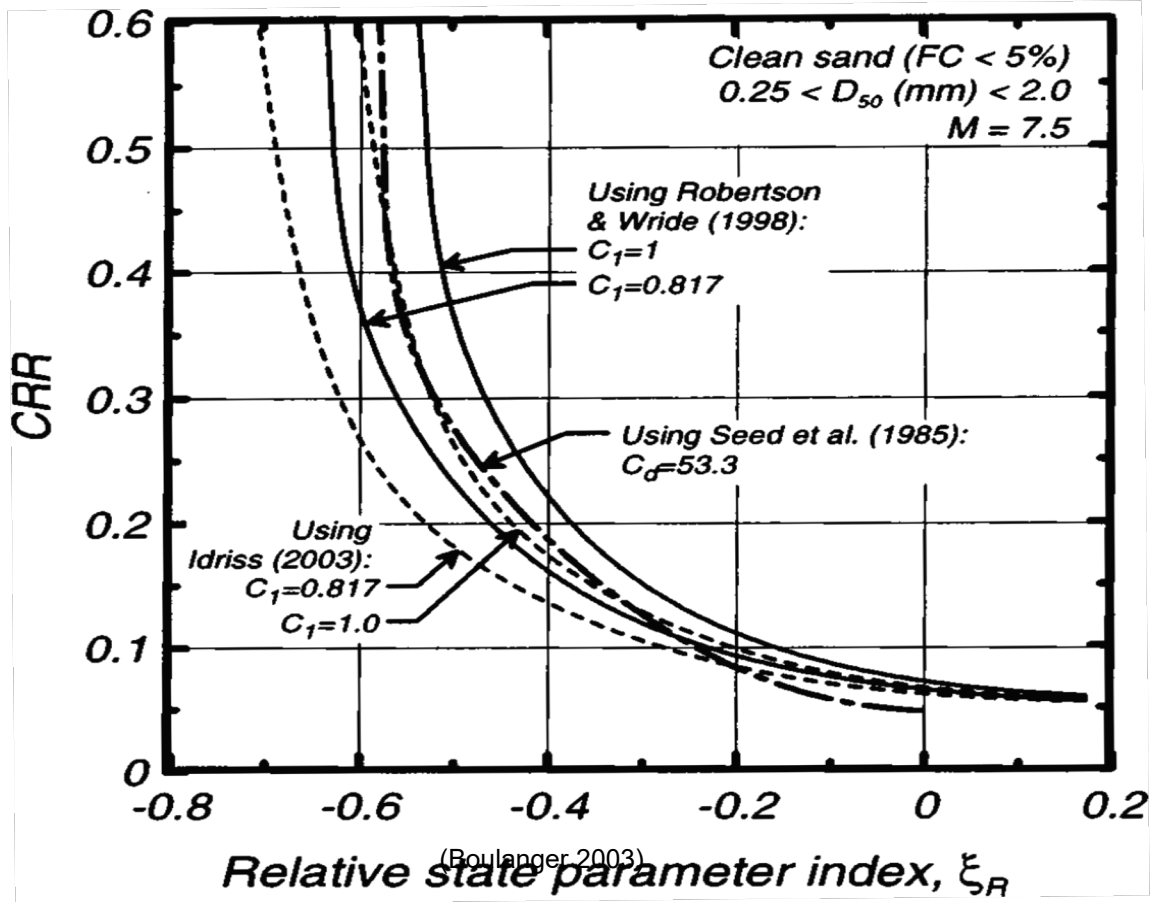
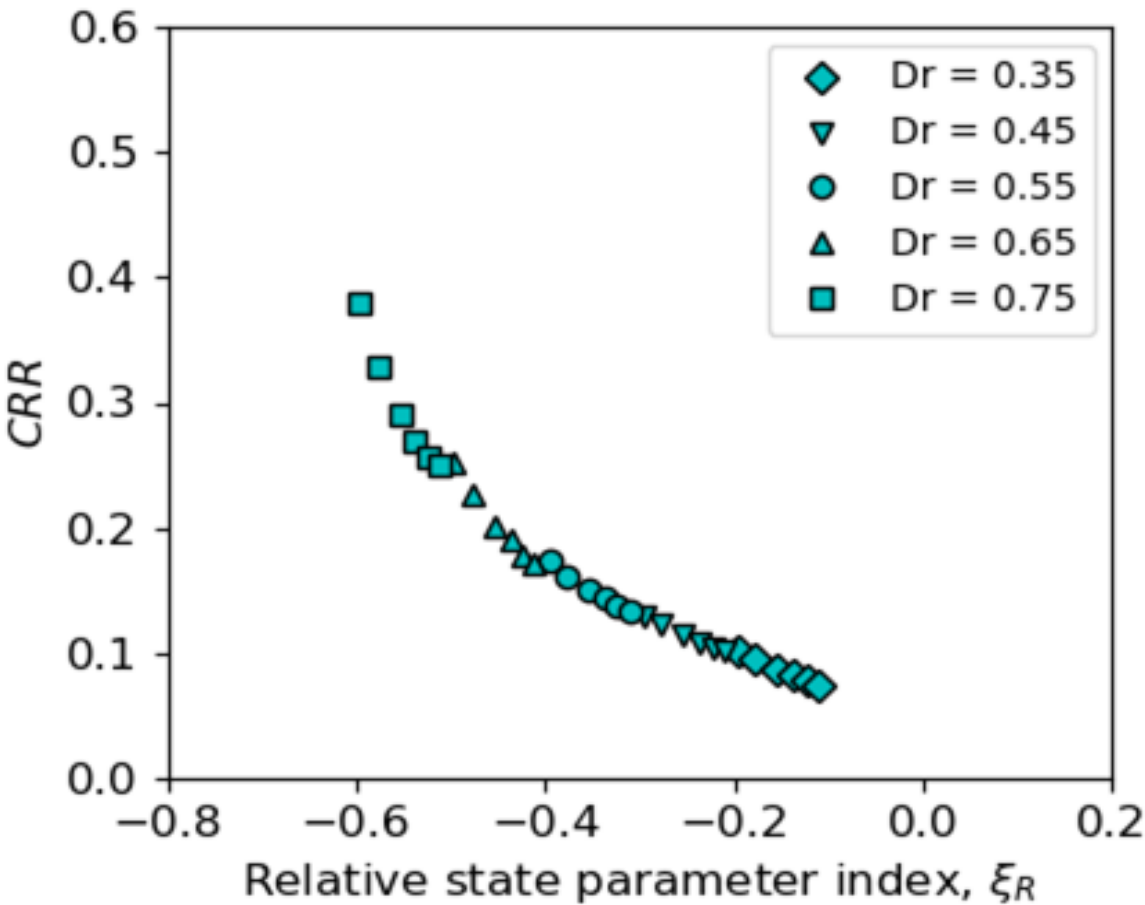
- Can we use one Index to represent ( $D_r$ ,  $\sigma'_{vn}$ ) to correlate CRR?

- Relative State Parameter Index:

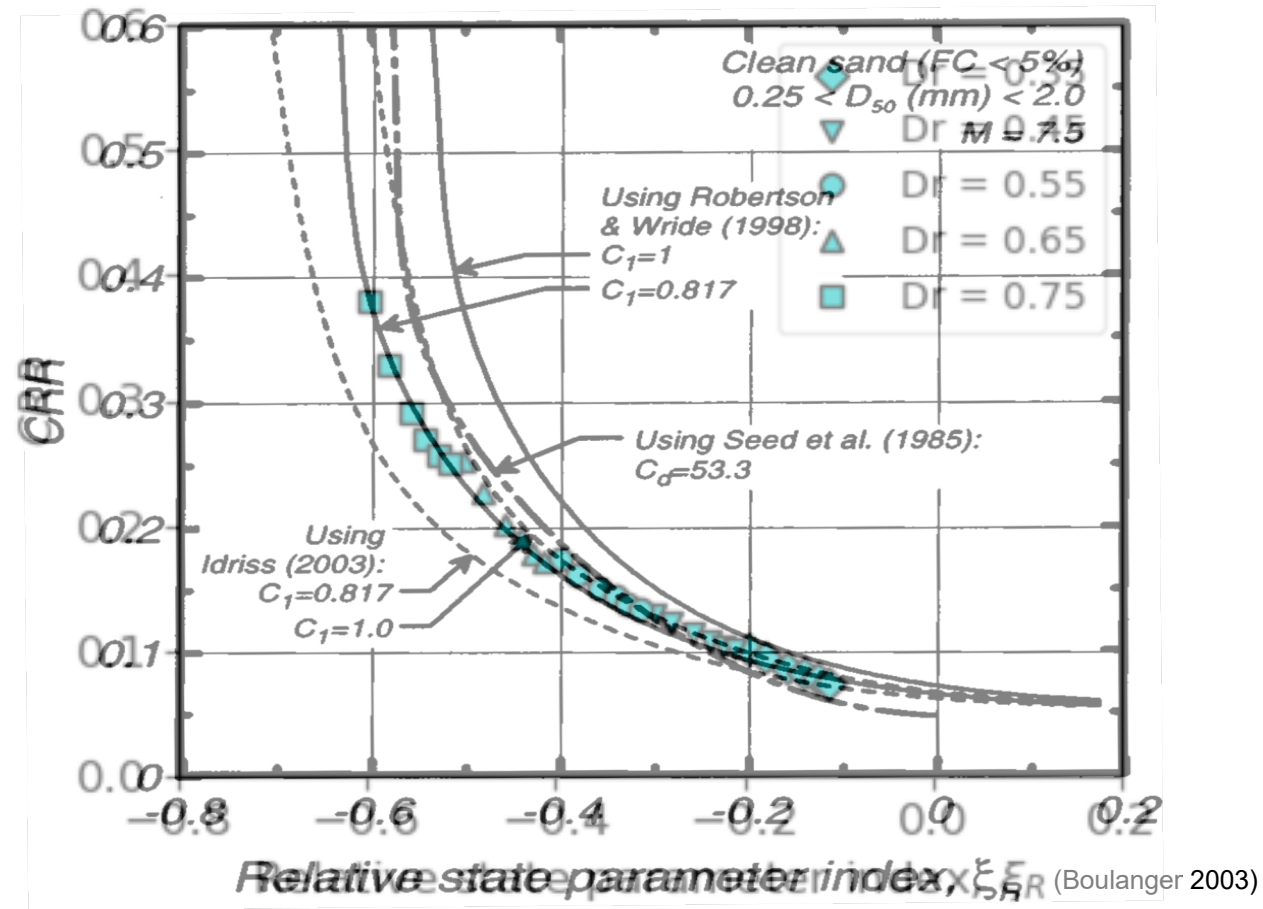
$$\xi_R = D_{rc} - D_r$$



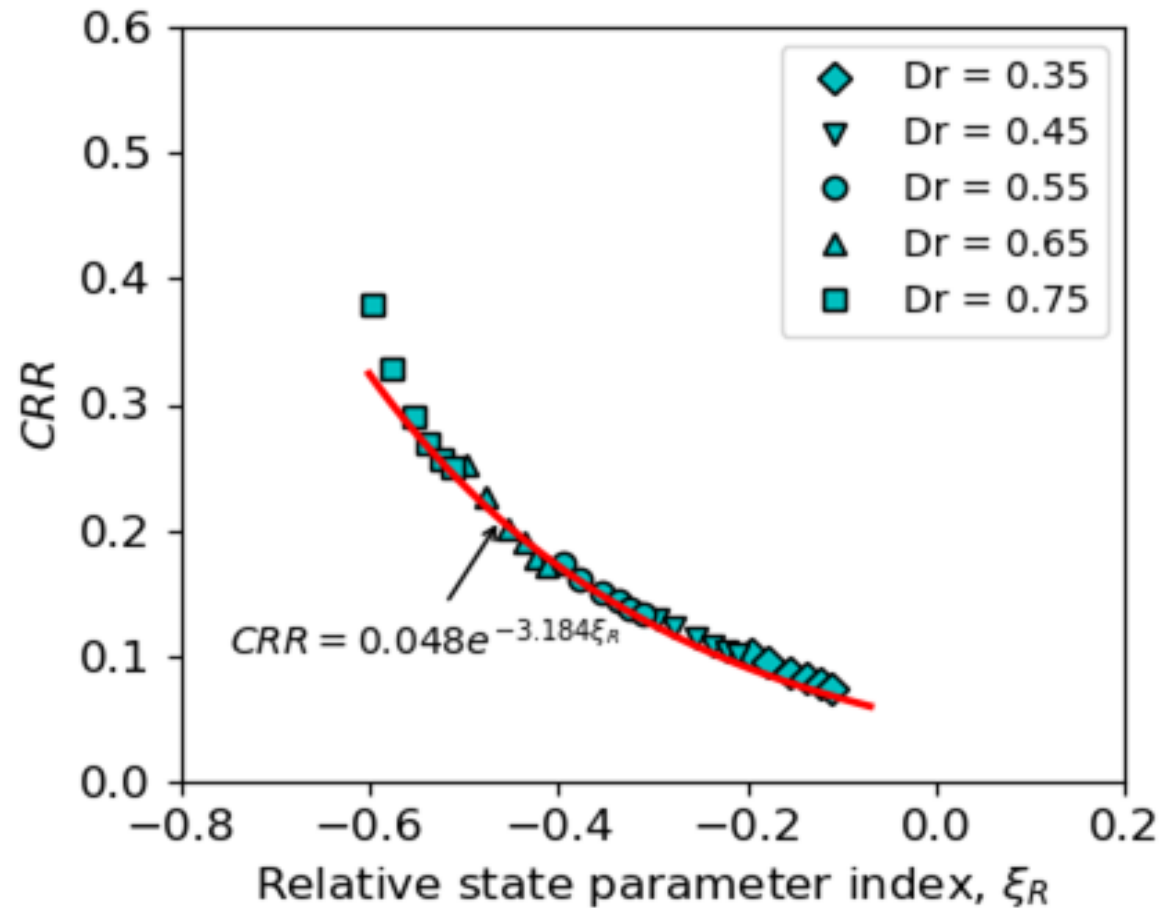
# Compare with field data



# Compare with field data, II



# Empirical relation purely derived from numerical experiments



- A simple power relation
- $K\sigma$  effect intrinsically included

# Summaries

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- Default properties of P2PSand model are compatible to SCRF Sand.
- Purely numerical cyclic DSS experiments using P2PSand model with various combinations of initial ( $D_r$ ,  $\sigma'_{v0}$ ) are performed.
- Numerical experiment results are validated by the results derived from field conditions.
- Numerical results suggest a simple power correlation between CRR vs  $\xi_R$  (relative state parameter index) for clean field sands.

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# Thank You!